

## LETTERS

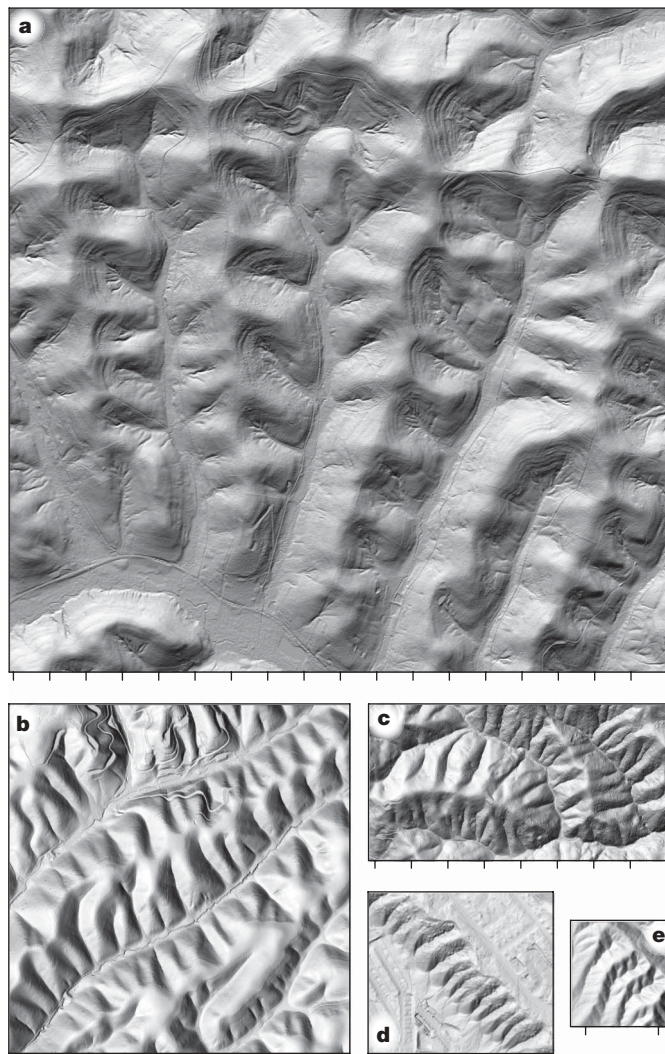
## Formation of evenly spaced ridges and valleys

J. Taylor Perron<sup>1</sup>, James W. Kirchner<sup>2,3,4</sup> & William E. Dietrich<sup>2</sup>

One of the most striking examples of self-organization in landscapes is the emergence of evenly spaced ridges and valleys<sup>1–6</sup>. Despite the prevalence of uniform valley spacing, no theory has been shown to predict this fundamental topographic wavelength. Models of long-term landscape evolution can produce landforms that look realistic<sup>7–9</sup>, but few metrics exist to assess the similarity between models and natural landscapes. Here we show that the ridge–valley wavelength can be predicted from erosional mechanics. From equations of mass conservation and sediment transport, we derive a characteristic length scale at which the time-scales for erosion by diffusive soil creep and advective stream incision are equal. This length scale is directly proportional to the valley spacing that emerges in a numerical model of landform evolution, and to the measured valley spacing at five field sites. Our results provide a quantitative explanation for one of the most widely observed characteristics of landscapes. The findings also imply that valley spacing is a fundamental topographic signature that records how material properties and climate regulate erosional processes.

The spacing between adjacent ridges and valleys is a fundamental dimension of hilly topography<sup>1–6</sup>. Even a casual observer can see from an aeroplane window that ridges and valleys in many landscapes appear to be uniformly spaced (Fig. 1), even where their locations are not controlled by bedrock structure. Indeed, uniform spacing is often most clearly visible where bedrock is mechanically homogeneous<sup>10</sup>. This implies that the characteristic ridge–valley wavelength is an emergent property of the erosion and sediment transport processes that shape the landscape. Any theory for the long-term evolution of Earth's surface should be able to explain fundamental landscape scales like the ridge–valley wavelength.

Some of the earliest theories of landscape evolution focused on the segmentation of landscapes into ridges (or, more generally, hillslopes) and valleys. Davis<sup>11</sup> and Gilbert<sup>10,12</sup> suggested that hillslopes are dominated by sediment transport mechanisms that smooth the land surface, and that hillslopes give way to valleys where water runoff becomes concentrated enough to outpace the smoothing processes and incise into the land surface. Later studies showed how this competition might lead to the development of evenly spaced valleys. Smith and Bretherton<sup>13</sup> demonstrated that a concave-up, erodible surface under a sheet of flowing water—a situation analogous to a freshly exposed soil embankment during a rainstorm—is unstable with respect to perturbations, with the shortest-wavelength topographic features growing fastest. This result implied no preferred wavelength. Subsequent studies found that if smoothing is introduced, either by diffusive processes<sup>14,15</sup> such as rain splash<sup>16</sup> or by the dispersive effects of the free water surface<sup>2</sup>, perturbations with an intermediate wavelength will grow fastest, forming incipient erosional rills with a characteristic spacing. Some studies additionally included a sediment transport threshold that encouraged the selection of an intermediate wavelength<sup>2,5</sup>.



**Figure 1 | Uniform valley spacing.** Shaded relief maps of representative sections of the study sites. **a**, Eaton Hollow, Pennsylvania. **b**, Gabilan Mesa, California. **c**, Napa Valley, California. **d**, Point of the Mountain, Utah. **e**, Dragon's Back, California. Tick spacing is 200 m. For clarity, **d** and **e** have been enlarged by a factor of two relative to **a–c**. Vegetation has been filtered out of the data to reveal the underlying topography. Eaton Hollow data are from the State of Pennsylvania PAMAP program; Point of the Mountain data are from the State of Utah Automated Geographic Reference Center; California data are from the National Center for Airborne Laser Mapping (NCALM).

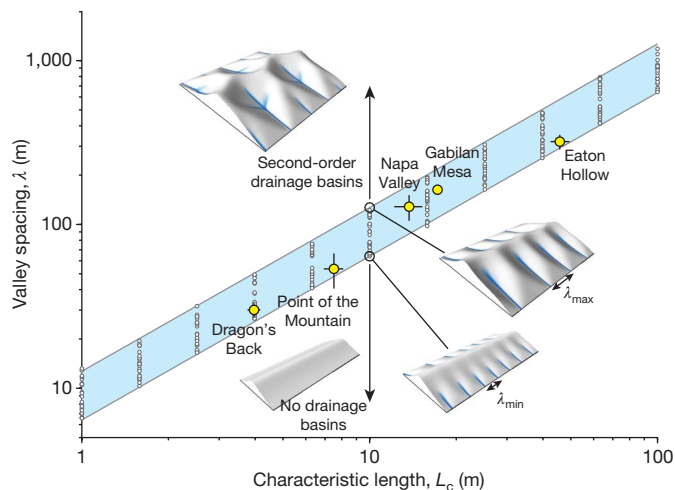
<sup>1</sup>Department of Earth, Atmospheric and Planetary Sciences, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139, USA. <sup>2</sup>Department of Earth and Planetary Science, University of California, Berkeley, California 94720, USA. <sup>3</sup>Swiss Federal Institute for Forest, Snow and Landscape Research (WSL), Birmensdorf, Switzerland. <sup>4</sup>Department of Environmental Sciences, Swiss Federal Institute of Technology (ETH), Zürich, Switzerland.

These studies considered incipient channelization of a surface by a sheet of flowing water, and cannot be used to predict the dimensions of large-scale landforms like those in Fig. 1. Numerical models based on a similar competition between stream channel incision and diffusive soil creep have been used to explore the long-term evolution of such landforms, including the factors controlling the upslope drainage area at which hillslopes transition into valleys<sup>8,9,17–21</sup>, but not the characteristic ridge–valley wavelength. Moreover, comparisons between models and natural landscapes have been hampered by the scarcity of high-resolution topographic data and the difficulty of measuring the long-term rates of erosion and transport processes in the field.

To investigate the factors that control valley spacing, we developed a numerical model (Methods, Supplementary Information) that simulates landscape evolution under the combined influence of soil creep (here used to mean downslope soil flux due to abiotic and biotic processes, linearly dependent on the local surface gradient) and stream incision. The transient evolution of the model illustrates how uniform valley spacing emerges over time (Supplementary Information). As the topography evolves from a randomly rough, horizontal initial surface, irregularly spaced incipient valleys form at the boundaries and begin to grow by lengthening and widening. Competition for drainage area (a proxy for water flux) stunts the growth of valleys that are too small or spaced too closely together. This transient evolution is similar in many respects to early conceptual models of drainage network development<sup>10,16,22</sup>. The model eventually reaches a deterministic equilibrium in which the spacing of valleys is approximately uniform.

Nonlinearities in the governing equation (equation (1)) preclude an analytic solution for the equilibrium topography, so we used dimensional analysis to explore how the erosion and transport parameters control the valley spacing. The governing equation is a nonlinear advection–diffusion equation, and we derived a quantity analogous to a Péclet number,  $Pe$  (equation (2)), that expresses the relative magnitudes of the advective stream incision and diffusive soil creep mechanisms shaping the landscape. When  $Pe$  is small, the landscape is dominated by creep, and forms a smooth slope with no valleys. When  $Pe$  is large, the landscape is dominated by stream incision, and forms networks of branching valleys. Setting  $Pe = 1$  yields a characteristic length scale,  $L_c$  (equation (3)), at which the characteristic timescales for stream incision and creep are equal. Numerical modelling has shown that  $L_c^2$  is approximately the drainage area at which the topography transitions from a concave-down, creep-dominated hillslope to a concave-up, stream-incision-dominated valley<sup>23</sup>. We computed equilibrium model solutions using parameters that give a range of values for  $L_c$ , and measured valley spacing,  $\lambda$ , by identifying the dominant peaks in the two-dimensional Fourier spectra of the simulated topography<sup>6,23</sup>. For a given value of  $L_c$ , a range of valley spacing is possible because a range of slope lengths can give rise to first-order valleys (valleys that do not branch), and longer slopes form more widely spaced valleys (Fig. 2). The range of slope lengths is limited, however, because slopes that are too long will become dissected by branching valleys, and slopes that are too short will remain smooth and undissected. The minimum and maximum valley spacings are directly proportional to  $L_c$ , as shown in Fig. 2.

To test whether this theoretical prediction is consistent with valley spacing in natural landscapes, we measured  $L_c$  in five landscapes in the United States that have different valley spacings: Gabilan Mesa and Napa Valley in the California Coast Ranges, the Dragon's Back pressure ridge along the San Andreas fault in the Carrizo Plain, California, Point of the Mountain in Salt Lake Valley, Utah, and Eaton Hollow in southwestern Pennsylvania. All five sites display uniform valley spacing (Fig. 1, Table 1) that is not determined by structural heterogeneities in the underlying bedrock. Gabilan Mesa is an oak savannah with a Mediterranean climate, and erosion of the moderately consolidated sandstones, siltstones and conglomerates of the Paso Robles Formation has formed valleys with a spacing of



**Figure 2 | Comparison of predicted and observed valley spacing.** Plot of valley spacing,  $\lambda$ , against the characteristic length scale,  $L_c$  (equation (3) in Methods), for first-order drainage basins. Each white circle represents the valley spacing in a single numerical model solution. The blue trend shows the range of possible valley spacings, which correspond to different slope lengths, for each value of  $L_c$ . Slope length was controlled by varying the width of the model grid in the direction normal to the main ridgeline. The minimum and maximum spacing for a given value of  $L_c$  correspond to the shortest and longest slopes that form first-order valleys. The expression for the blue trend is  $6.4L_c \leq \lambda \leq 12.7L_c$ . Insets are perspective views of numerical model solutions with the same  $L_c$  but different slope lengths, with valley bottoms shaded blue. Yellow points are the means for first-order valleys in the study sites. Error bars are one standard error of the mean.

$163 \pm 11$  m. Napa Valley has similar vegetation and climate, with valleys spaced at  $128 \pm 23$  m that have formed in sandstones and mudstones of the Franciscan Complex. Dragon's Back is a semi-arid grassland underlain by sediments of the Paso Robles Formation that are less consolidated than in Gabilan Mesa, with a valley spacing of  $30 \pm 3$  m. Point of the Mountain is a sand and gravel spit formed by Pleistocene Lake Bonneville, with a valley spacing of  $54 \pm 13$  m. Eaton Hollow is a temperate mixed forest underlain by horizontal beds of Permian and Pennsylvanian sandstone, shale, limestone and coal, with a valley spacing of  $321 \pm 33$  m. Valley spacings were measured from peaks in two-dimensional Fourier spectra derived from high-resolution laser altimetry maps<sup>6</sup>. Comparison with spectra for random surfaces with the same roughness characteristics as the observed topography<sup>6</sup> shows that valley spacing as uniform as that observed in the study sites is very unlikely to arise by chance ( $P < 0.001$ ).

Erosion and transport at all five sites are dominated by stream channel incision and by diffusive soil creep, which occurs mainly through bioturbation such as tree throw and rodent burrowing. Mean hillslope gradients are between 0.2 and 0.4, and evidence of landslides is rare. In Napa Valley, some of the areas surrounding our study site are steeper and have experienced landslides, but we avoided these areas in our analysis. Similarly, portions of Dragon's Back experience nonlinear creep and frequent landslides due to a spatial gradient in uplift rates<sup>24</sup>, but we restricted our analysis to the drainage basins farthest from the zone of maximum uplift, which are dominated by linear creep. The mechanically homogeneous substrates and the two dominant erosion and transport mechanisms conform to the simplifying assumptions behind the numerical model, making these sites suitable locations to test predictions of valley spacing.

An estimate of  $L_c$  for each landscape requires values for the constants that describe the long-term strengths of the erosional processes: soil diffusivity  $D$ , stream erosivity  $K$ , and drainage area exponent  $m$  (equation (3)). These parameters are difficult to measure directly because erosion is usually slow or episodic, and because present-day rates may not be representative of long-term rates. We



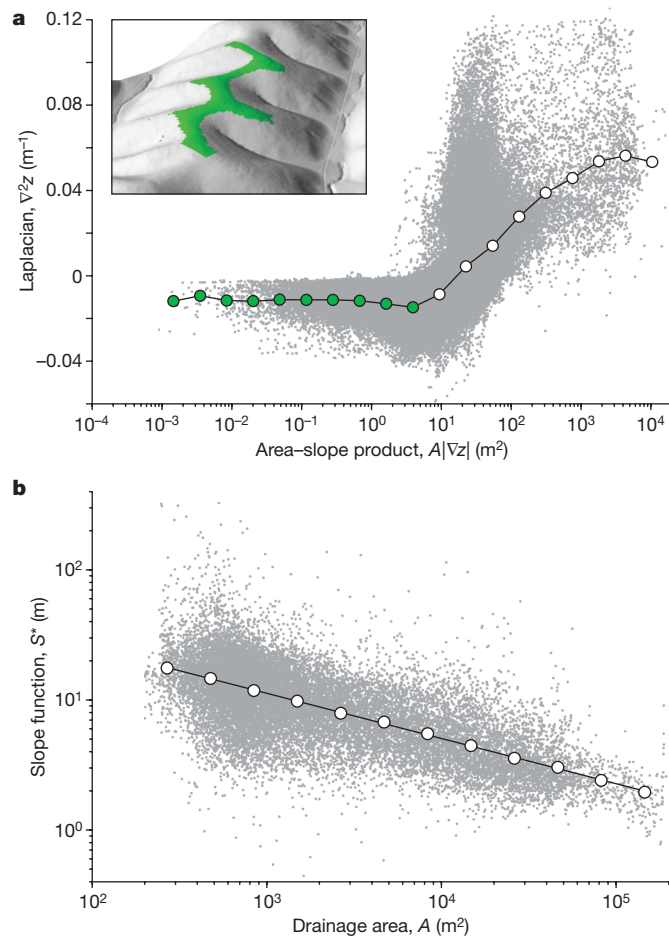
**Table 1 | Topographic measurements**

	$\nabla^2 z_h$ ( $10^{-3} \text{ m}^{-1}$ )	$D/K$ ( $\text{m}^{2m+1}$ )	$m$	$L_c$ (m)	$\lambda$ (m)	Mean annual precipitation* (m)
Dragon's Back	$-94 \pm 3$	$12 \pm 1$	$0.42 \pm 0.01$	$4.0 \pm 0.2$	$30 \pm 3$	0.23
Point of the Mountain	$-28 \pm 4$	$26 \pm 3$	$0.31 \pm 0.02$	$7.5 \pm 0.6$	$54 \pm 13$	0.50
Napa Valley	$-18.8 \pm 0.3$	$86 \pm 13$	$0.35 \pm 0.02$	$13.7 \pm 1.5$	$128 \pm 23$	0.93
Gabilan Mesa	$-11.8 \pm 0.4$	$124 \pm 3$	$0.35 \pm 0.003$	$17.2 \pm 0.4$	$163 \pm 11$	0.32
Eaton Hollow	$-5.5 \pm 0.1$	$802 \pm 82$	$0.37 \pm 0.01$	$46.0 \pm 3.4$	$321 \pm 33$	1.05

\*For the period 1971–2000. Data are from the PRISM Climate Group, Oregon State University, <http://prismclimate.org>.

therefore used the shapes of hilltops and stream profiles measured from high-resolution topography to solve for time-averaged values of  $D/K$  and  $m$  (Fig. 3, Methods).

The comparison in Fig. 2 shows that valley spacing is proportional to  $L_c$  across all five study sites, consistent with the predictions of the numerical model. This good agreement suggests that the two-process model, despite its simplifications, captures the mechanisms that exert the strongest influence on valley spacing in these landscapes. To demonstrate that this agreement is not an inevitable consequence



**Figure 3 | Measurement of model parameters from topography.** **a**, Plot of the Laplacian of elevation against the product of drainage area and slope for first-order drainage basins in Gabilan Mesa. Filled circles are means of log-transformed data within logarithmically spaced bins. On hilltops, where both drainage area and slope are small (green shading), the Laplacian is roughly constant, consistent with equilibrium topography (equation (4), Methods). The inset shows several representative hilltops. For clarity, the plot shows a random subsample of 25% of the raw data points. **b**, Plot of slope function (equation (5), Methods) against drainage area for stream profiles in the same basins. Filled circles are means of log-transformed data within logarithmically spaced bins, and the line is a least-squares fit to the binned data. Error bars showing one standard error of the mean for the filled circles are smaller than the symbols. Plots for all study sites are shown in the Supplementary Information.

of our procedure for measuring  $L_c$ , we performed the same topographic measurements in three landscapes shaped by erosional processes that are not well described by our model; the valley spacing in those landscapes is inconsistent with the inferred values of  $L_c$  (Supplementary Information).

Our measurements and the geology and climate of the study sites offer some insight into the differences in  $L_c$  and valley spacing. In our model, longer  $L_c$  and wider valley spacing can result from larger  $D$ , smaller  $K$ , or smaller  $m$  (equation (3)). Our topographic measurements (Table 1) indicate that the drainage area exponent  $m$  is similar for the five sites, and that the differences in valley spacing primarily reflect differences in  $D/K$ , the ratio of soil diffusivity to stream erosivity. Systematic variations in bedrock mechanical strength among the five sites further suggest that rock strength, which we expect to be negatively correlated with  $K$ , is a major source of variability in  $D/K$ . Sites with the least consolidated sediments (Dragon's Back and Point of the Mountain) have the narrowest valley spacing, sites with moderately consolidated sediments (Gabilan Mesa and Napa Valley) have intermediate spacing, and the site with the most competent bedrock (Eaton Hollow) has the widest valley spacing.

A comparison of precipitation rates at the five sites (Table 1) suggests that climate may also influence valley spacing: with the exception of Gabilan Mesa, wider valley spacing corresponds to greater present-day mean annual precipitation. One possible cause is the stream erosivity, which depends on drainage basin hydrology as well as on rock strength<sup>7–9,23</sup>. Although higher rainfall should increase streamflow, the dominant effect of precipitation in soil-mantled landscapes like those analysed here may be to reduce  $K$  by promoting vegetation growth and infiltration, thereby inhibiting overland flow erosion<sup>9</sup>. It also seems likely that more intense bioturbation in wetter environments leads to higher soil diffusivity<sup>9</sup>, an effect consistent with previous measurements<sup>25</sup> of  $D$  and with the observed correlation between precipitation and the hilltop curvature,  $\nabla^2 z_h$  (Table 1, Methods). Although we are at present unable to quantify the relative importance of these mechanisms, our observations suggest that valley spacing may serve as a topographic proxy for the combined effects of bedrock mechanical strength and climate on the relative magnitudes of different erosional processes.

It is notable that our theory closely predicts valley spacing in the five study sites even though it does not include a threshold for fluvial erosion. Soil cohesion and plant roots impart strength to the soil surface, such that very small flows may not exert enough stress to erode the underlying material. There is evidence that such thresholds influence the locations of fluvial channel heads<sup>26</sup>, and it has been proposed that thresholds also influence the scale at which hillslopes transition into valleys<sup>22,27–29</sup>. If a fluvial erosion threshold is included in the model equations, its effect is generally to widen valley spacing<sup>23</sup>, though not as much as a comparable fractional change in  $D$  or  $K$ . The fact that our model does not systematically underpredict valley spacing suggests that competition between soil creep and stream incision is the primary mechanism that controls valley spacing in these landscapes, but we acknowledge that erosion thresholds could have a stronger influence in others.

Also notable is the prediction that  $L_c$ , and therefore valley spacing, is independent of erosion rate. This is consistent with previous observations<sup>8,9,23</sup> that steady-state drainage density is independent of erosion rate when both creep flux and stream incision rate vary

linearly with topographic slope (equation (1)). The trend in Fig. 2, defined by sites that probably have different erosion rates, suggests that this linearity assumption is reasonable.

Valley spacing is a fundamental topographic signature that varies widely across the Earth<sup>1–6,23</sup> and other planetary surfaces<sup>23</sup>. The simplified yet mechanistic approach introduced here enables us to predict valley spacing by parameterizing erosion and transport expressions through topographic analysis. This analysis shows that differences in valley spacing are linked to elementary ratios of rate coefficients that may in turn depend on geologic materials and climate, two regulators of landform evolution that are currently poorly quantified in erosion theory. Thus, valley spacing is a measurable clue to aspects of a site's geologic past that can otherwise be difficult to assess. The same may be true of other emergent patterns in landscapes.

## METHODS SUMMARY

**Numerical model.** Following several previous studies<sup>7–9,17</sup>, we describe the evolution of the topography with a nonlinear advection–diffusion equation:

$$\frac{\partial z}{\partial t} = D\nabla^2 z - KA^m |\nabla z| + U \quad (1)$$

where  $z$  is elevation,  $t$  is time,  $D$  is soil diffusivity,  $A$  is drainage area,  $K$  and  $m$  are constants, and  $U$  is surface uplift rate. Equation (1) assumes that soil creep flux is proportional to the local topographic gradient, and that the rate of erosion by channelized flow of water is proportional to the rate of energy expenditure<sup>30</sup>. A derivation of equation (1) and details of the numerical solution method can be found in ref. 23. Non-dimensionalizing equation (1) yields a quantity analogous to a Péclet number<sup>23</sup>:

$$Pe = \frac{KL^{2m+1}}{D} \quad (2)$$

where  $L$  is a horizontal length scale. Setting  $Pe = 1$ , we solved for a characteristic length,  $L_c$ , at which the timescales for advection and diffusion are equal:

$$L_c = \left(\frac{D}{K}\right)^{\frac{1}{2m+1}} \quad (3)$$

By solving equation (1) numerically, we found that the valley spacing,  $\lambda$ , is proportional to  $L_c$  (Fig. 2).

**Topographic analysis.** We used topographic data to infer the value of  $L_c$  for the study sites. At equilibrium ( $\partial z/\partial t = 0$ ) and on hilltops, where  $A$  and  $|\nabla z|$  approach zero, equation (1) reduces to:

$$\frac{U}{D} \approx -\nabla^2 z_h \quad (4)$$

and thus  $U/D$  can be inferred from the Laplacian of elevation on hilltops,  $\nabla^2 z_h$ . Rearranging equation (1) with  $\partial z/\partial t = 0$  and using equation (4) gives:

$$\frac{|\nabla z|}{\nabla^2 z - \nabla^2 z_h} = \frac{D}{K} A^{-m} \quad (5)$$

This implies a power-law relationship between drainage area  $A$  and the quantity  $|\nabla z|/(\nabla^2 z - \nabla^2 z_h)$ , which we abbreviate as  $S^*$ . We used laser altimetry data to calculate  $A$ ,  $|\nabla z|$ , and  $\nabla^2 z$ , and measured  $\nabla^2 z_h$  as the value that  $\nabla^2 z$  approaches as  $A|\nabla z| \rightarrow 0$  (Fig. 3a). We then calculated  $S^*$ , found  $D/K$  and  $m$  from least-squares regression of  $\log_{10}(S^*)$  against  $\log_{10}(A)$  (Fig. 3b), and calculated  $L_c$  using equation (3). Values of  $\nabla^2 z_h$ ,  $D/K$ ,  $m$ ,  $L_c$  and  $\lambda$  for the five study sites are listed in Table 1.

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**Supplementary Information** is linked to the online version of the paper at [www.nature.com/nature](http://www.nature.com/nature).

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