

# On the use of 'physical' models to understand glacier and ice sheets dynamics

Ginny Catania, Institute for Geophysics, University of Texas at Austin



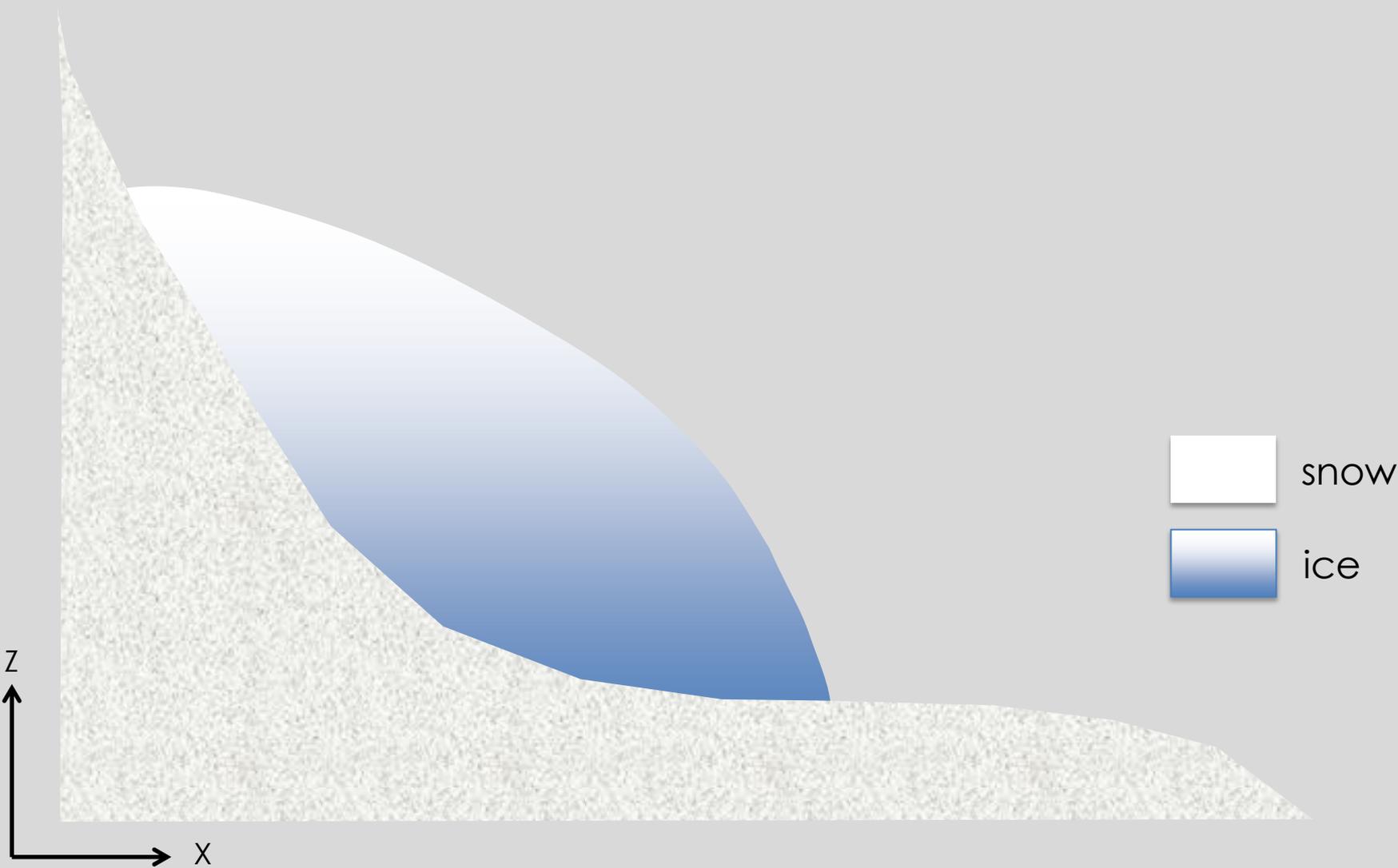
meager

# On the use of 'physical' models to understand glacier and ice sheets dynamics

Ginny Catania, Institute for Geophysics, University of Texas at Austin



# Glacier Fundamentals



# Glacier Fundamentals

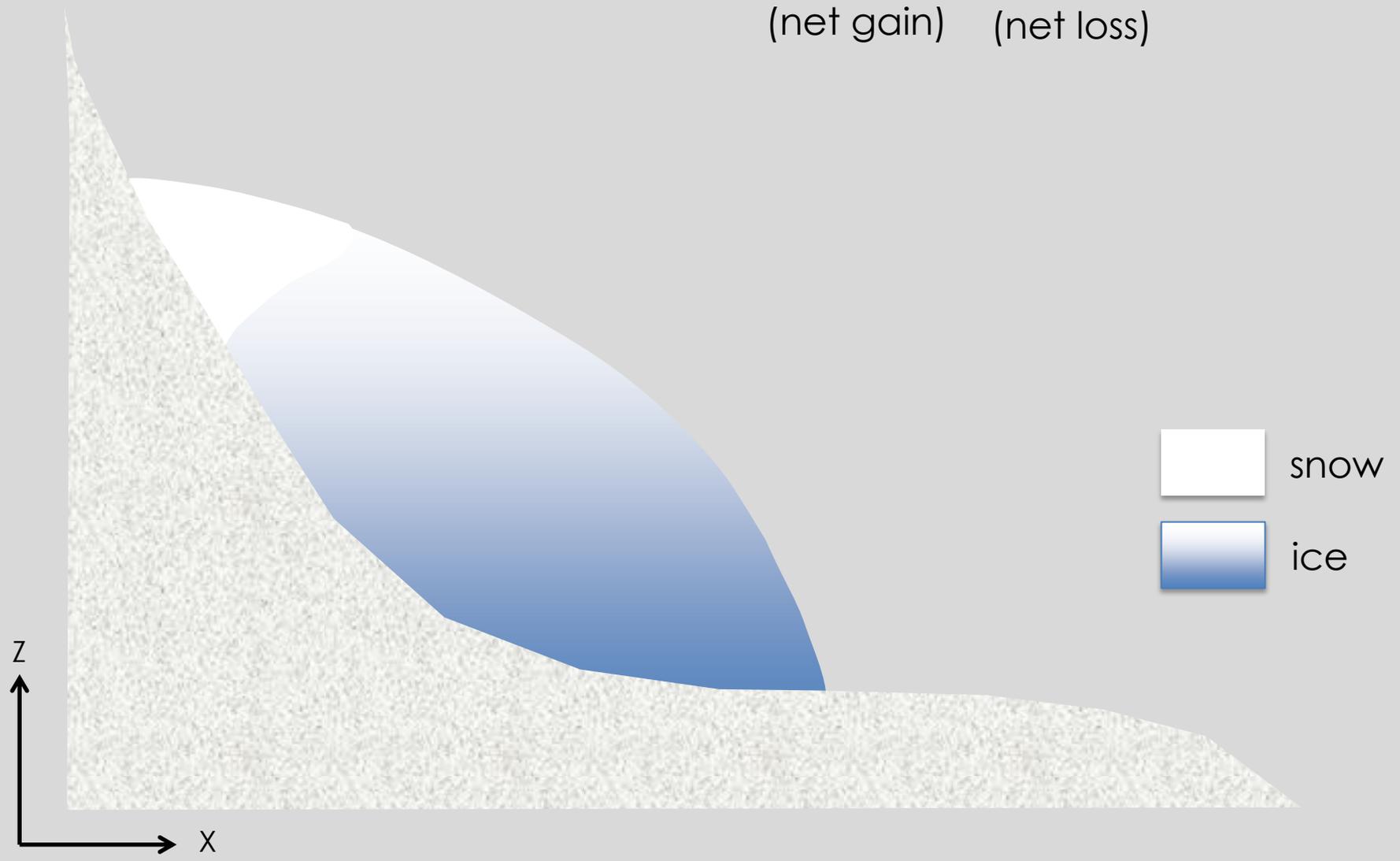


# Glacier Fundamentals



# Glacier Fundamentals

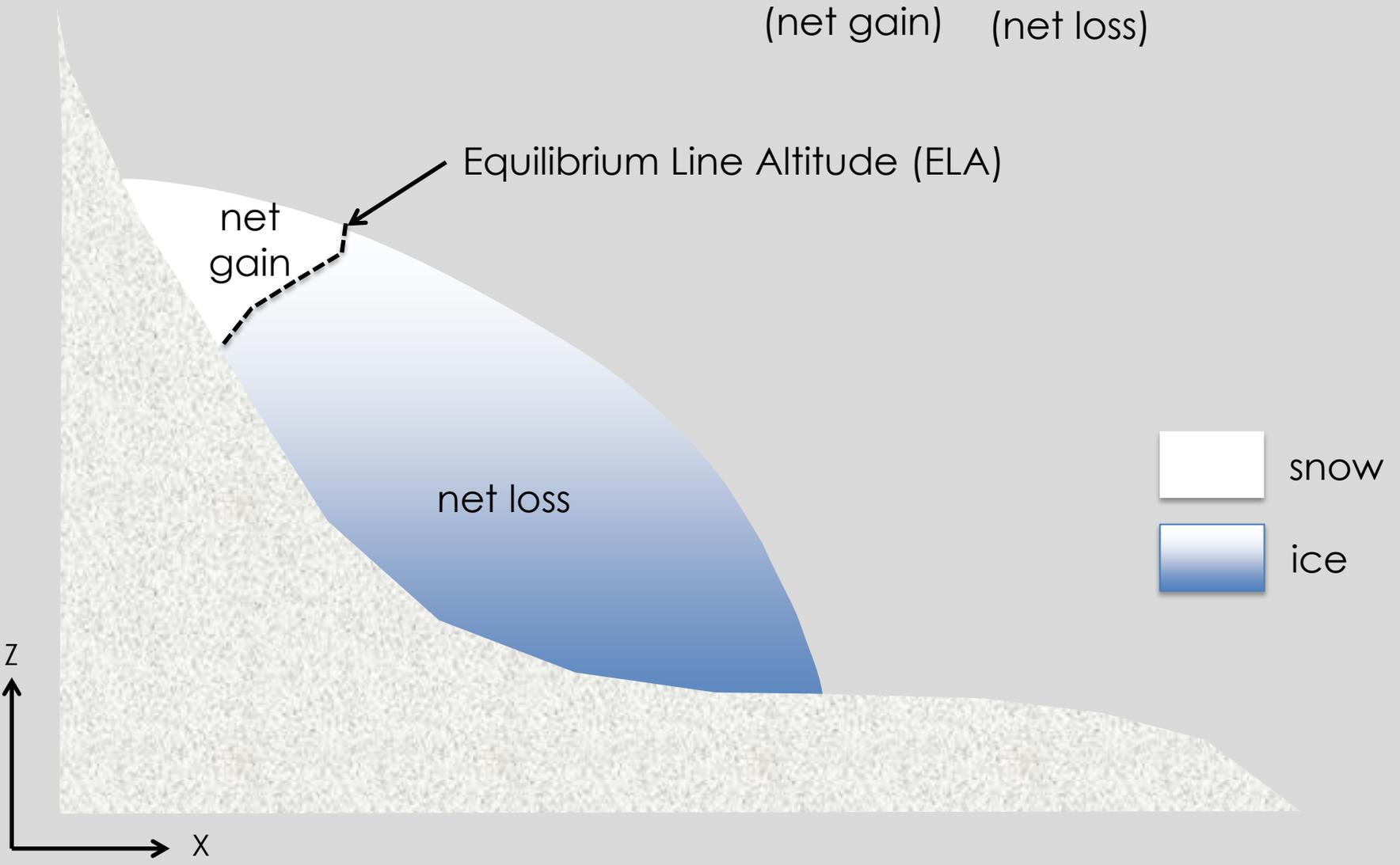
Net mass balance = accumulation - ablation  
(net gain) (net loss)



# Glacier Fundamentals

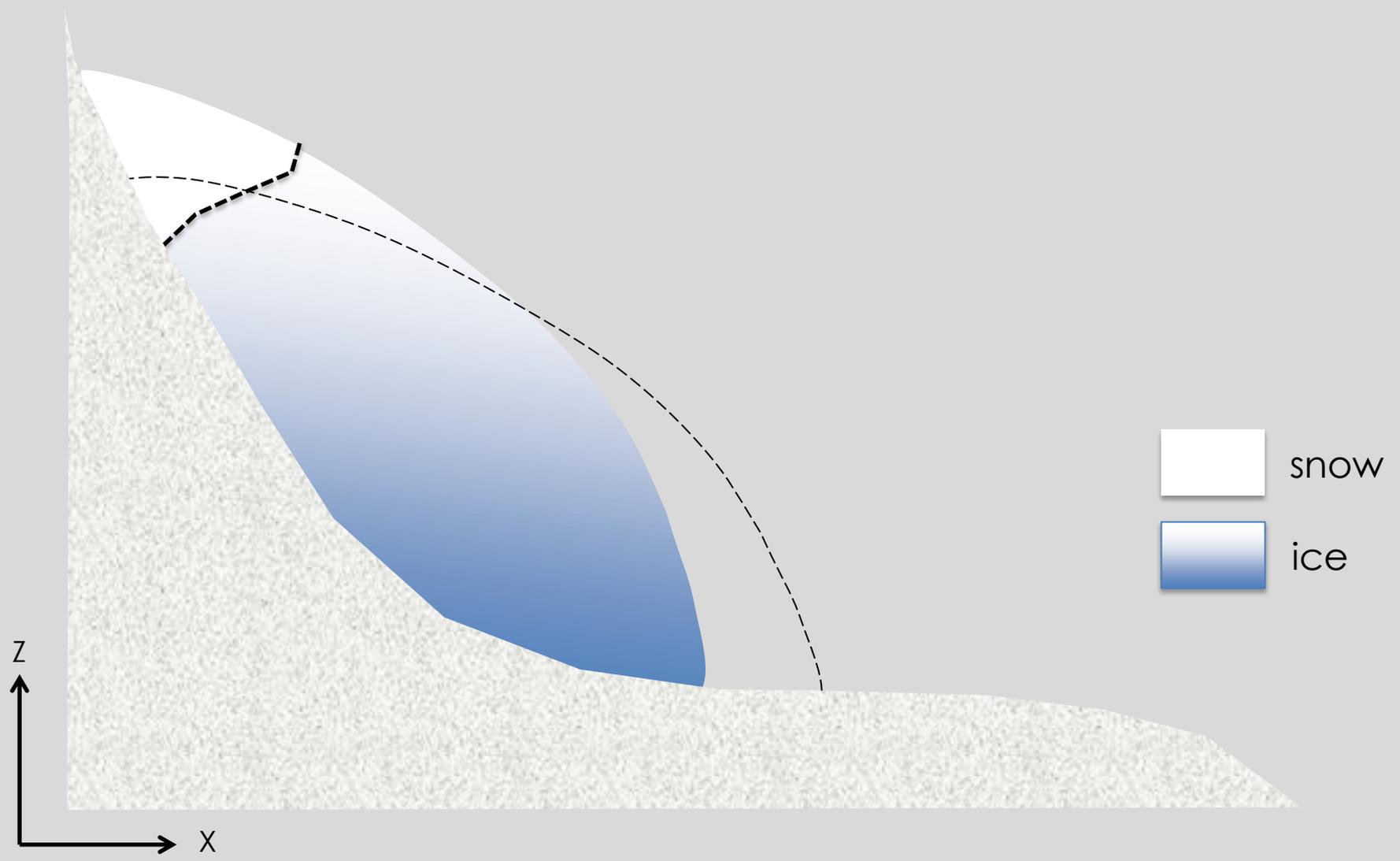
$$\text{Net mass balance} = \text{accumulation} - \text{ablation}$$

(net gain)    (net loss)



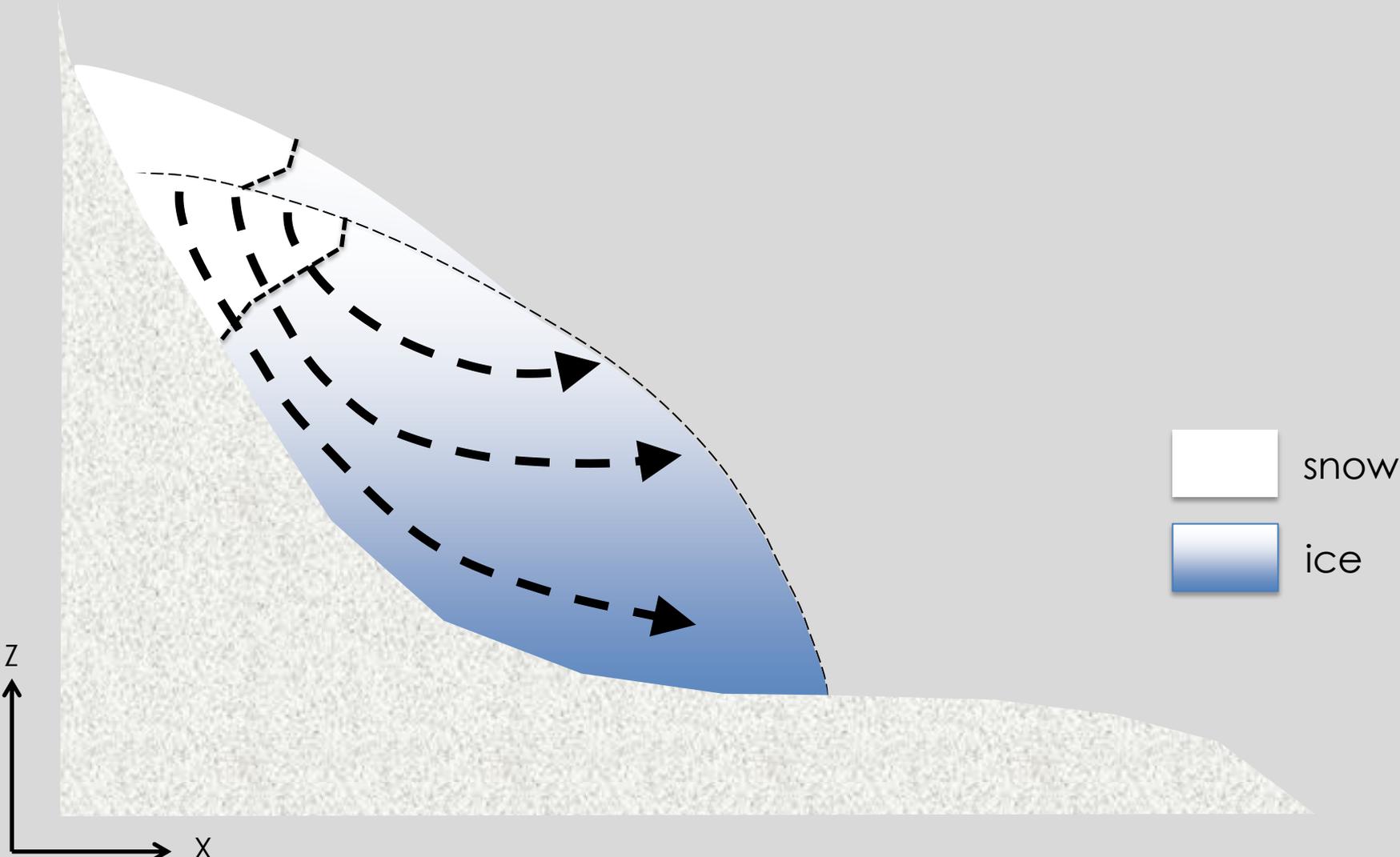
# Glacier Fundamentals

In the absence of flow, glaciers would steepen



# Glacier Fundamentals

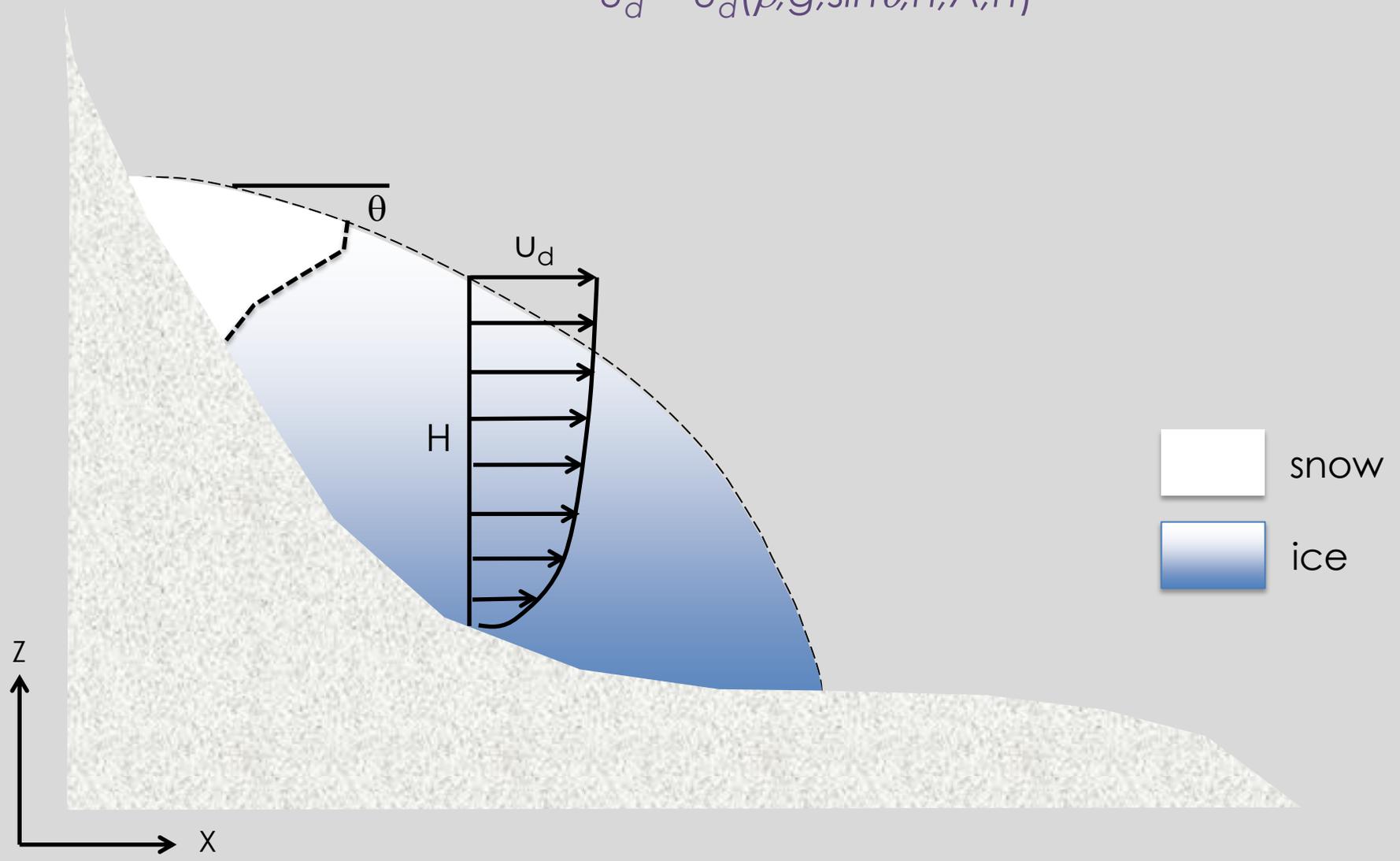
Glacier flow conveys mass from high to low elevations



# Glacier Fundamentals

Glacier flow mechanisms:  
Internal (viscous) deformation:

$$u_d = u_d(\rho, g, \sin \theta, h, A, n)$$



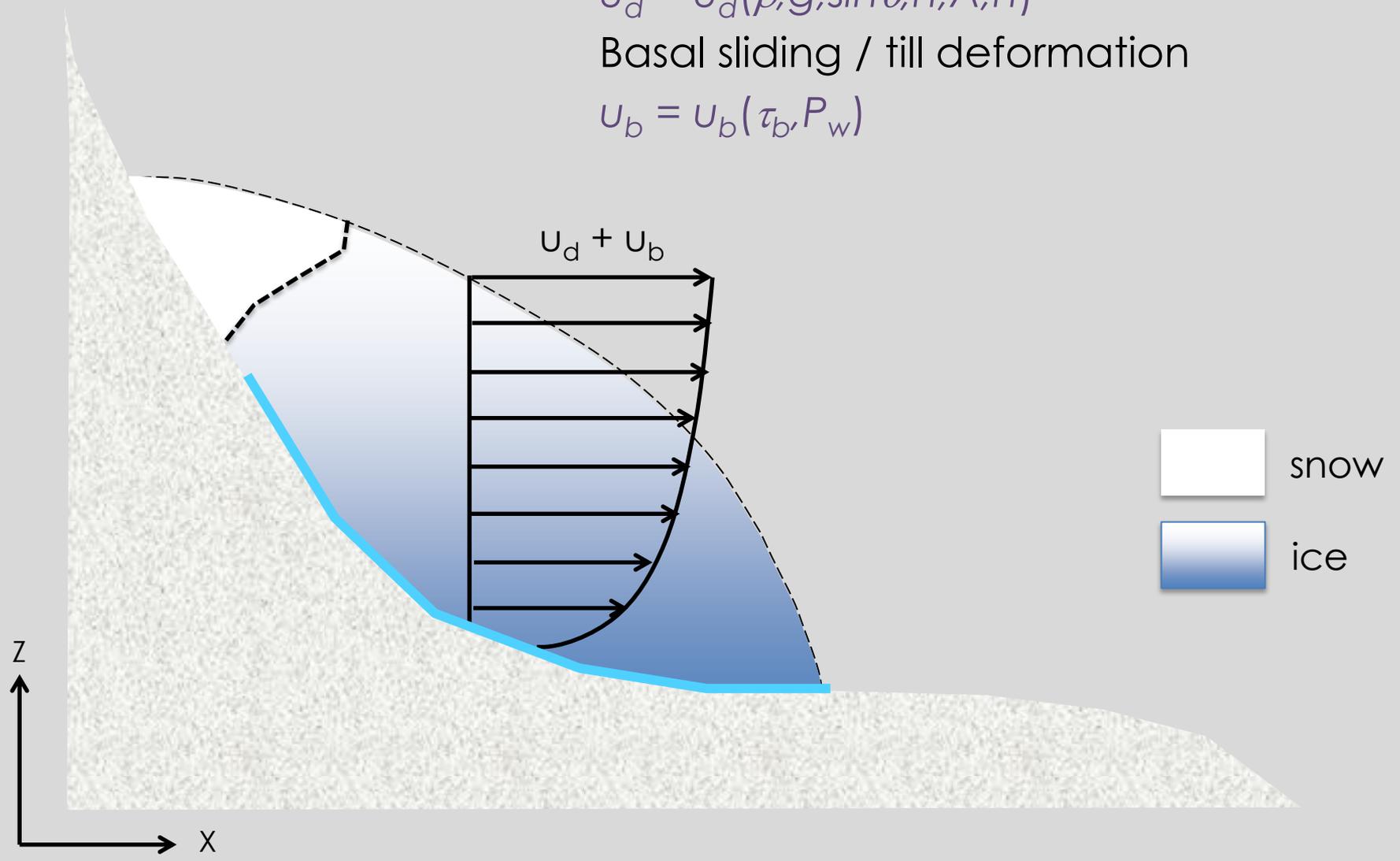
# Glacier Fundamentals

Glacier flow mechanisms:  
Internal (viscous) deformation:

$$U_d = U_d(\rho, g, \sin \theta, h, A, n)$$

Basal sliding / till deformation

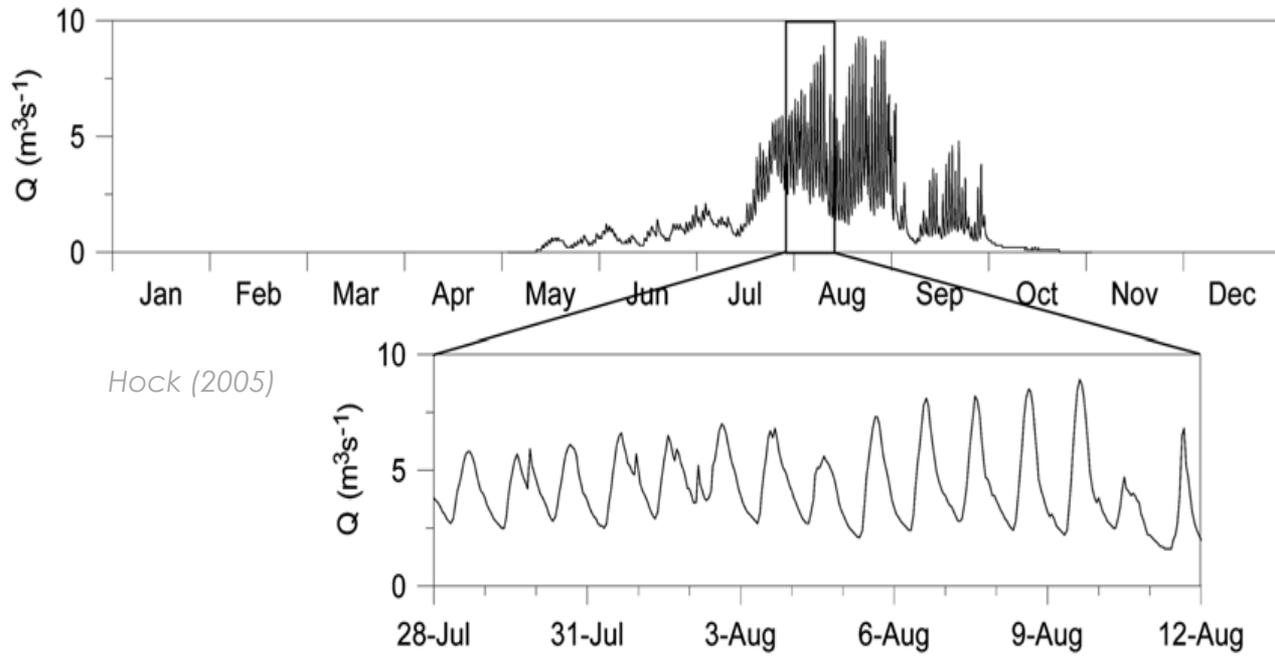
$$U_b = U_b(\tau_b, P_w)$$



# Glacier Fundamentals: basal sliding



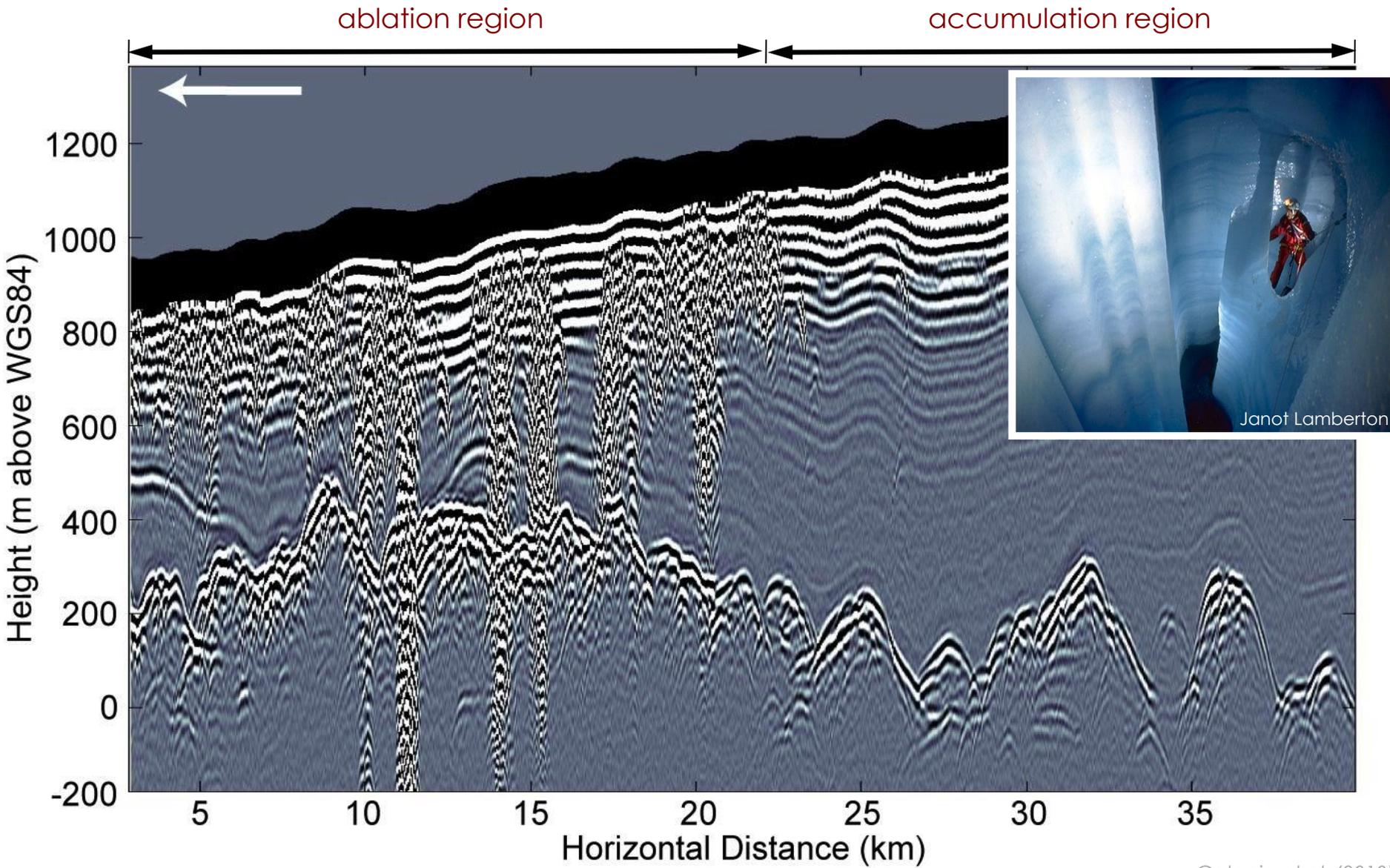
- glacier-fed streams show seasonal-daily variations in water discharge related to variations in solar radiation causing melt



Hock (2005)

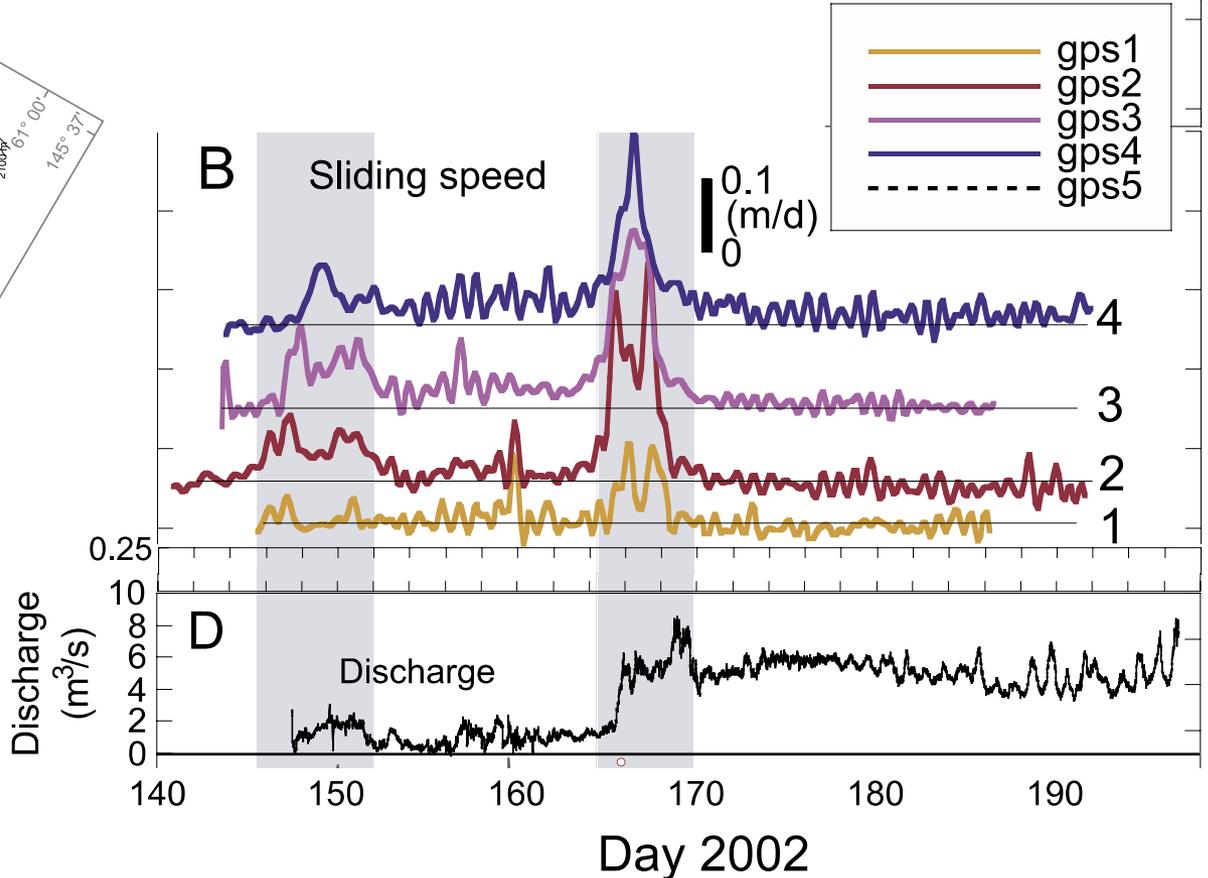
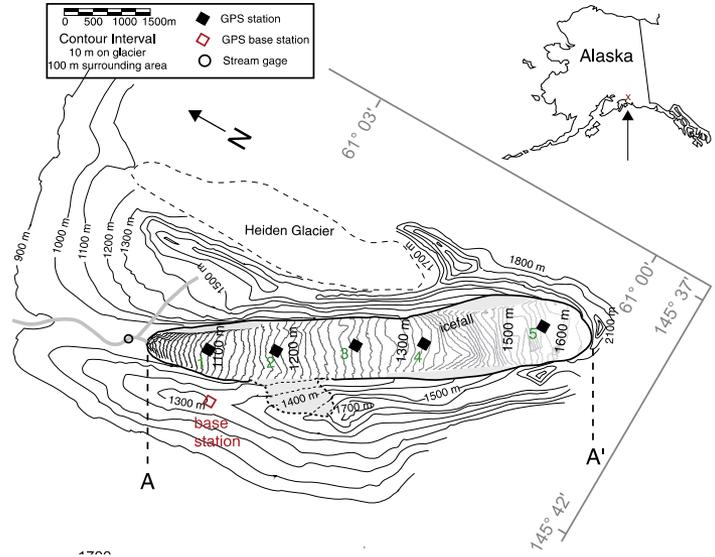
# Glacier Fundamentals: basal sliding

- variations in melt supply are routed through glaciers via moulin which deliver water to the bed



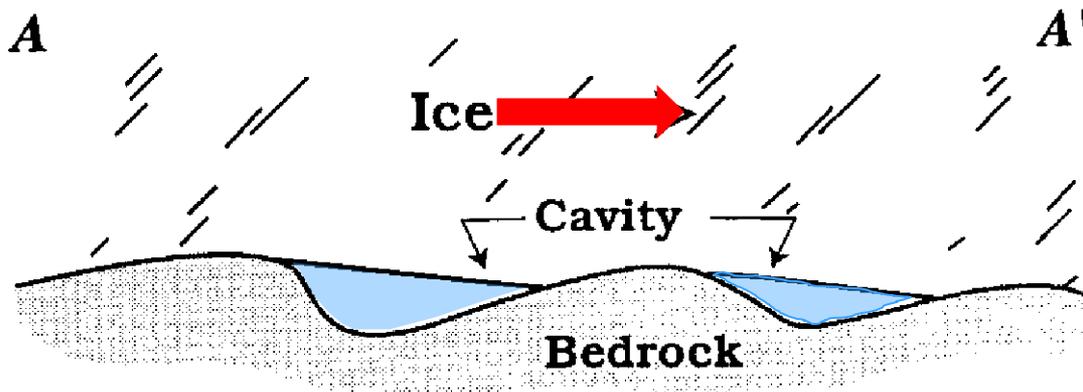
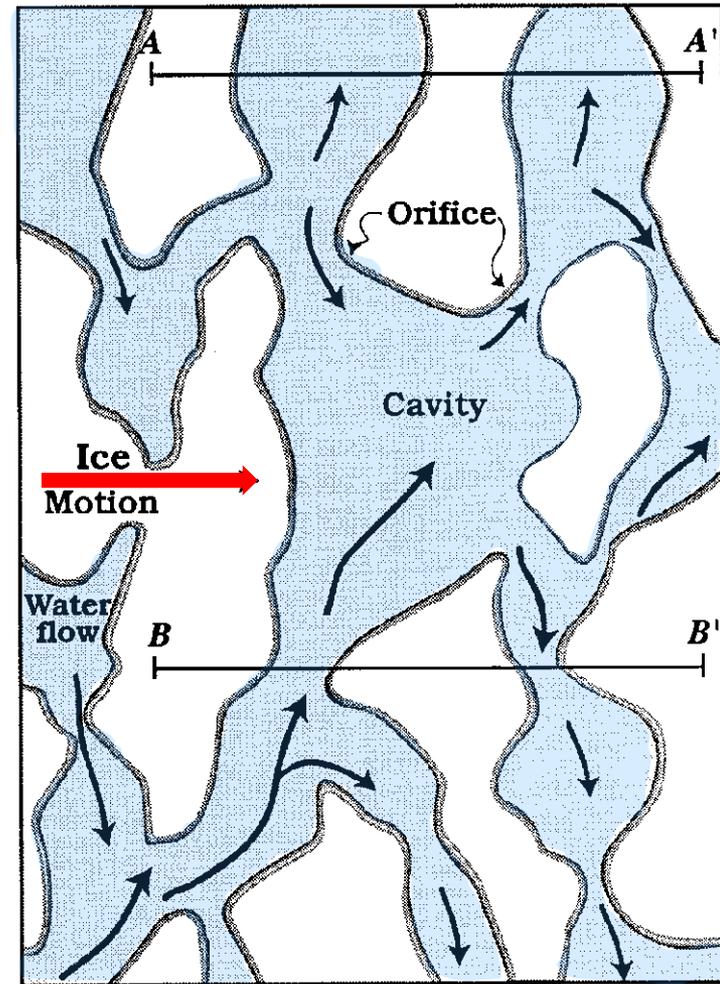
# Glacier Fundamentals: basal sliding

- changes in water discharge are well-correlated to changes in ice flow speed
- what is the physical mechanism?



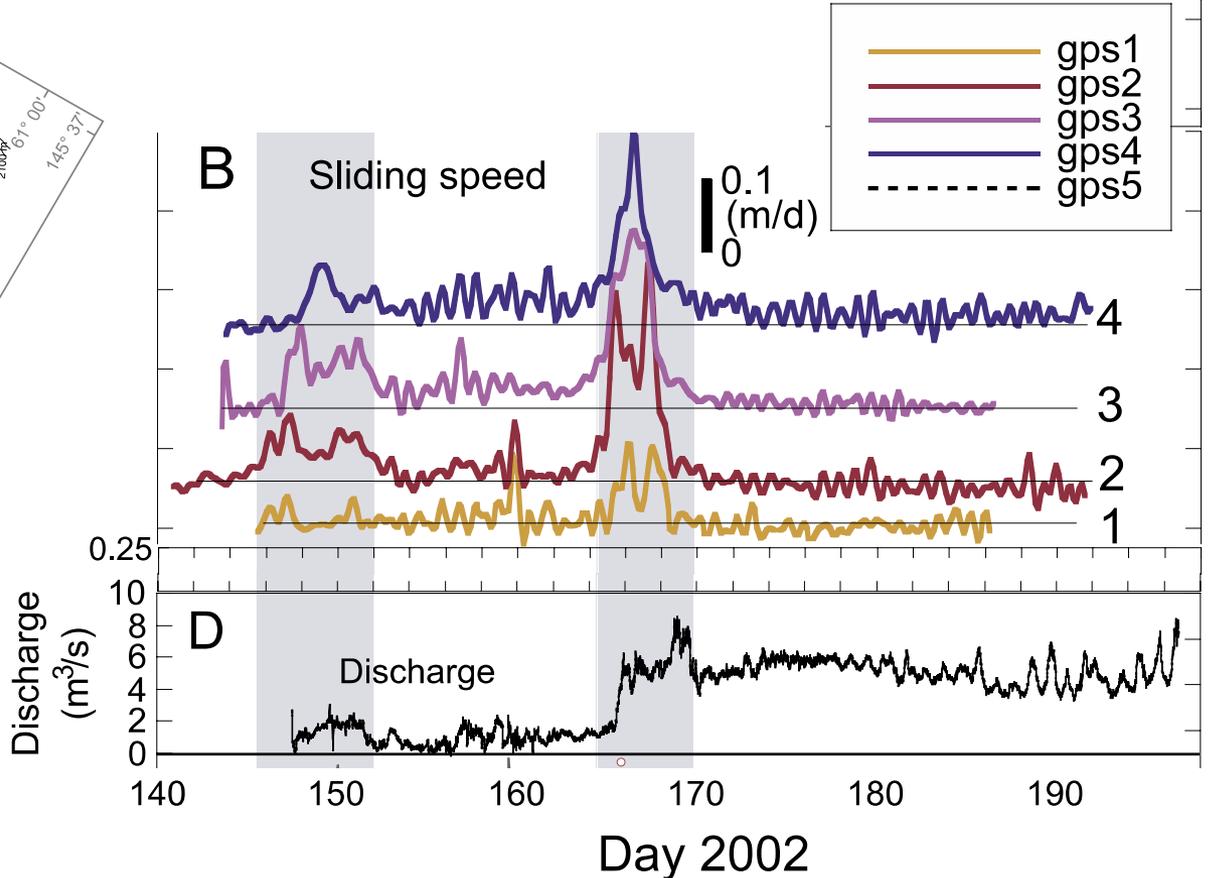
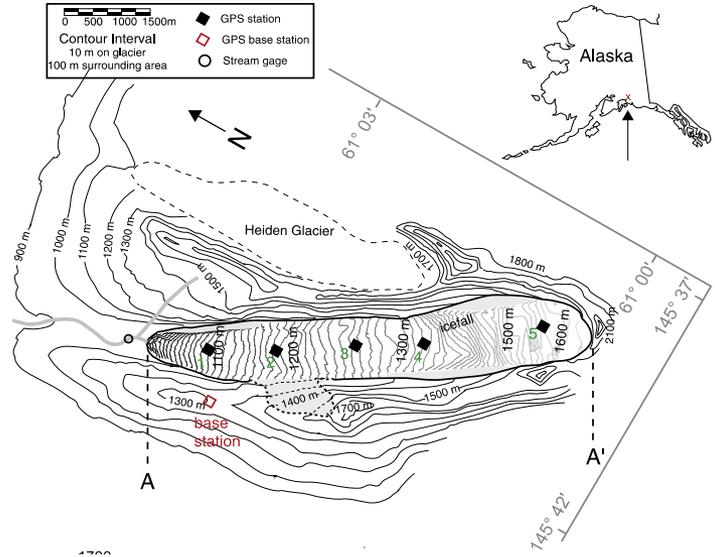
# Glacier Fundamentals: basal sliding

- distributed drainage system of linked cavities that form on the lee side of bed protrusions
- system operates at a higher water pressure because the drainage of water is inefficient
- cavities grow with increasing water pressure and sliding speed



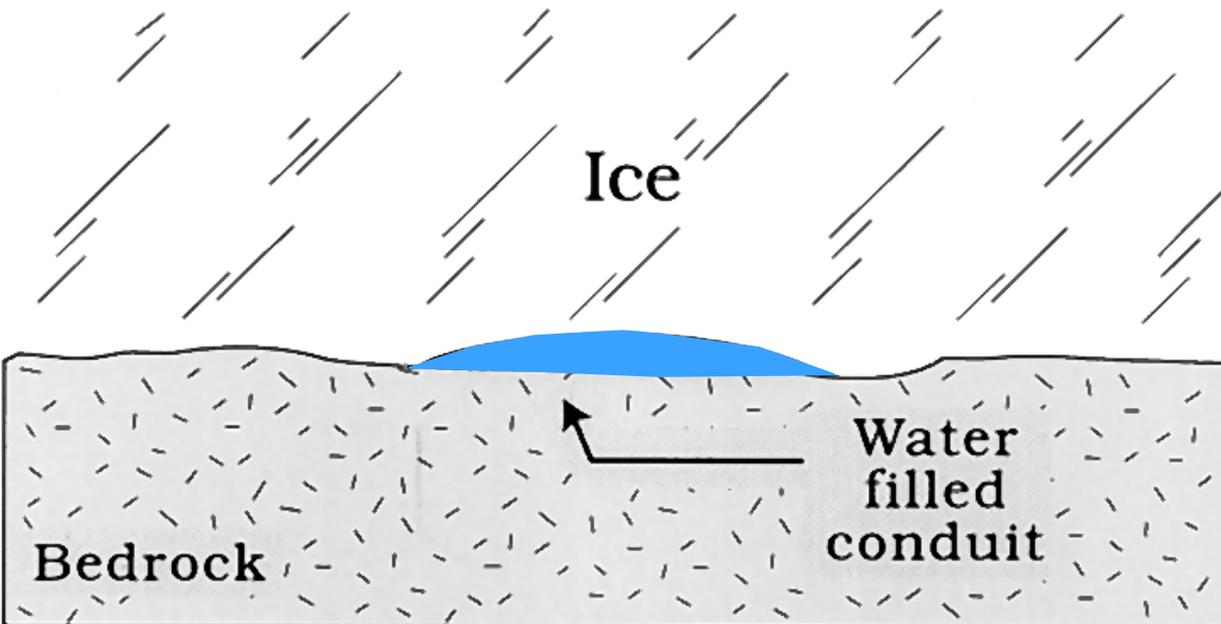
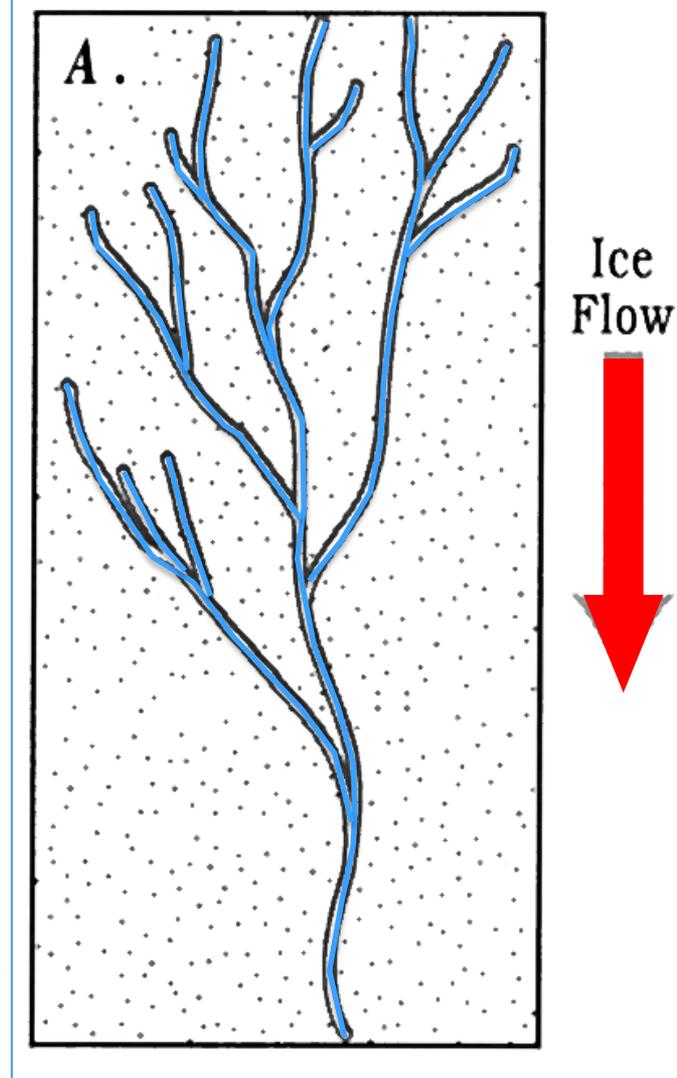
# Glacier Fundamentals: basal sliding

- changes in water discharge are well-correlated to changes in ice flow speed
- physical mechanism: drowning of bed obstacles



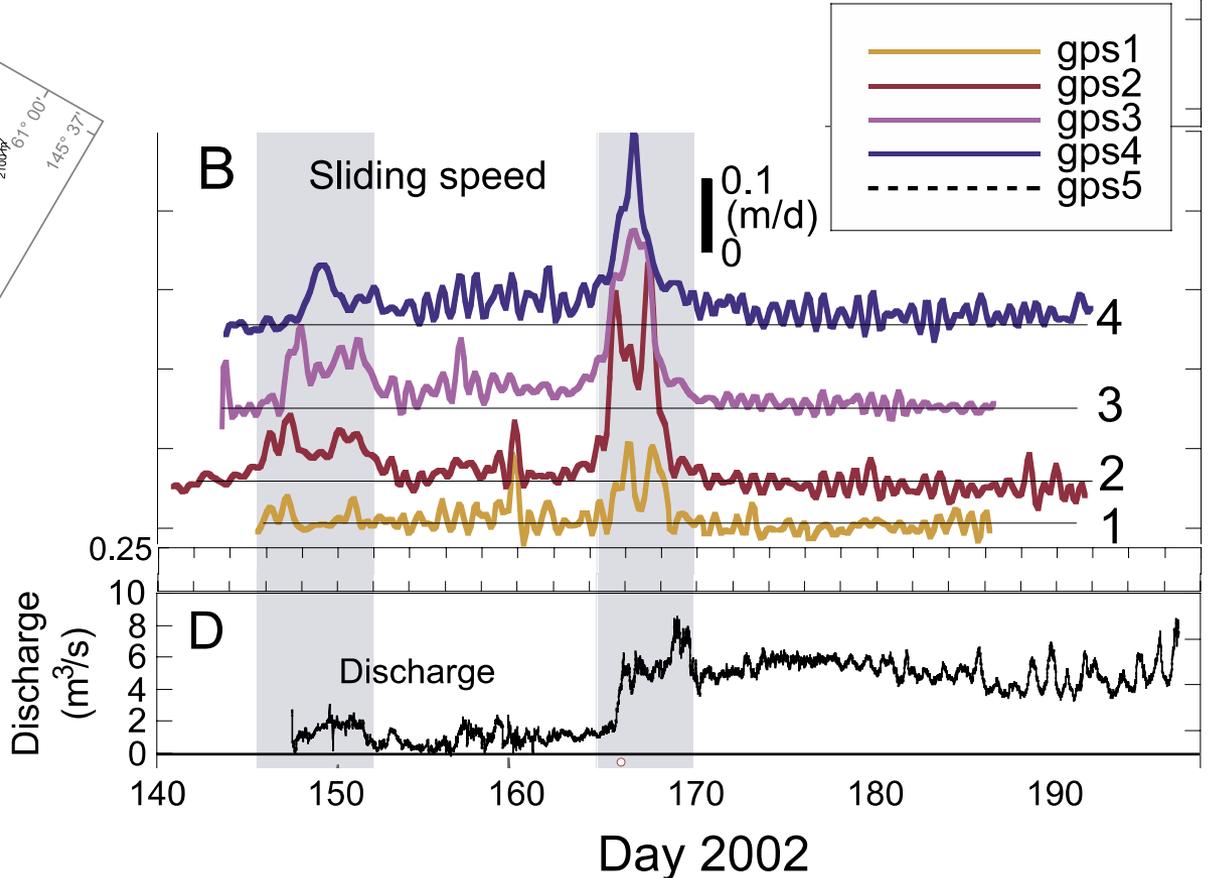
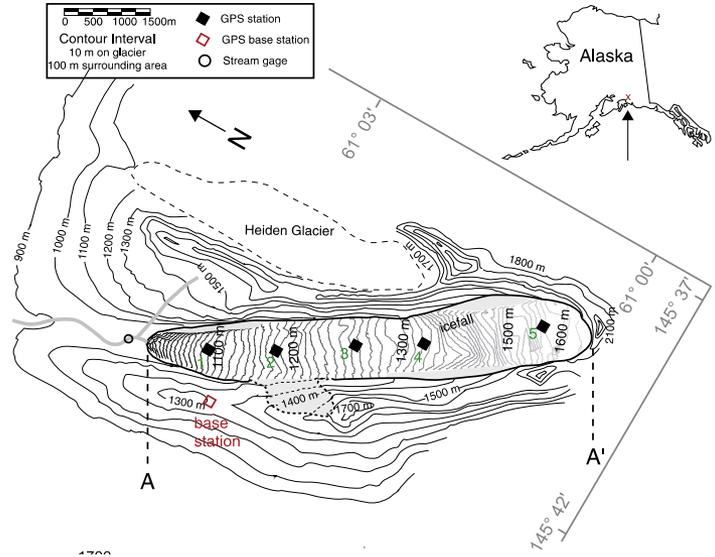
## Glacier Fundamentals: basal sliding

- as water supply increases channels cut up, into the ice and enlarge through melt
- channels operate at lower pressures and grow at the expense of smaller ones
- channels can efficiently transport water whereas cavities require high pressures to transport the same flux

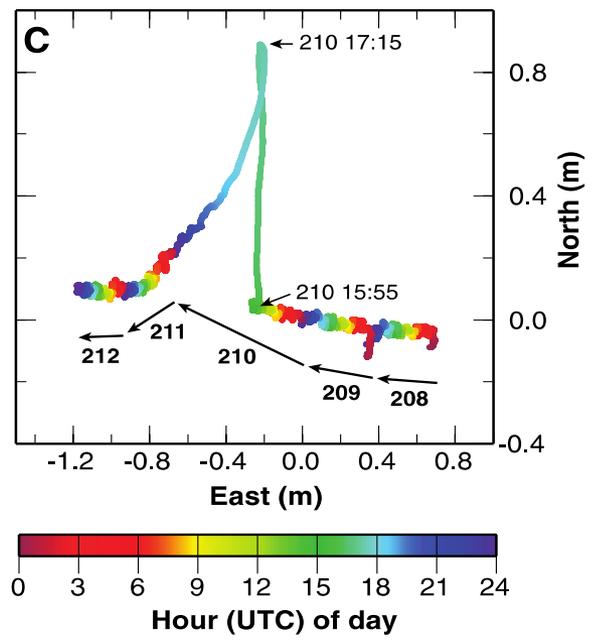
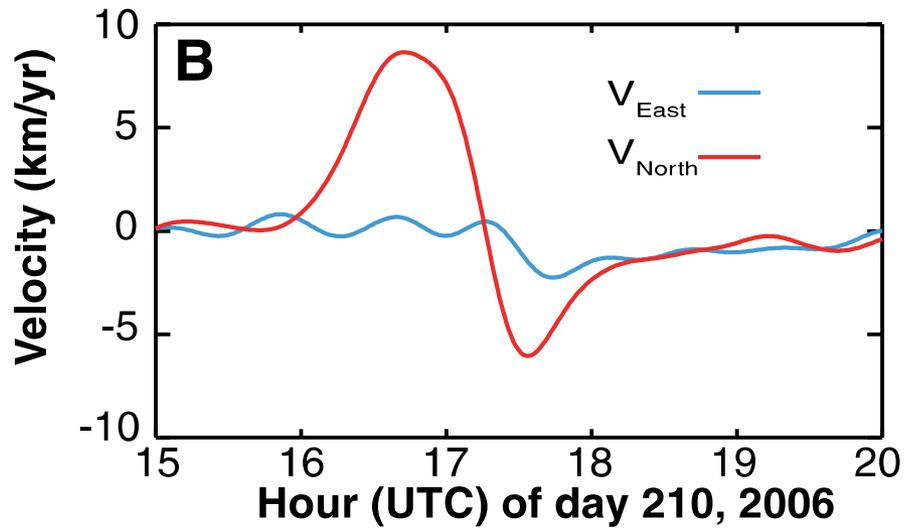
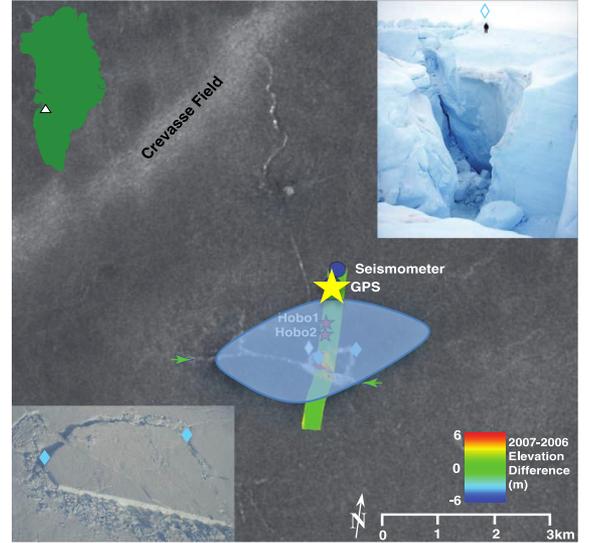
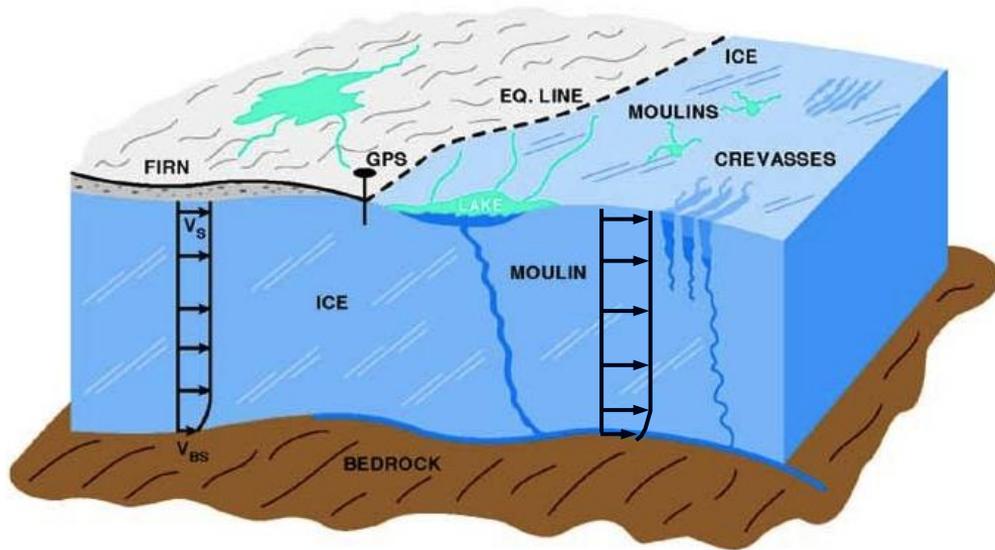


# Glacier Fundamentals: basal sliding

- changes in water discharge are well-correlated to changes in ice flow speed
- physical mechanism: drowning of bed obstacles



# Glacier Fundamentals: basal sliding



**Physical Model:** discharge variability



# Physical Model: discharge variability

- polydimethyl-siloxane (PDMS) used in tectonics experiments
- non-Newtonian at strain rates larger than  $10^{-2} \text{ s}^{-1}$
- Newtonian at strain rates used in experiments ( $10^{-4} \text{ s}^{-1}$ )
- scale **geometry**, **density**, **time** and **rheology**

## Geometry:

$$\frac{H_m}{W_m} = 0.1 \quad \frac{H_i}{W_i} = 0.1$$

## Density:

$$\frac{\rho_m}{\rho_w} = 0.97 \quad \frac{\rho_i}{\rho_w} = 0.91$$

## Time:

$$t_m = \left( \frac{\eta_m \rho_i H_i}{\eta_i \rho_m H_m} \right) t_i \quad \text{for } t_i = 1 \text{ day, } t_m \sim 7 \text{ min}$$

## Rheology:

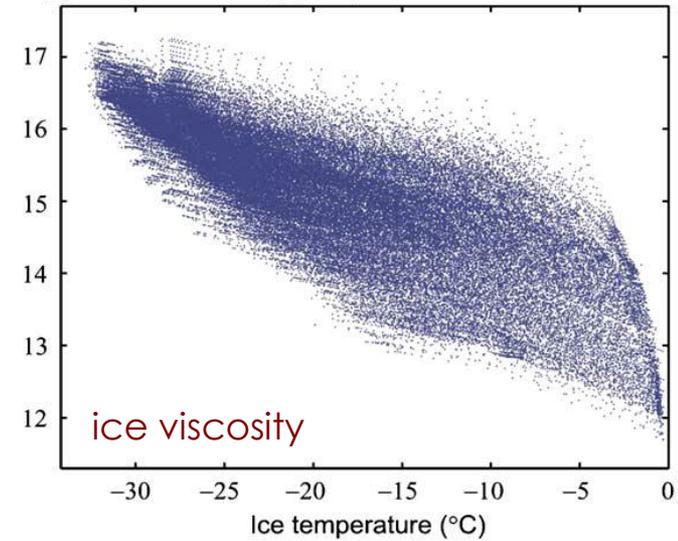
$$Re_i = \frac{\rho_i v_i H_i}{\eta_i} \sim 10^{-9} \quad (\text{small, laminar})$$

$$Re_m = \frac{\rho_m v_m H_m}{\eta_m} \sim 10^{-12} - 10^{-15}$$

## Rheology:

$$\eta_i = \left( \frac{\rho_i}{\rho_m} \frac{H_i}{H_m} \frac{\dot{\epsilon}_m}{\dot{\epsilon}_i} \right) \eta_m \sim 10^{14} \text{ Pa s}$$

Log<sub>10</sub> effective viscosity (Pa s) Marshall (2005)



Quantity	Model	Ice
Thickness (m)	~0.1	~1000
Width (m)	~1	~100000
Density kg/m <sup>3</sup>	970	910
Viscosity (Pa s)	$5 \times 10^4$	$10^{11} - 10^{17}$
$\dot{\epsilon}$ (s <sup>-1</sup> )	$10^{-4}$	~ $10^{-9}$

# Physical Model: discharge variability

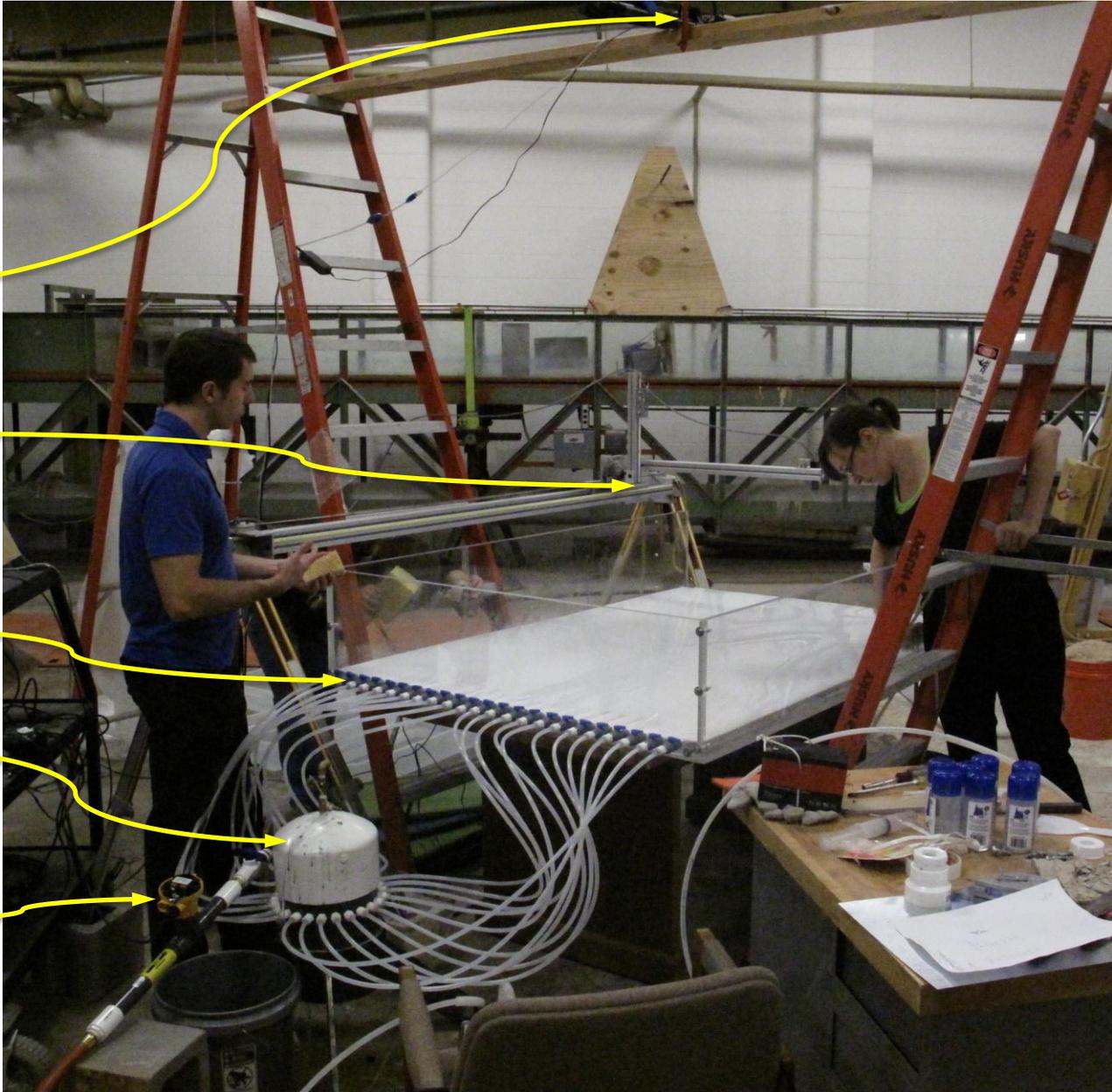
camera: horizontal surface velocity

acoustic sensor: surface elevation

distributed discharge valves vary water input

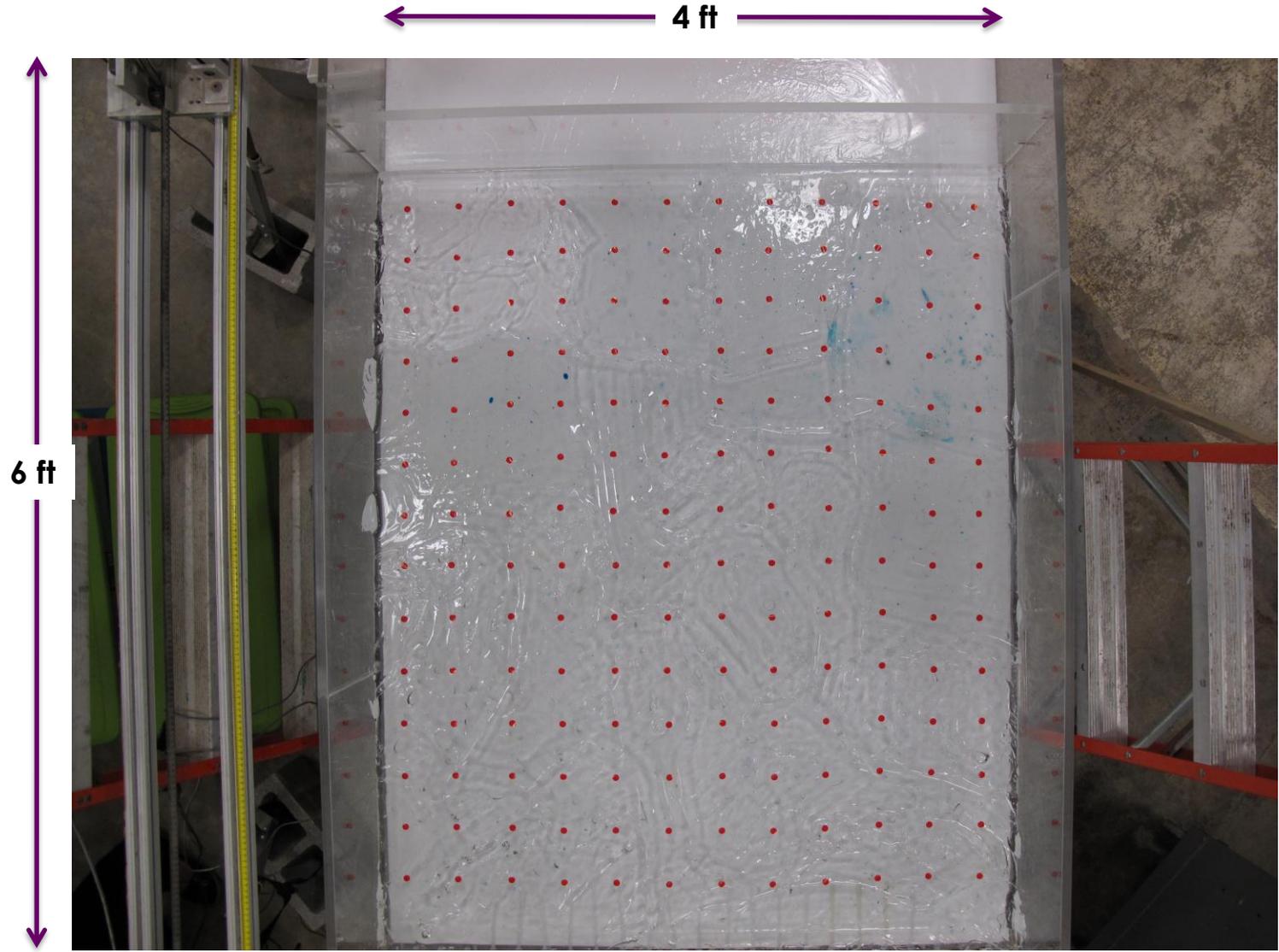
pressure tank: keeps water pressure high and uniform across width

flow meter: water discharge



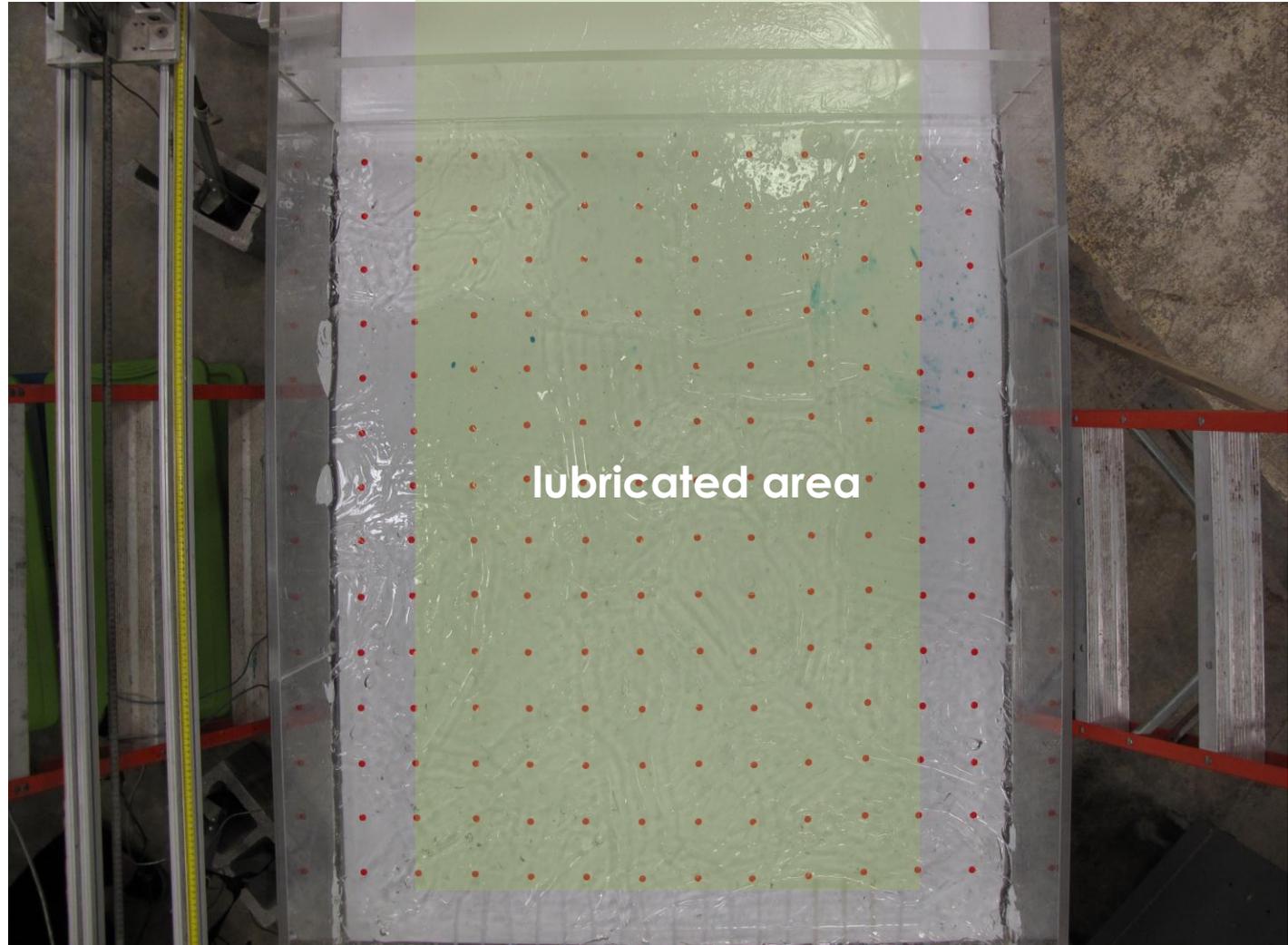
# Physical Model: discharge variability

- polymer is loaded to achieve a ~10 cm thick layer of polymer
- held in place temporarily with plexiglas wall
- no slope



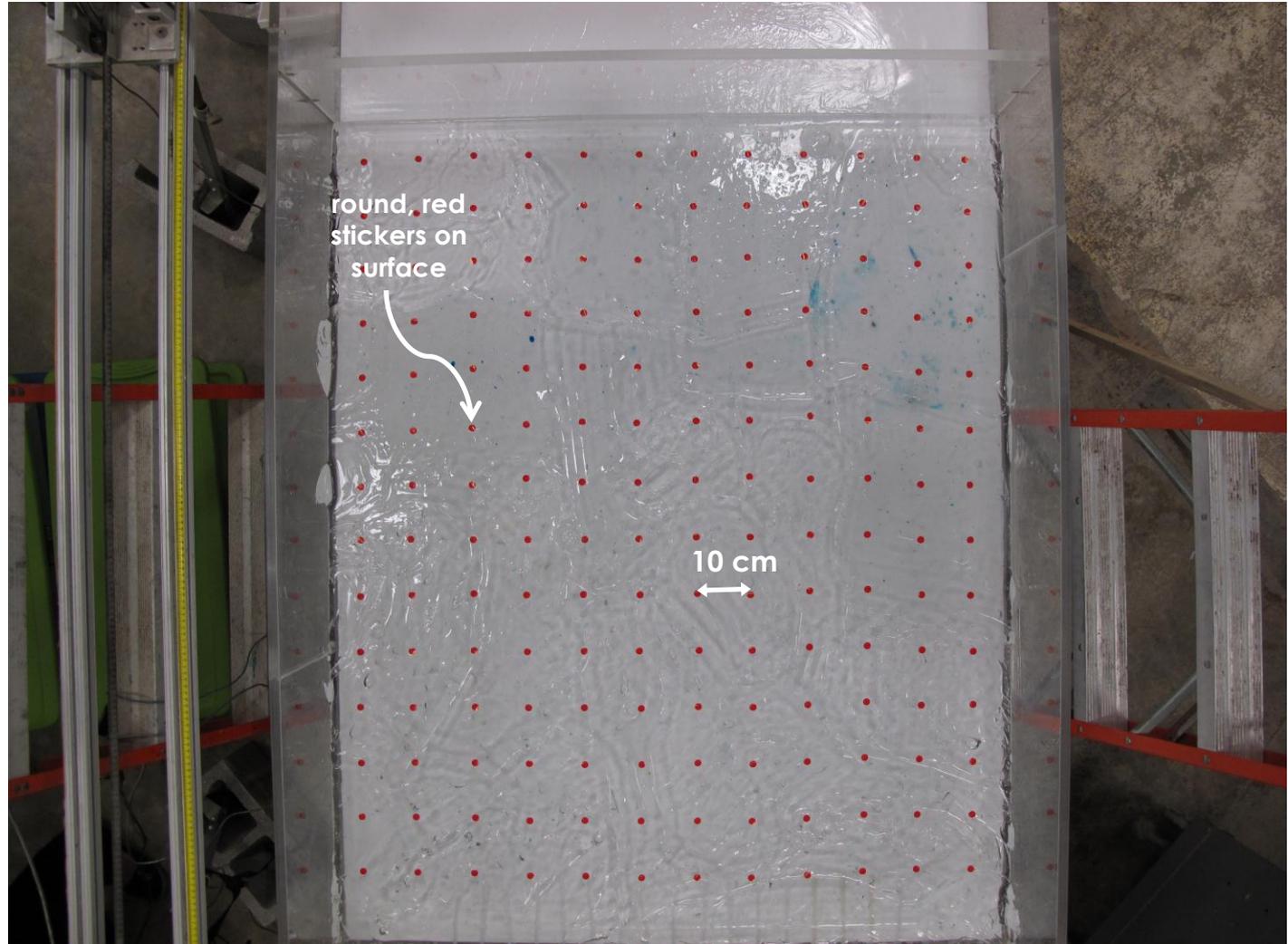
## Physical Model: discharge variability

- lubricant is applied over the plexiglas box before polymer is loaded
- reduces friction at the polymer/box interface
- lack of lubricant at edges provides a water-tight seal on flume edges

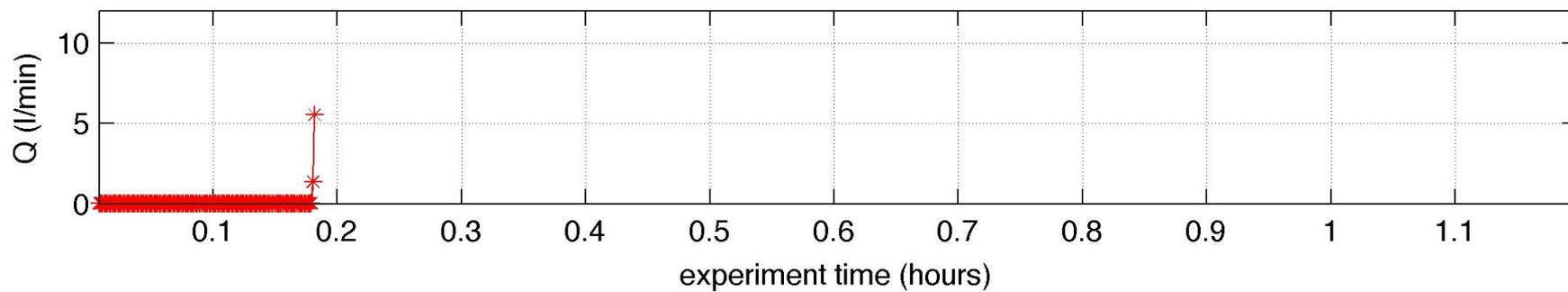
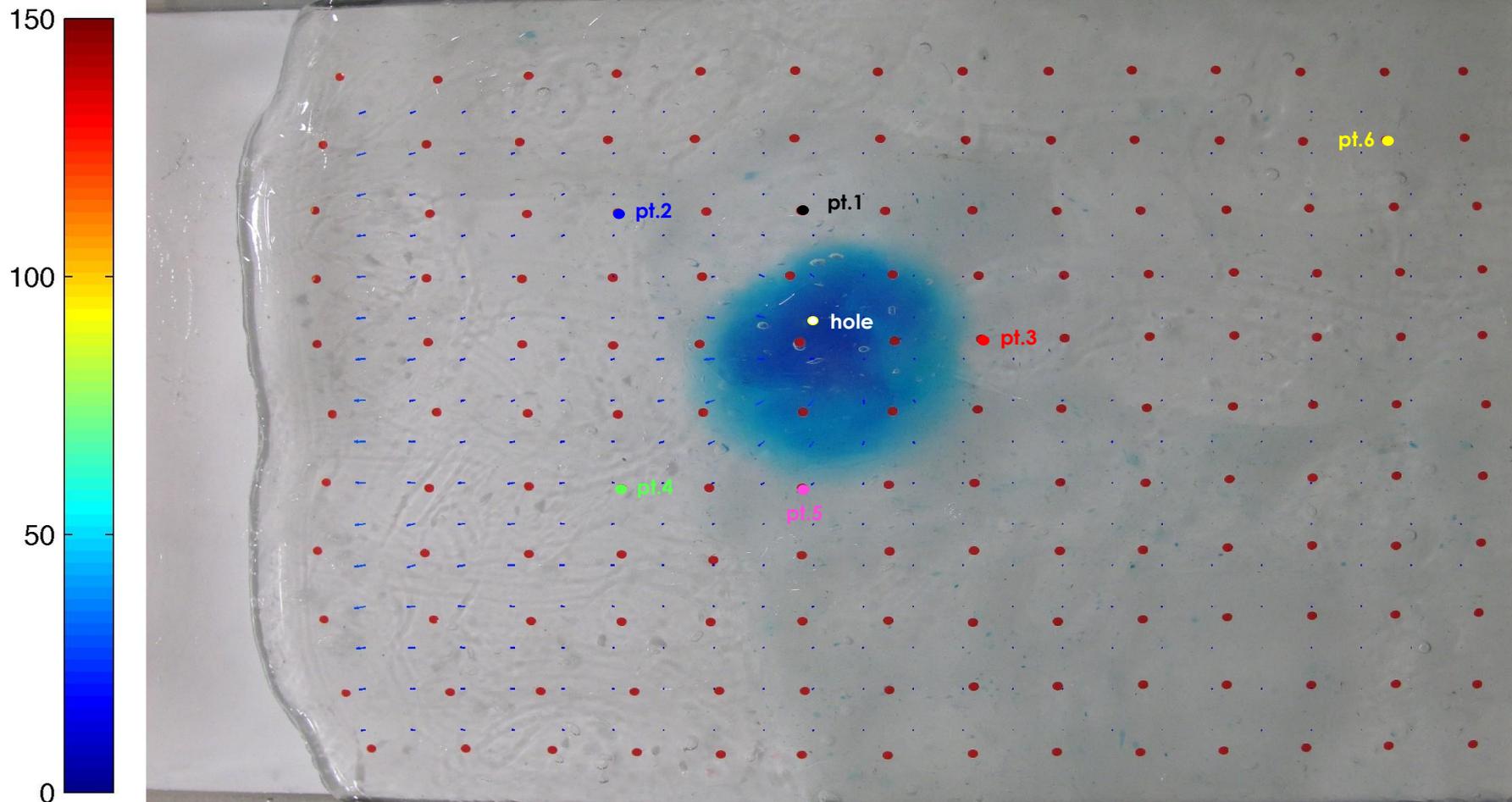


## Physical Model: discharge variability

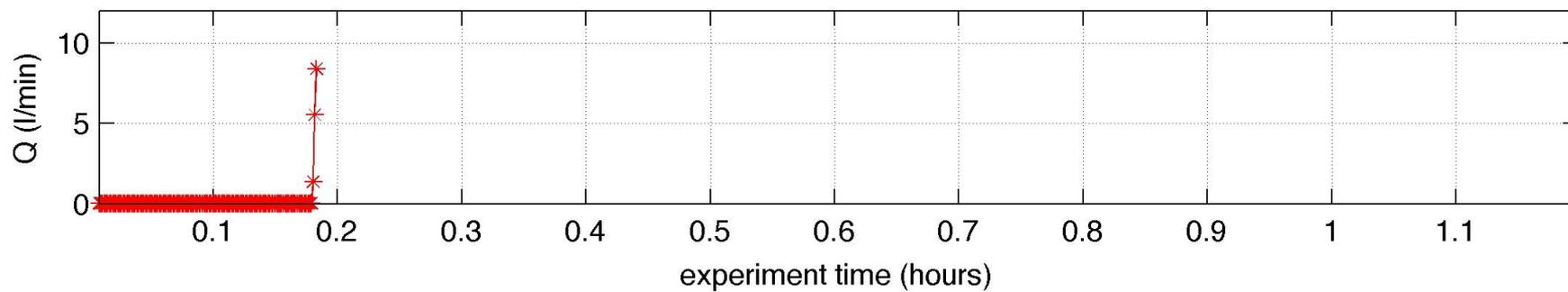
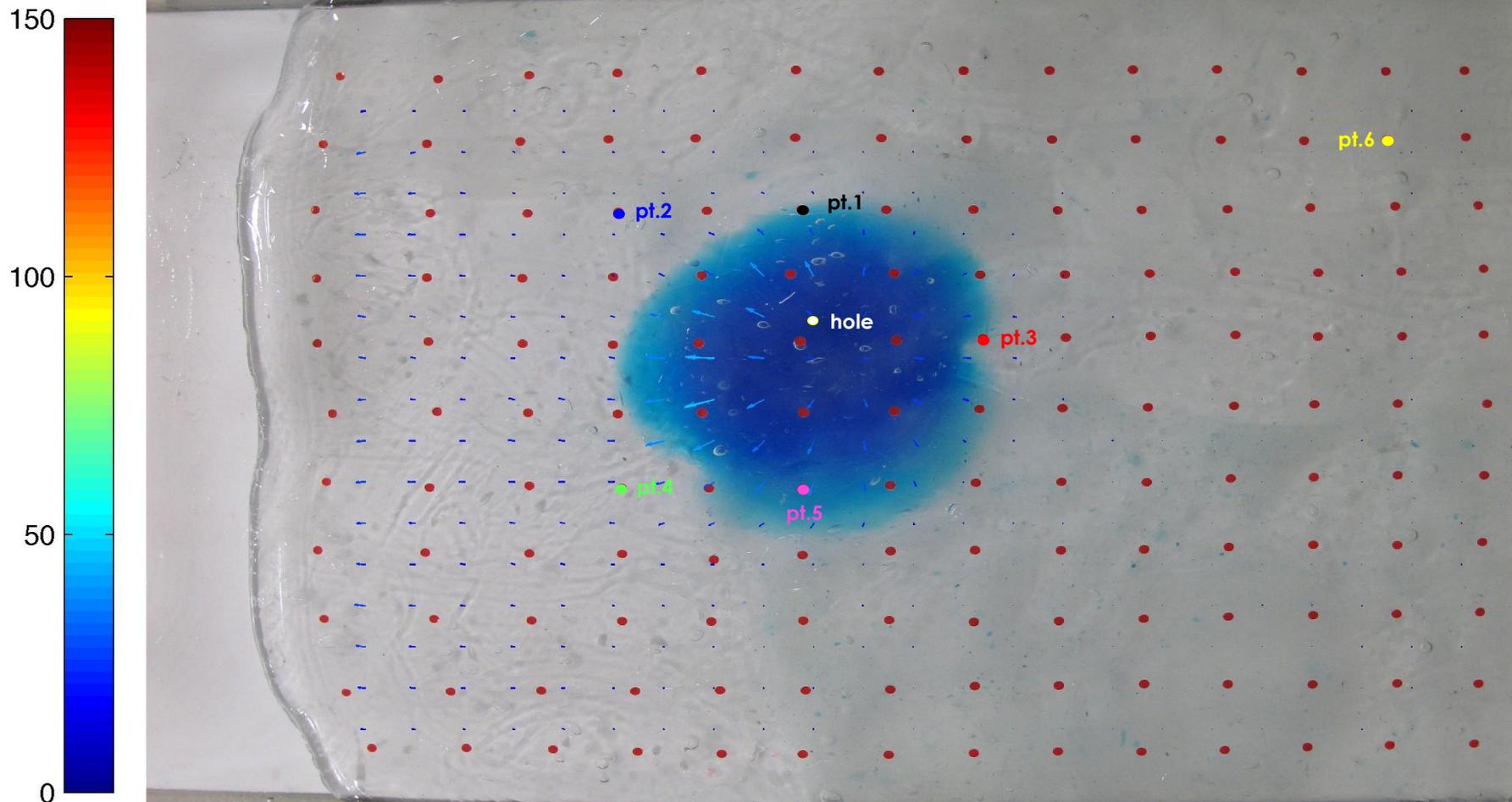
- stickers are placed on the surface in a 10 cm grid to measure surface horizontal velocity field



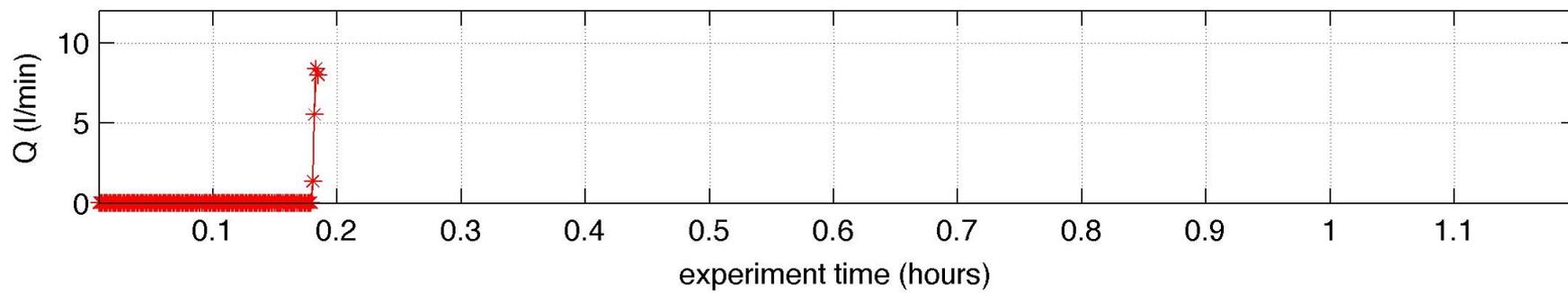
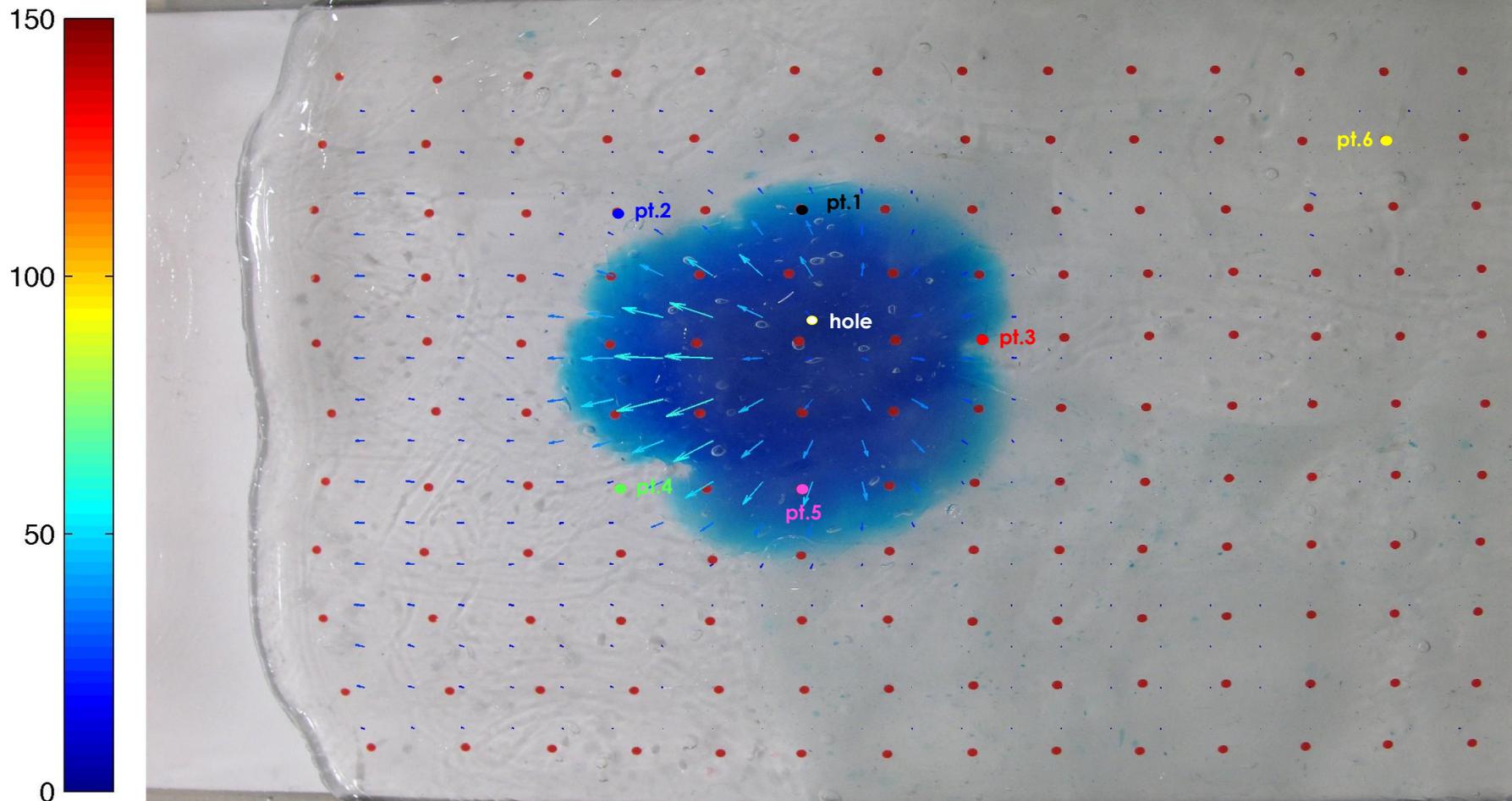
velocity (cm/hr)



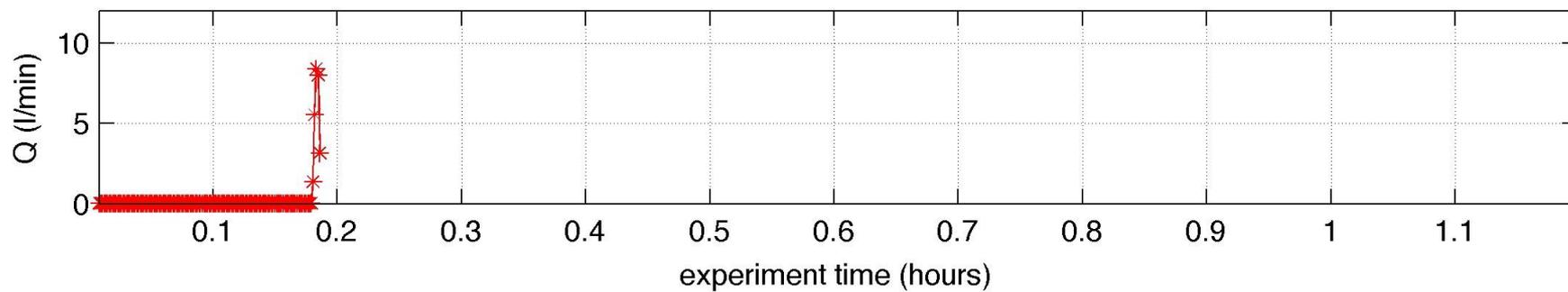
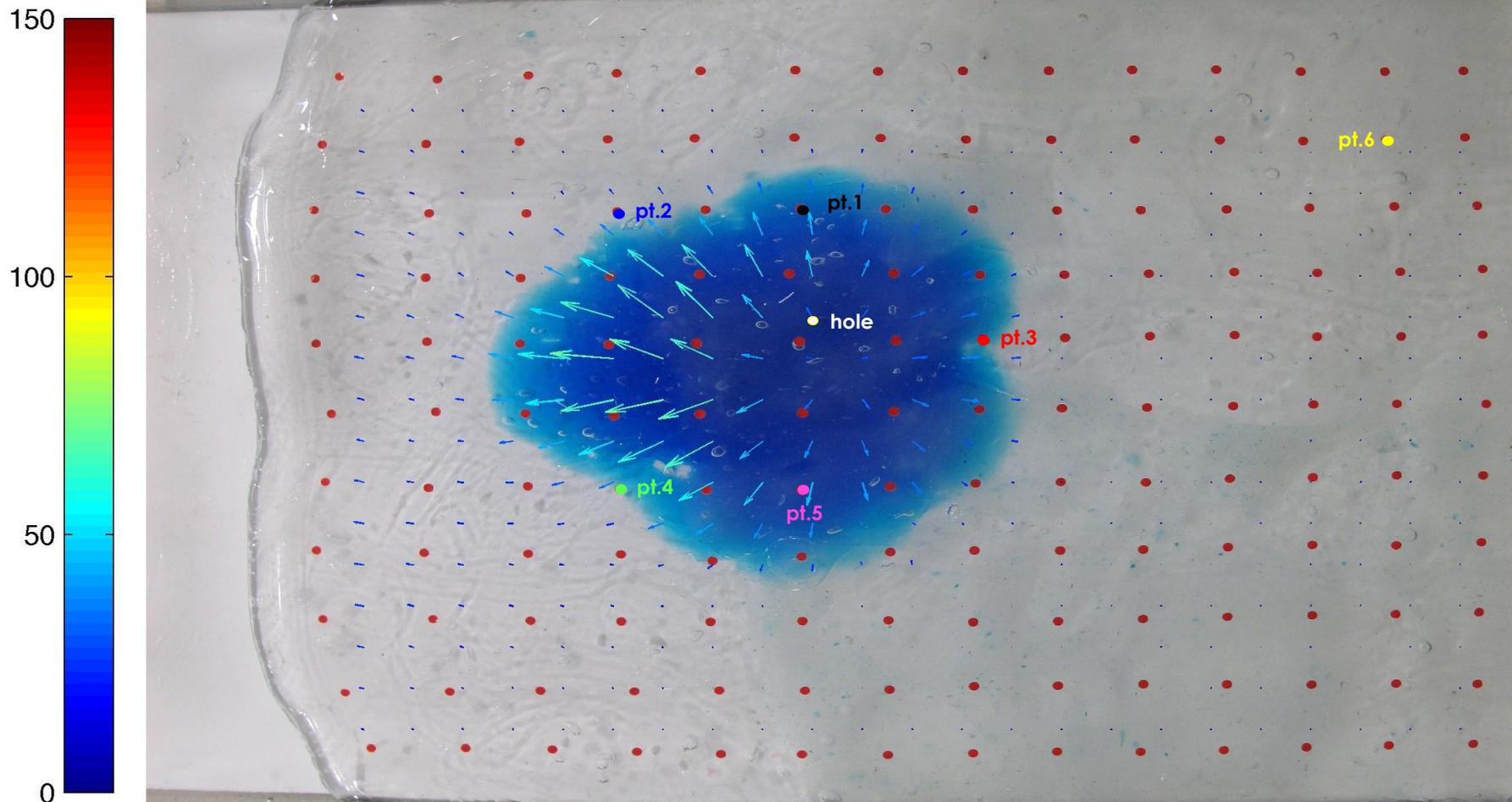
velocity (cm/hr)



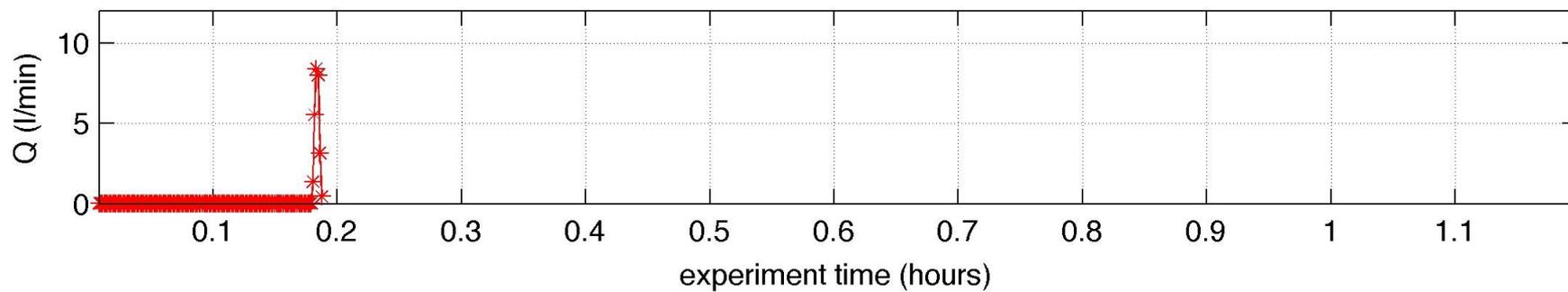
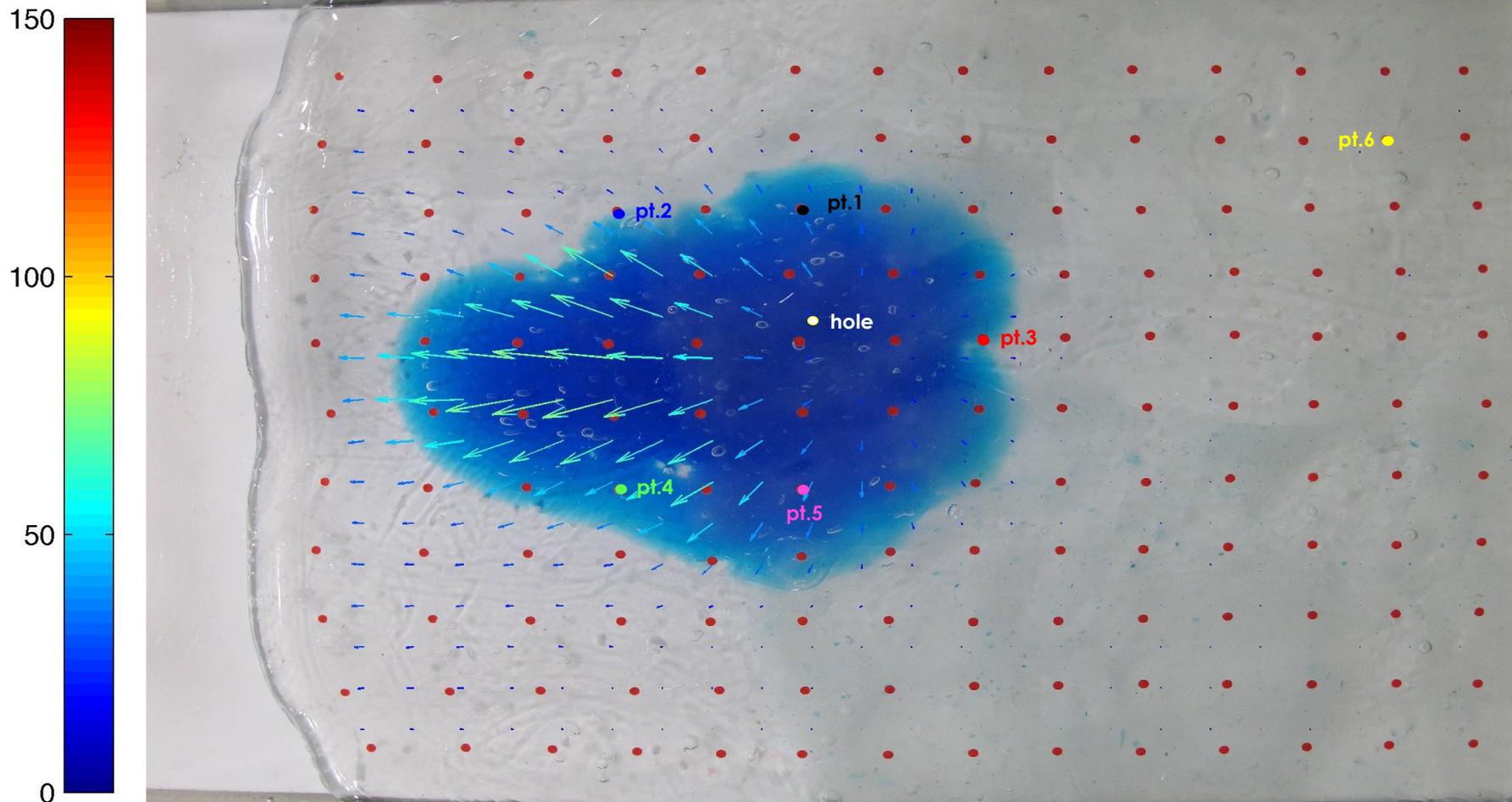
velocity (cm/hr)



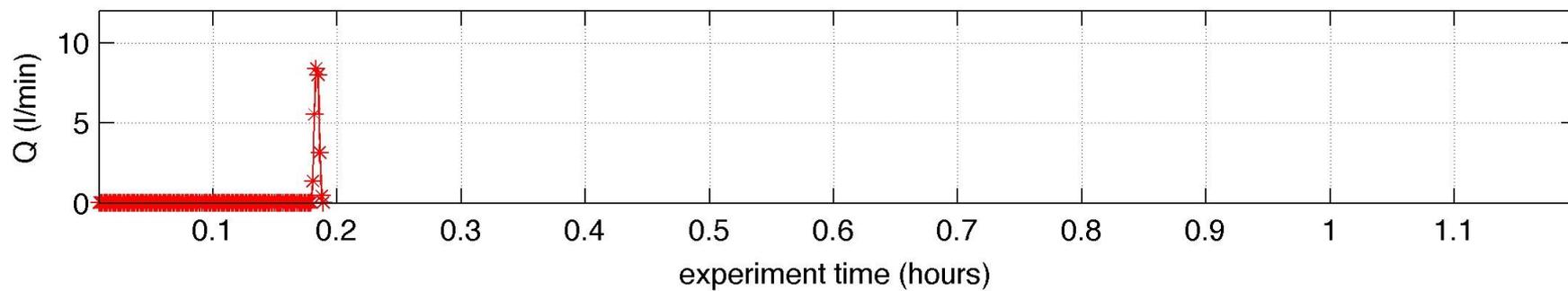
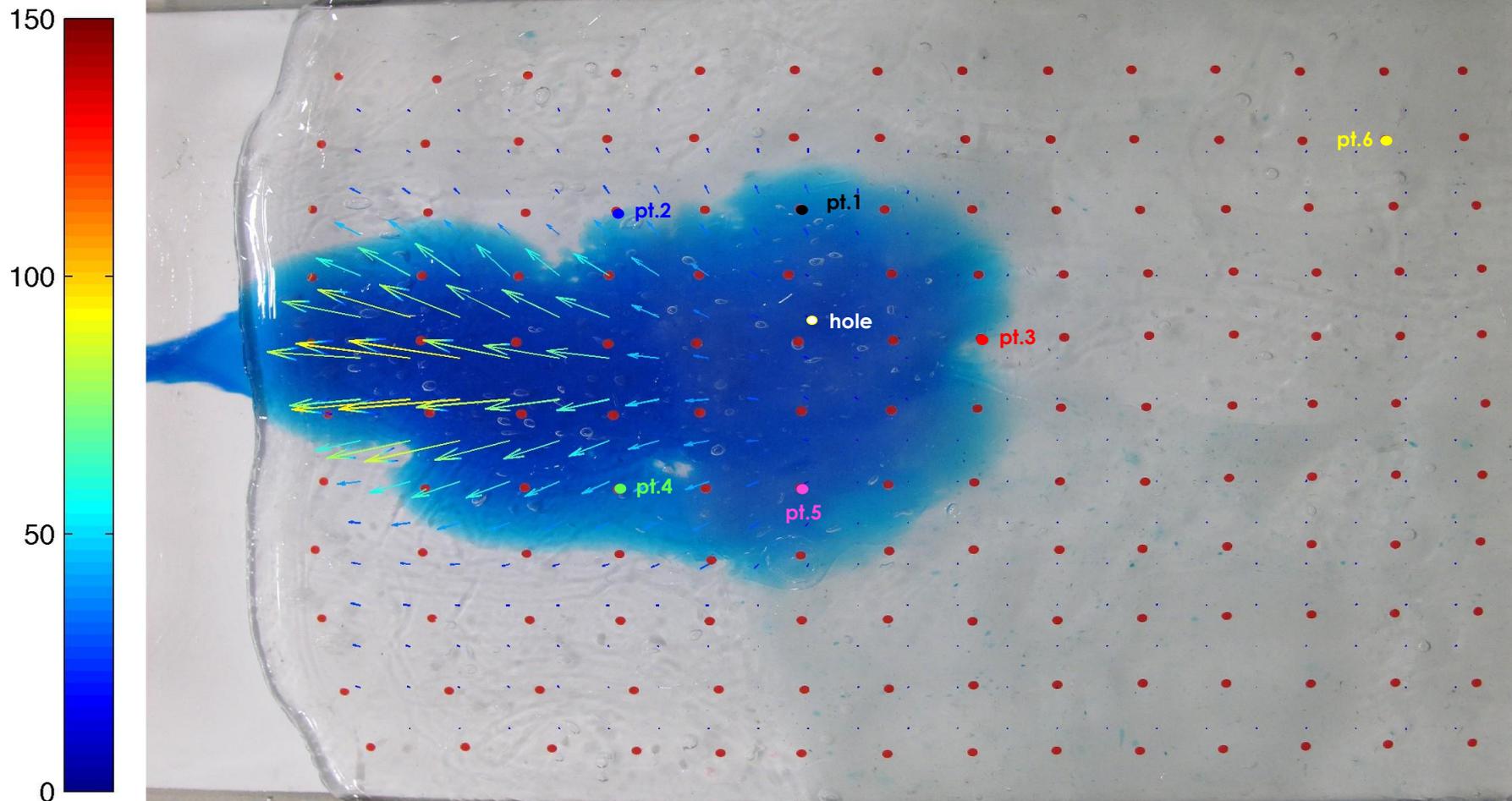
velocity (cm/hr)



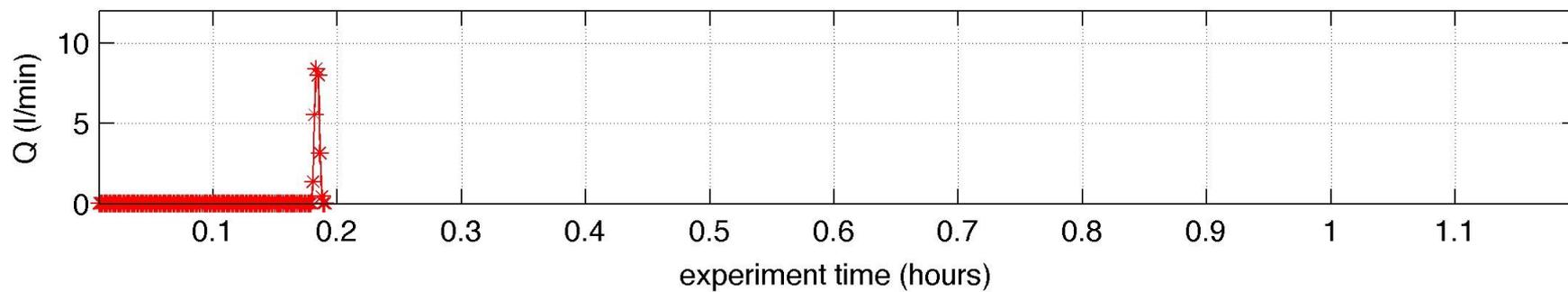
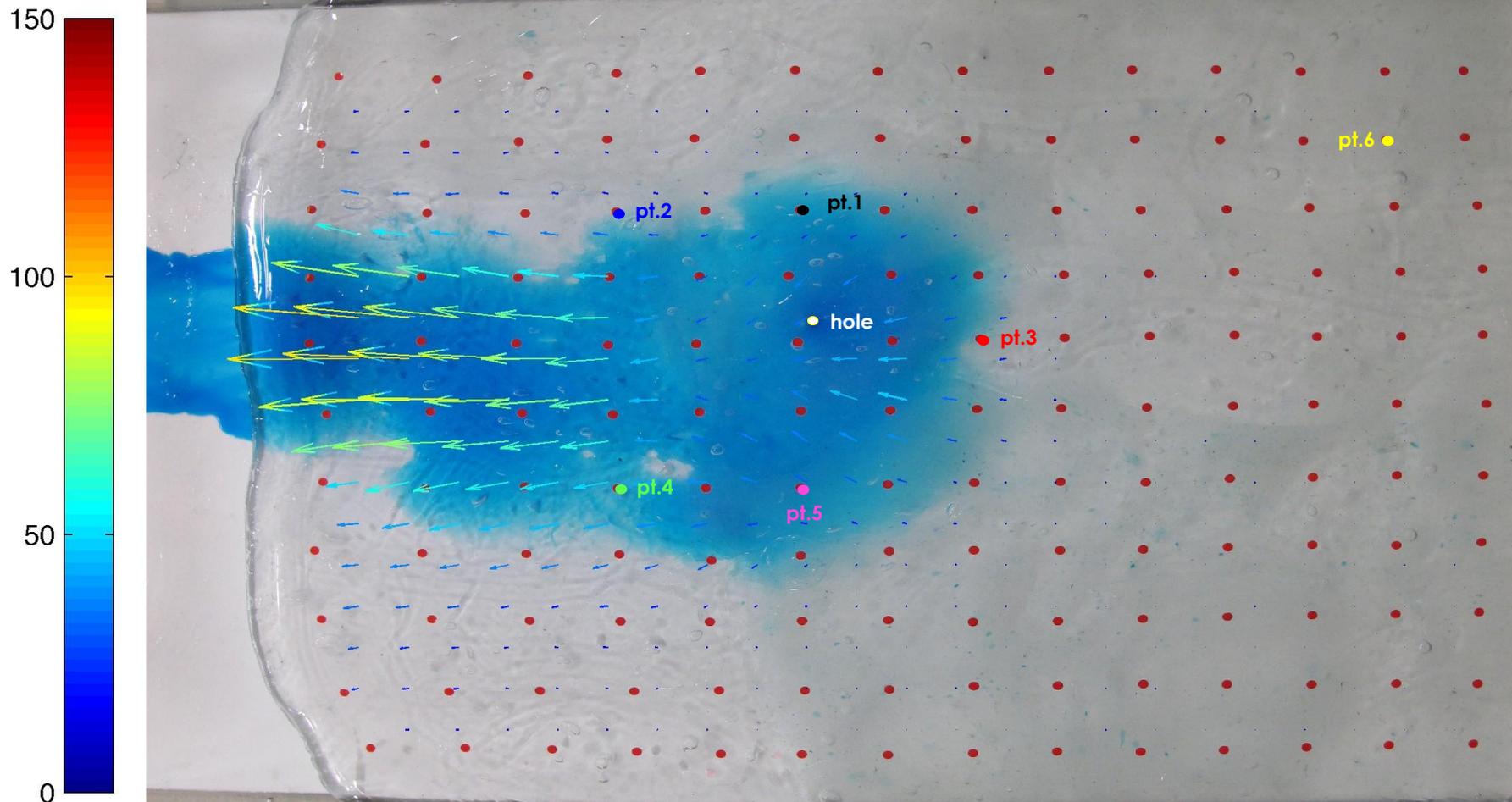
velocity (cm/hr)



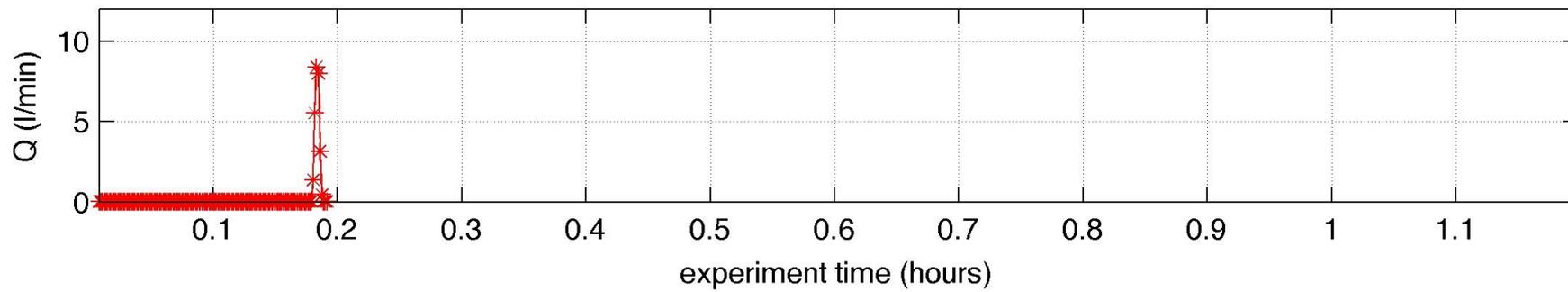
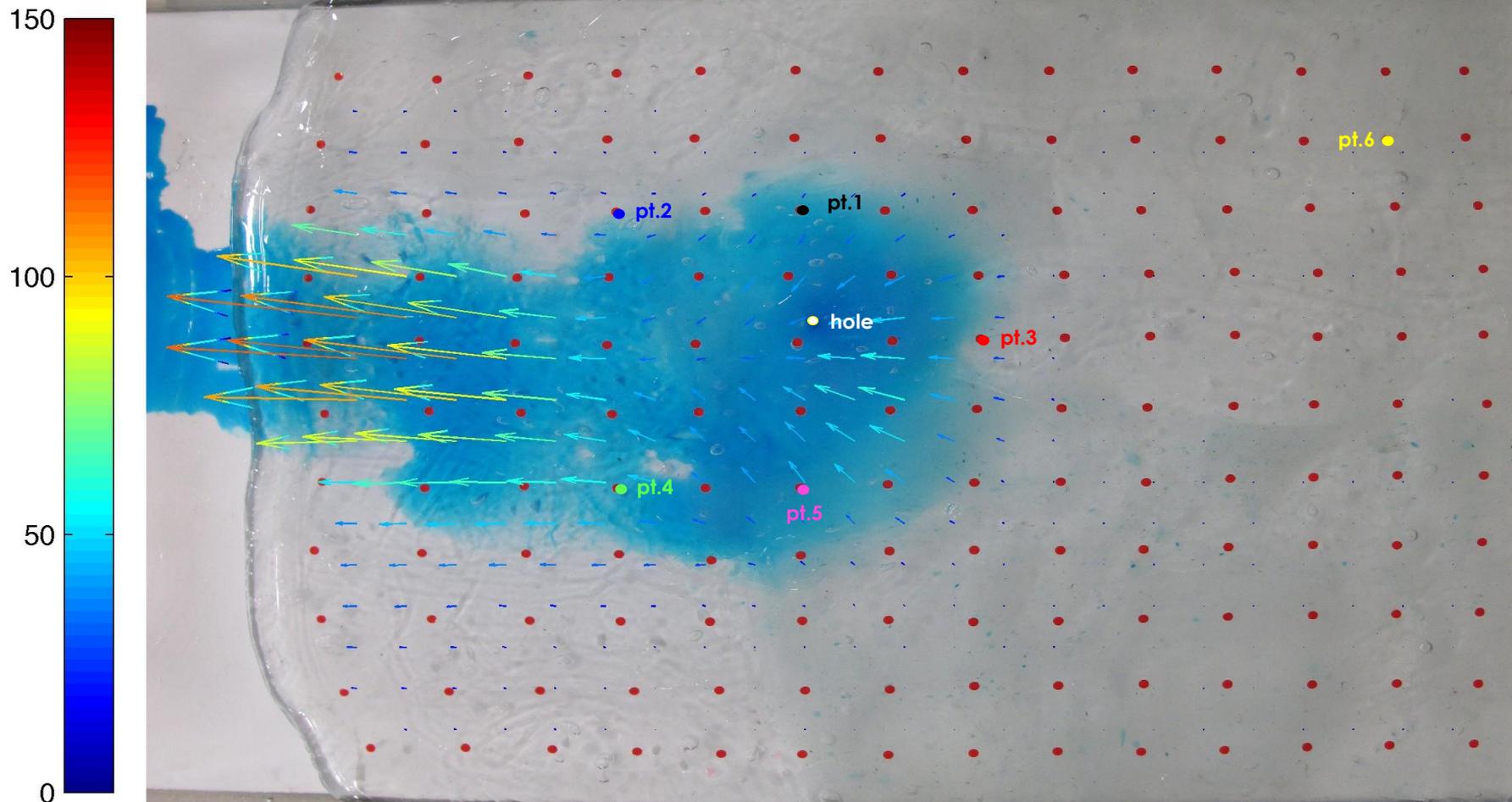
velocity (cm/hr)



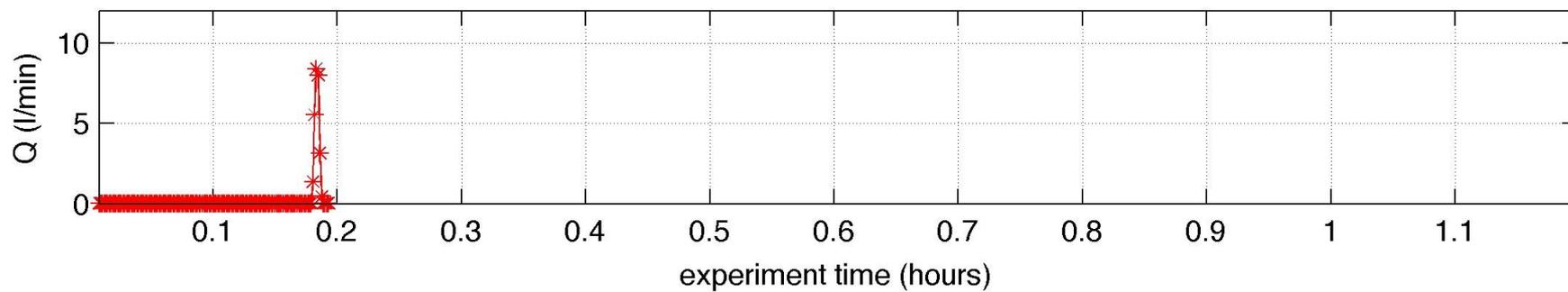
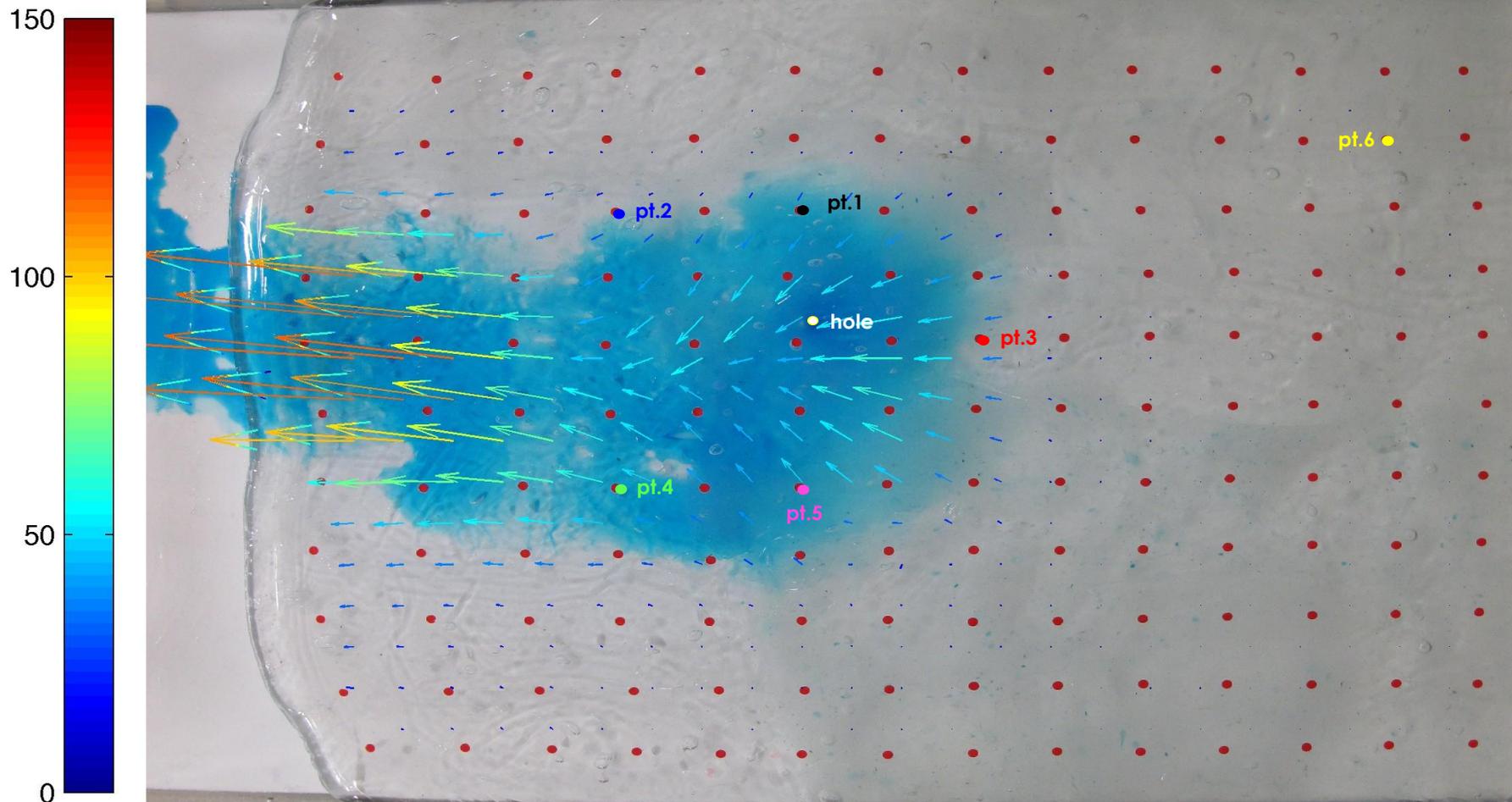
velocity (cm/hr)



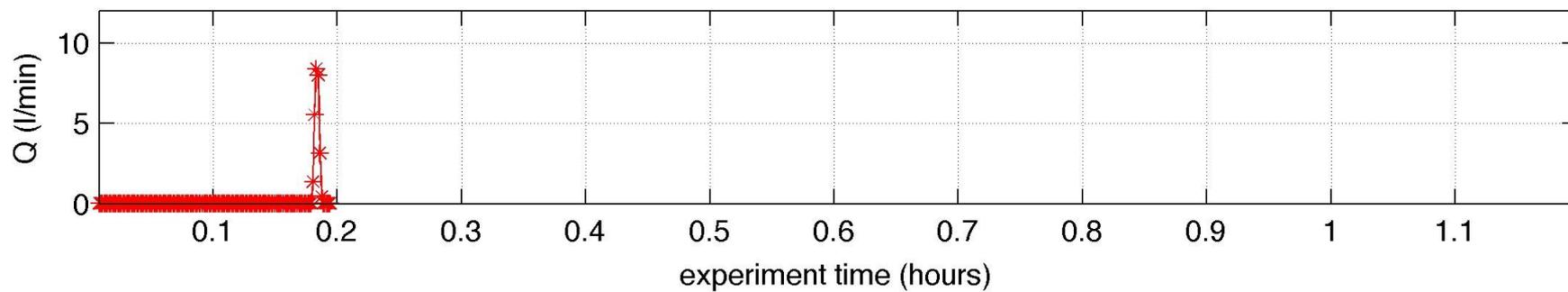
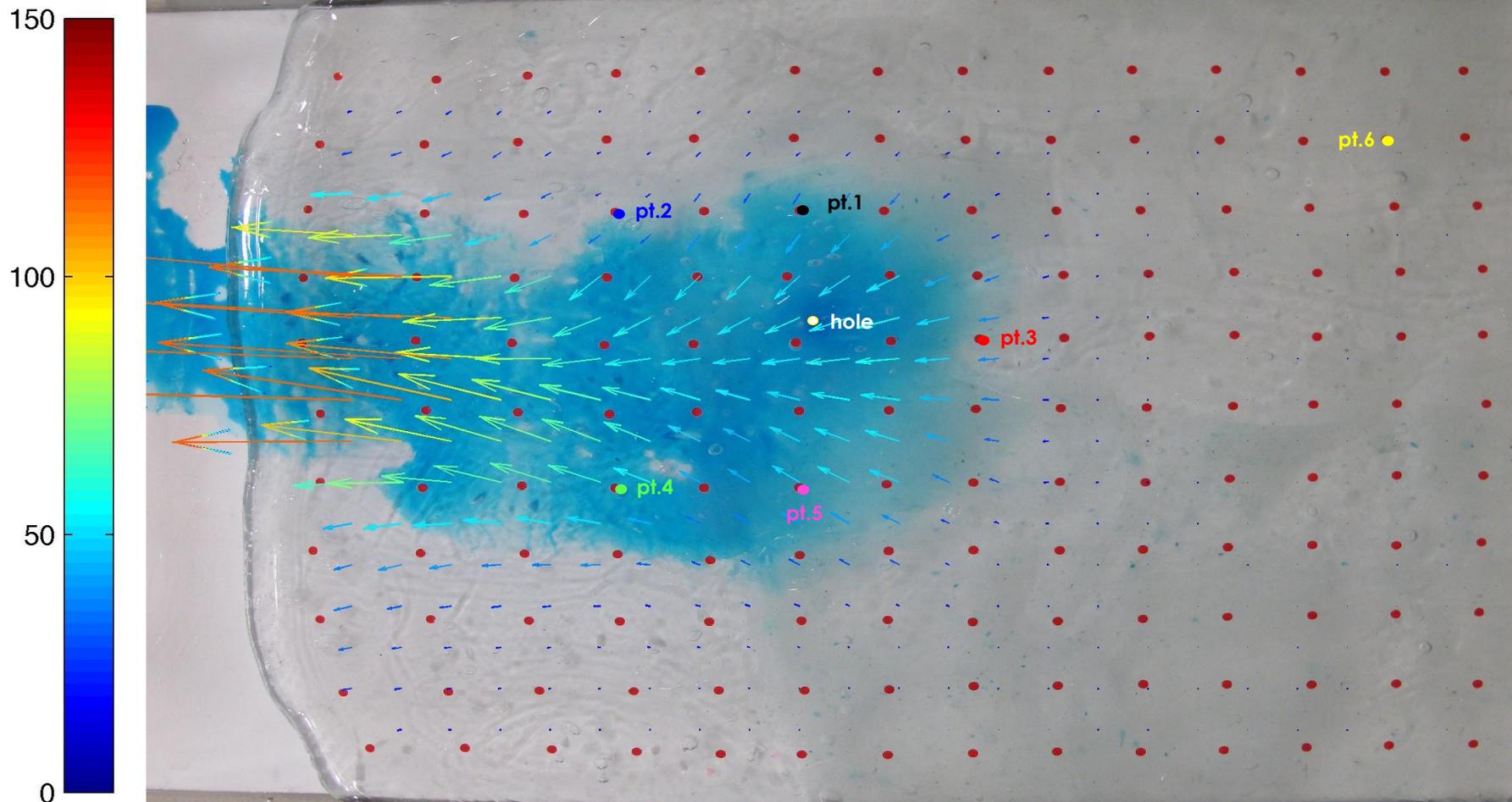
velocity (cm/hr)



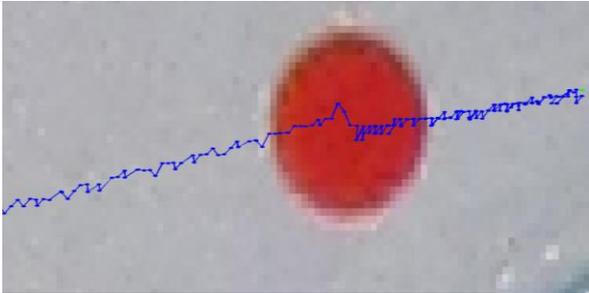
velocity (cm/hr)



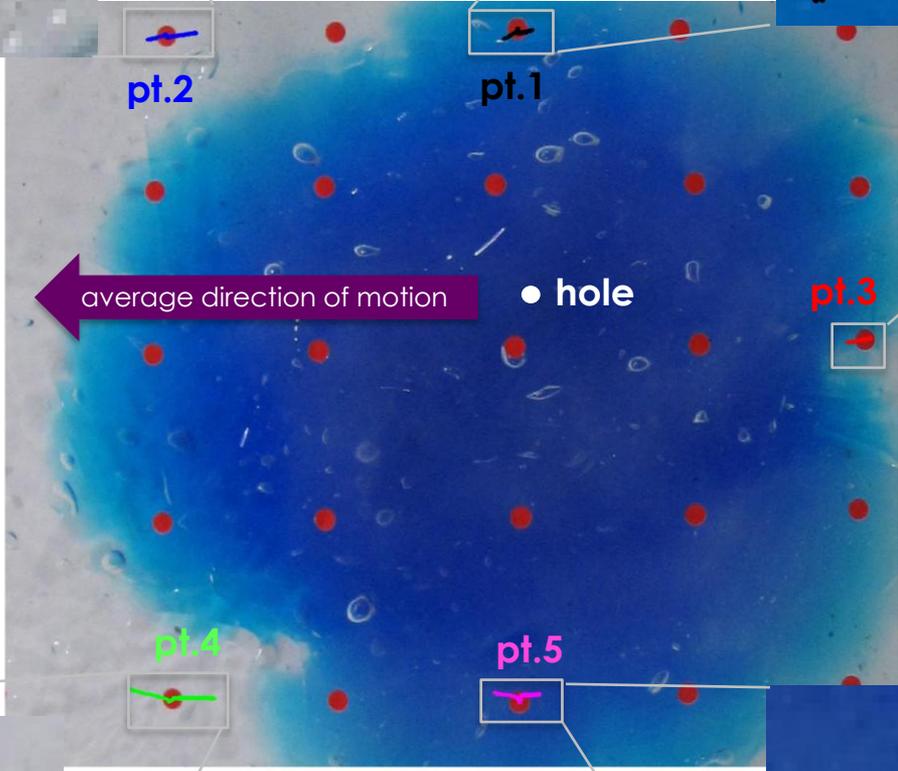
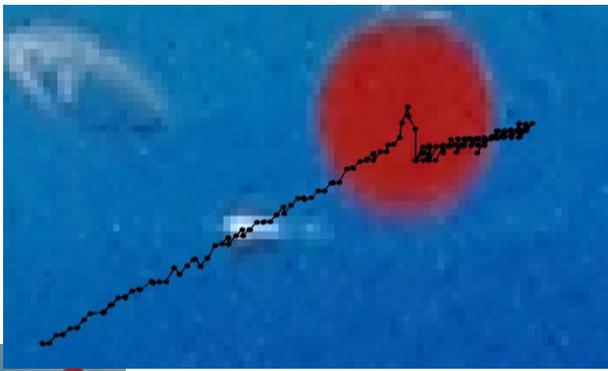
velocity (cm/hr)



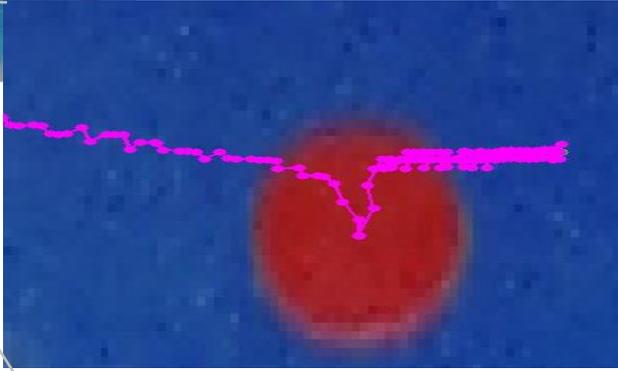
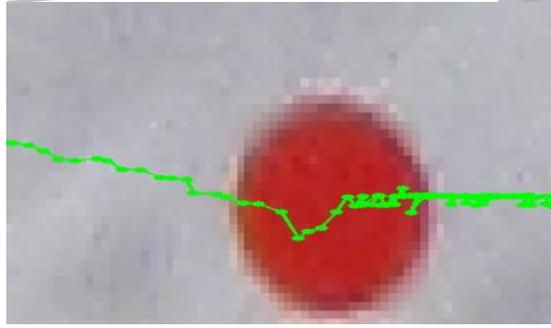
# Physical Model: discharge variability



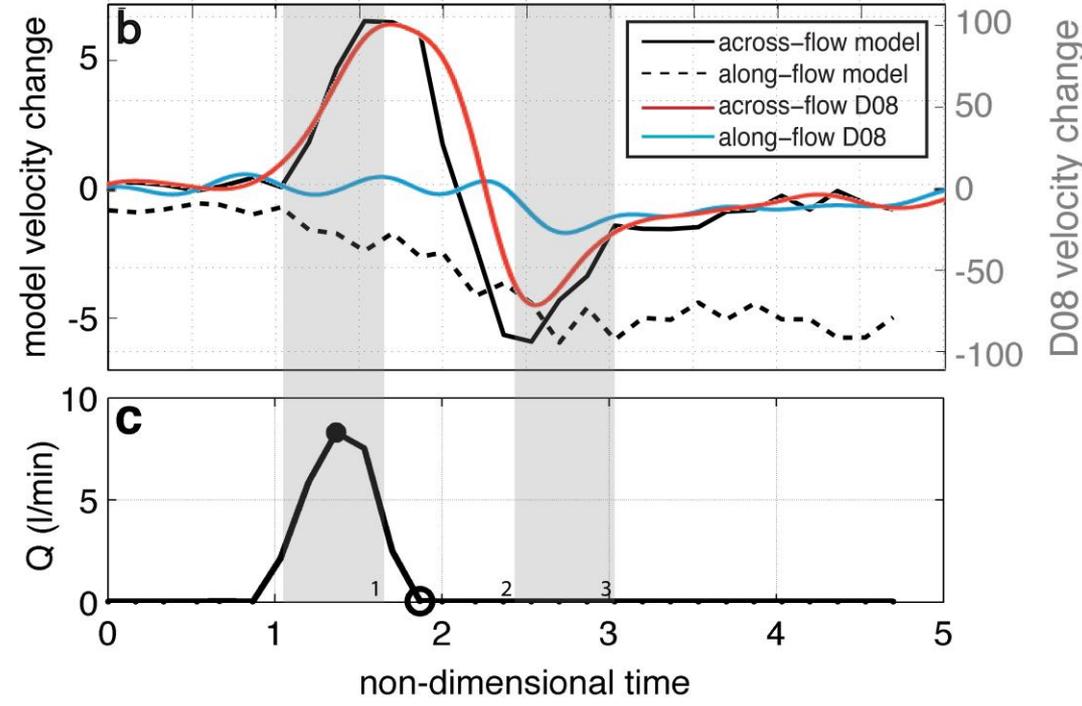
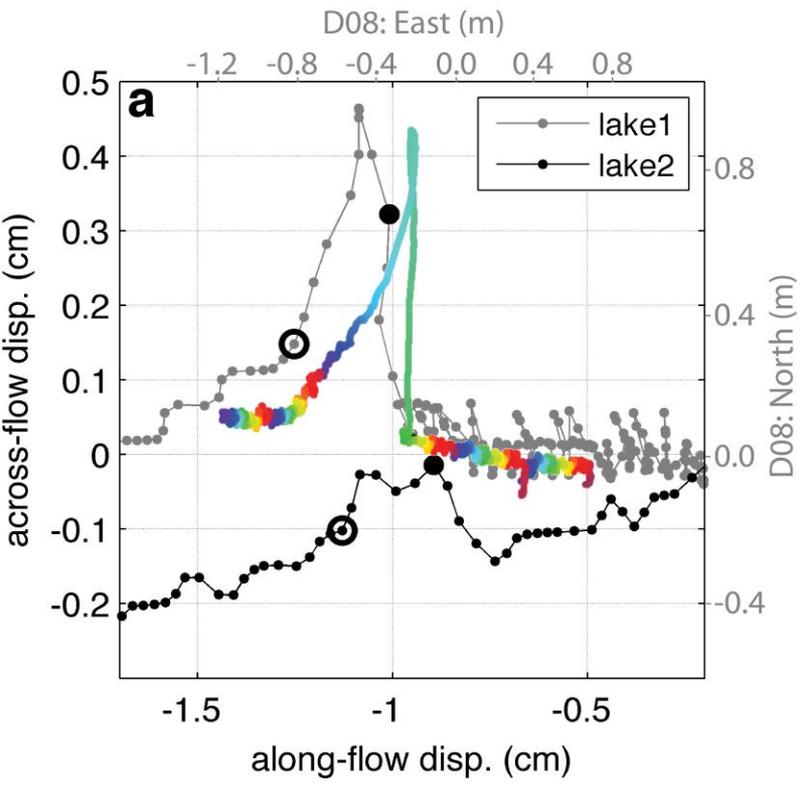
tracking the points on the surface through time



pt. 3 backtracks onto itself



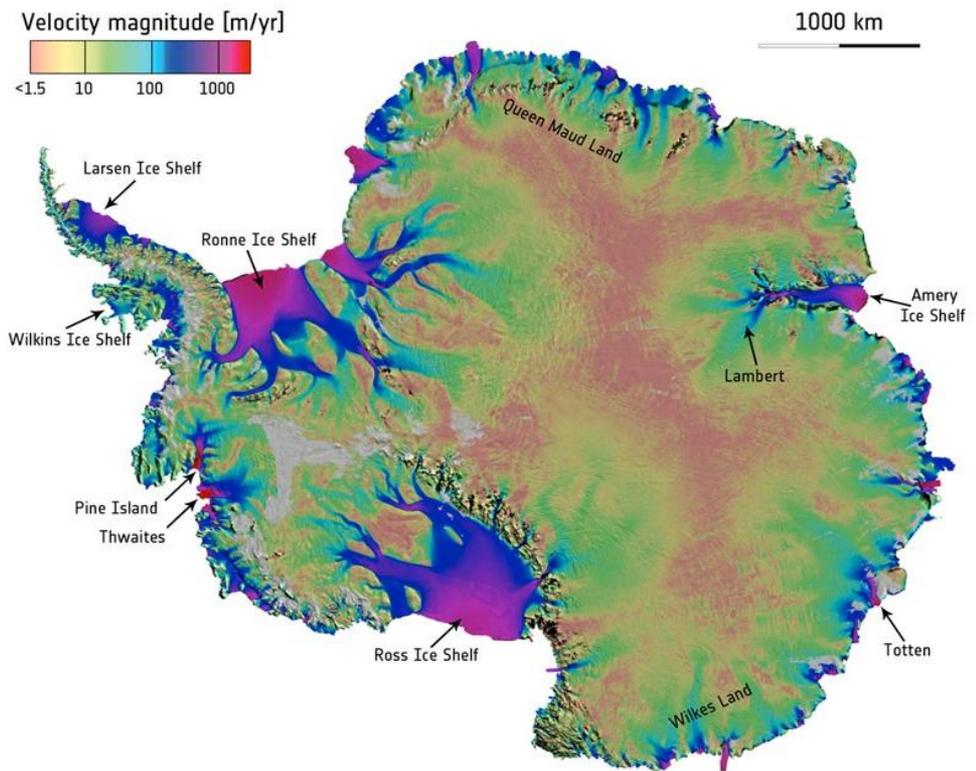
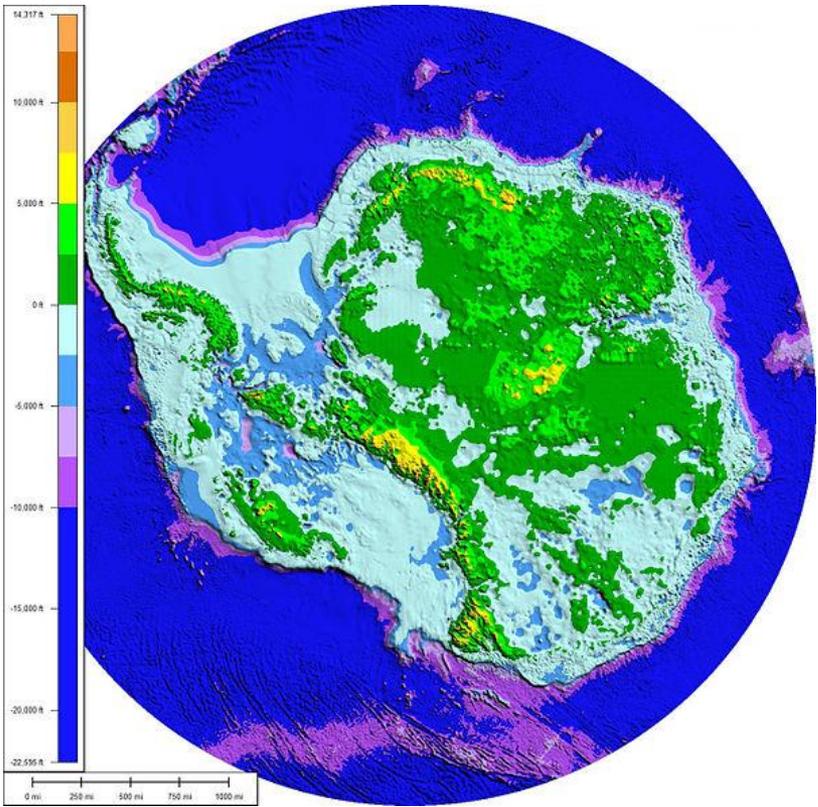
# Physical Model: discharge variability



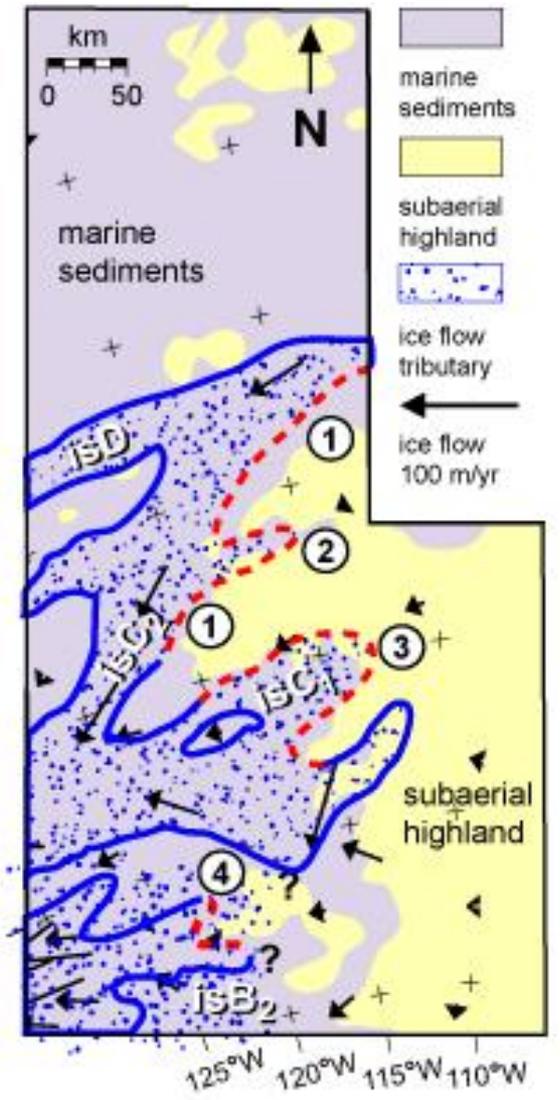
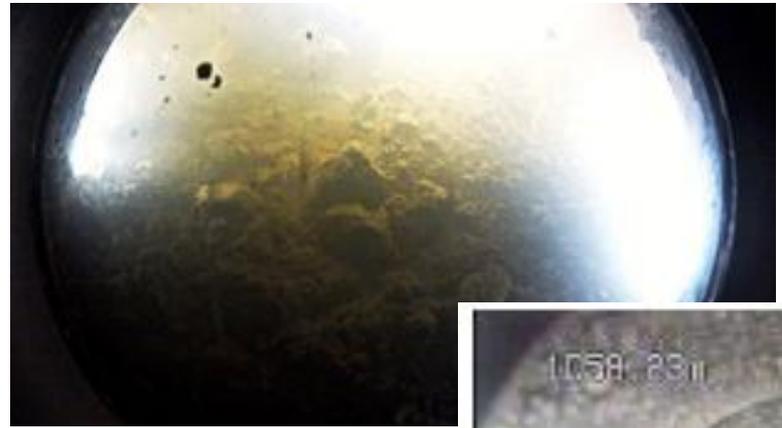
- overburden is important in that it re-sets the system when discharge decreases

# Glacier Fundamentals: basal sliding

- what about channel system beneath glaciers underlain with sediments?



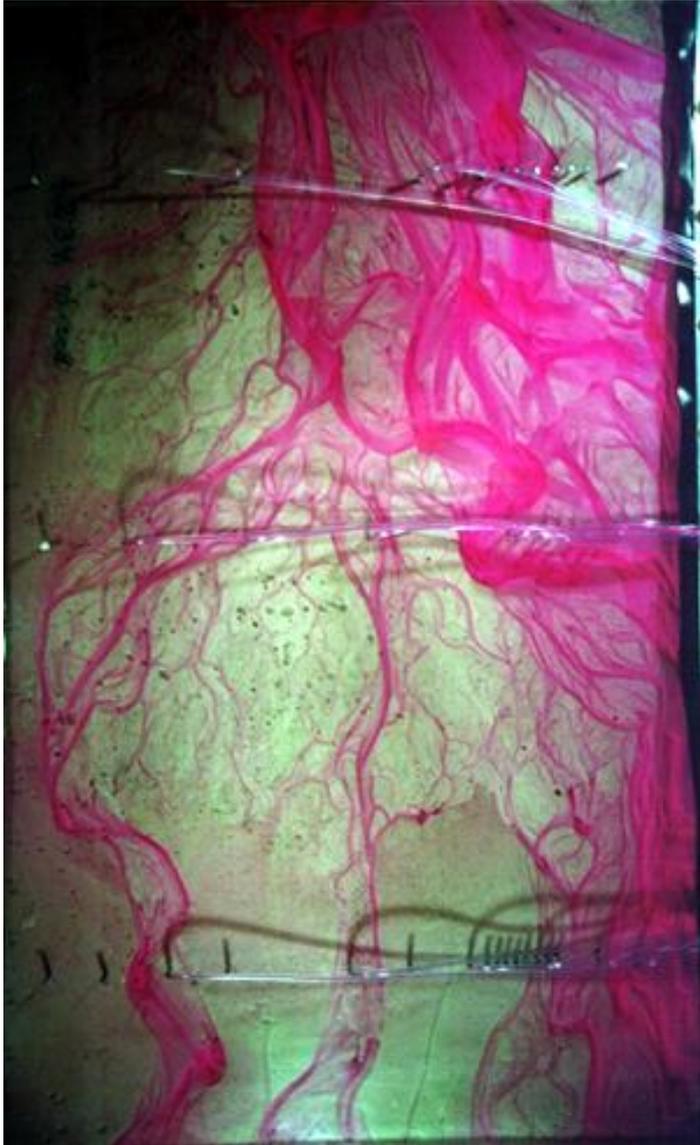
# Glacier Fundamentals: basal sliding



**Physical Model:** ice stream subglacial drainage

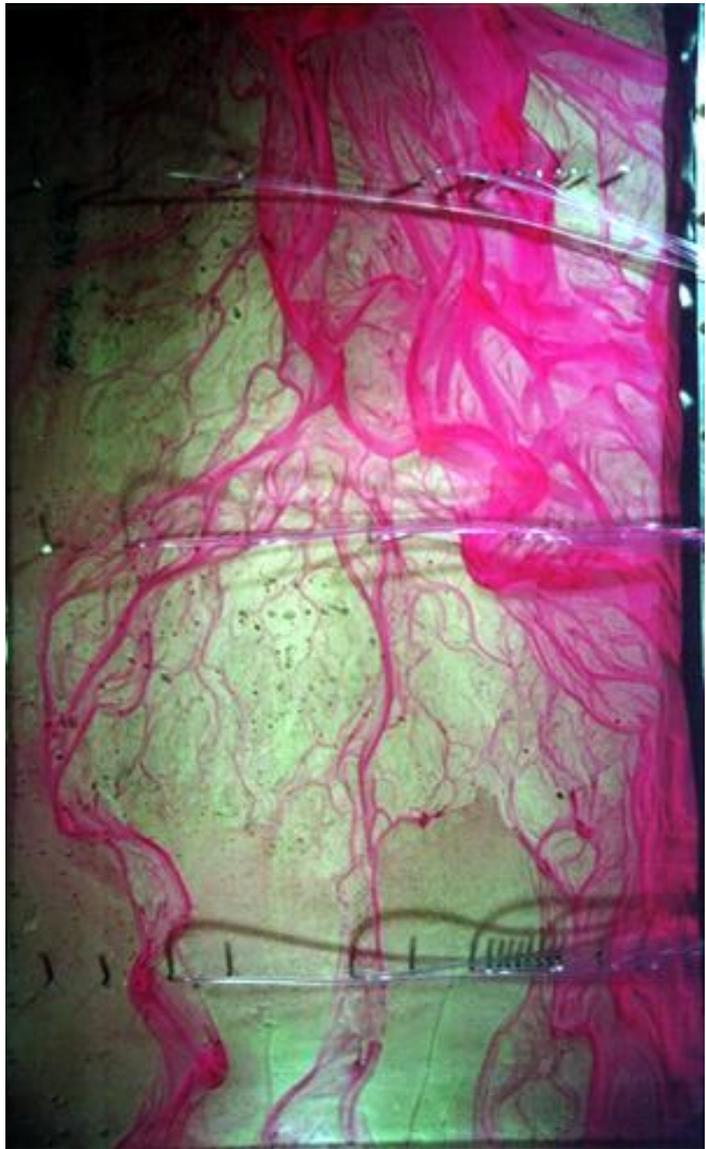


## Physical Model: ice stream subglacial drainage



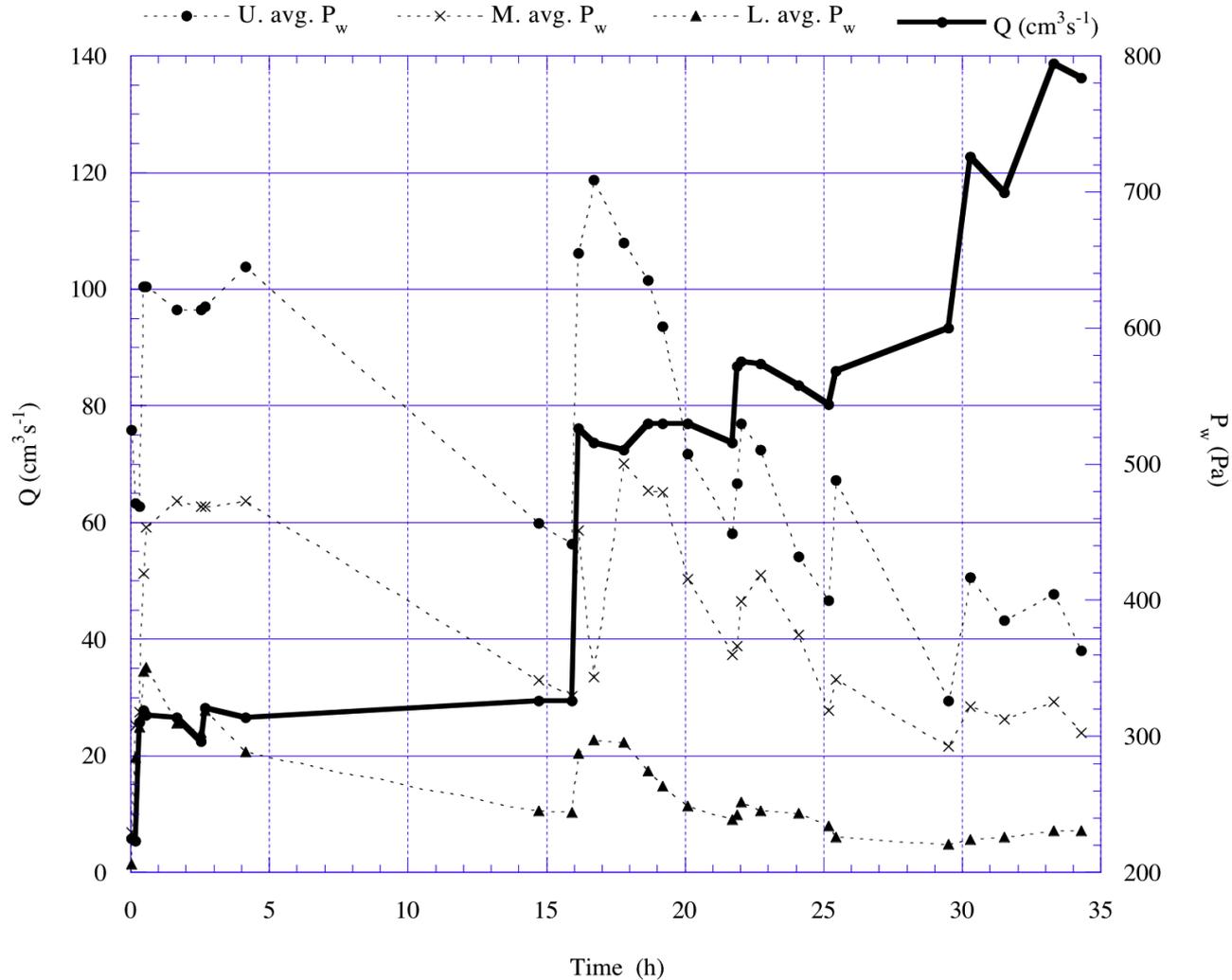
- near-flat surface slope creates lateral pressure gradients on scale of downstream pressure gradients
- causes intricate braided channel network

**Physical Model:** ice stream subglacial drainage

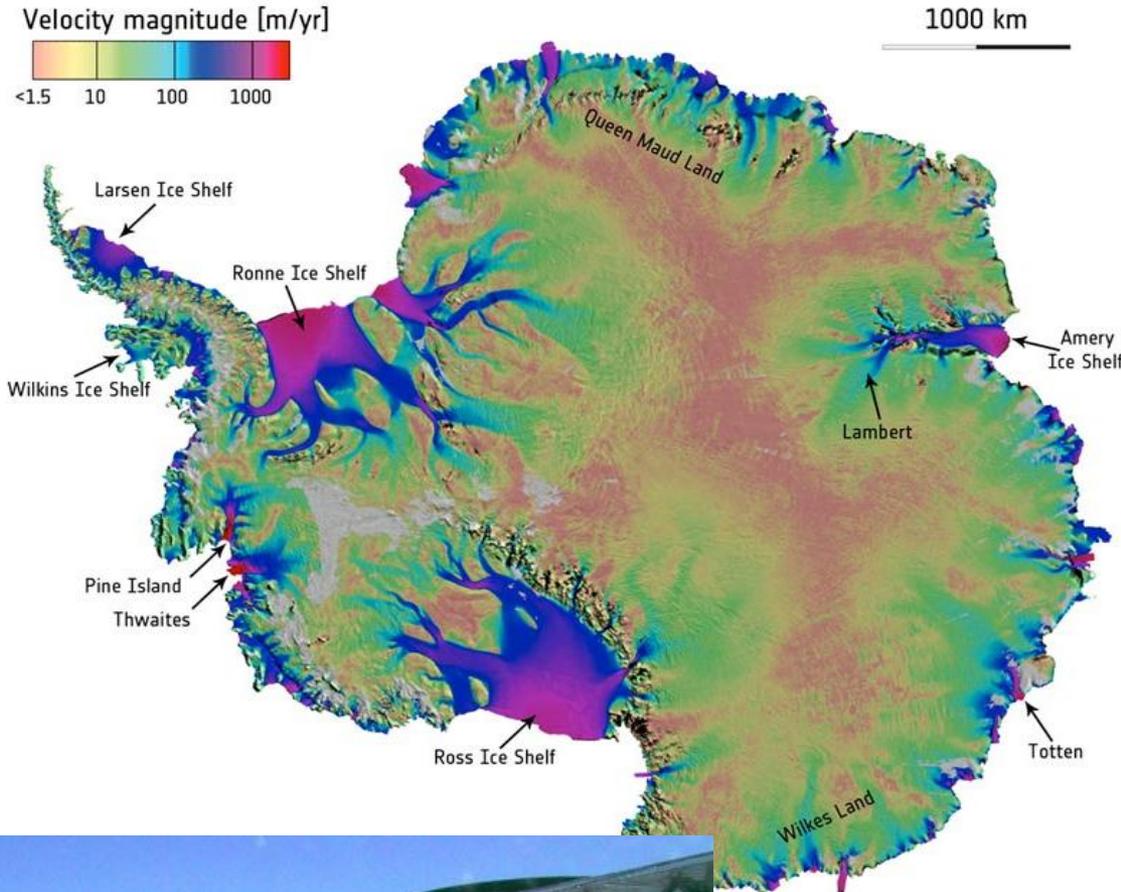


# Physical Model: ice stream subglacial drainage

- increases in water flux cause increases in pressure in the system
- but, sediment erosion allows for drops in pressure over time; depend on sediment supply from upstream and erodibility of substrate to maintain high pressure



# Glacier Fundamentals: ice streams



# Glacier Fundamentals: ice stream force balance

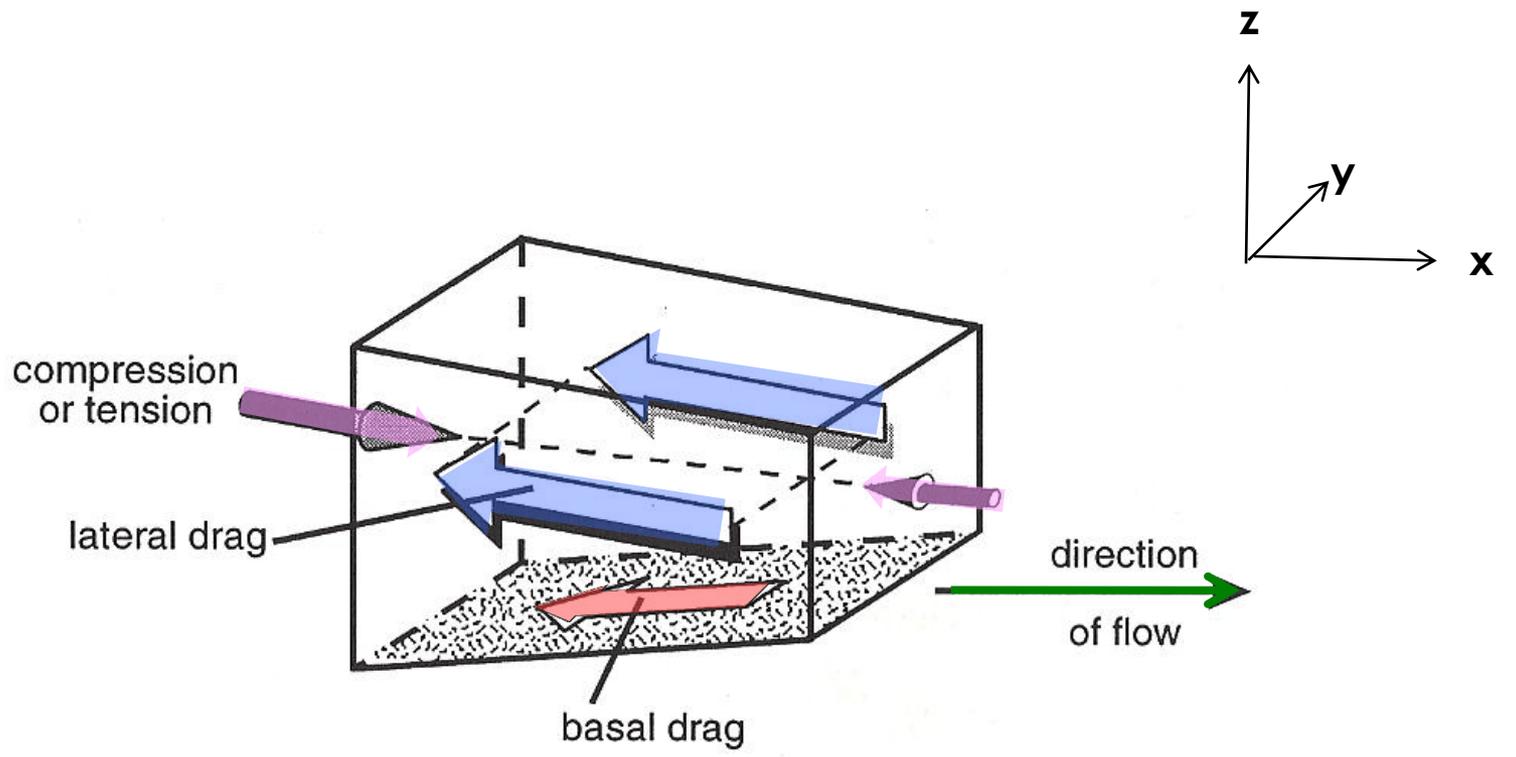
Gravitational  
Driving Stress

Basal Drag

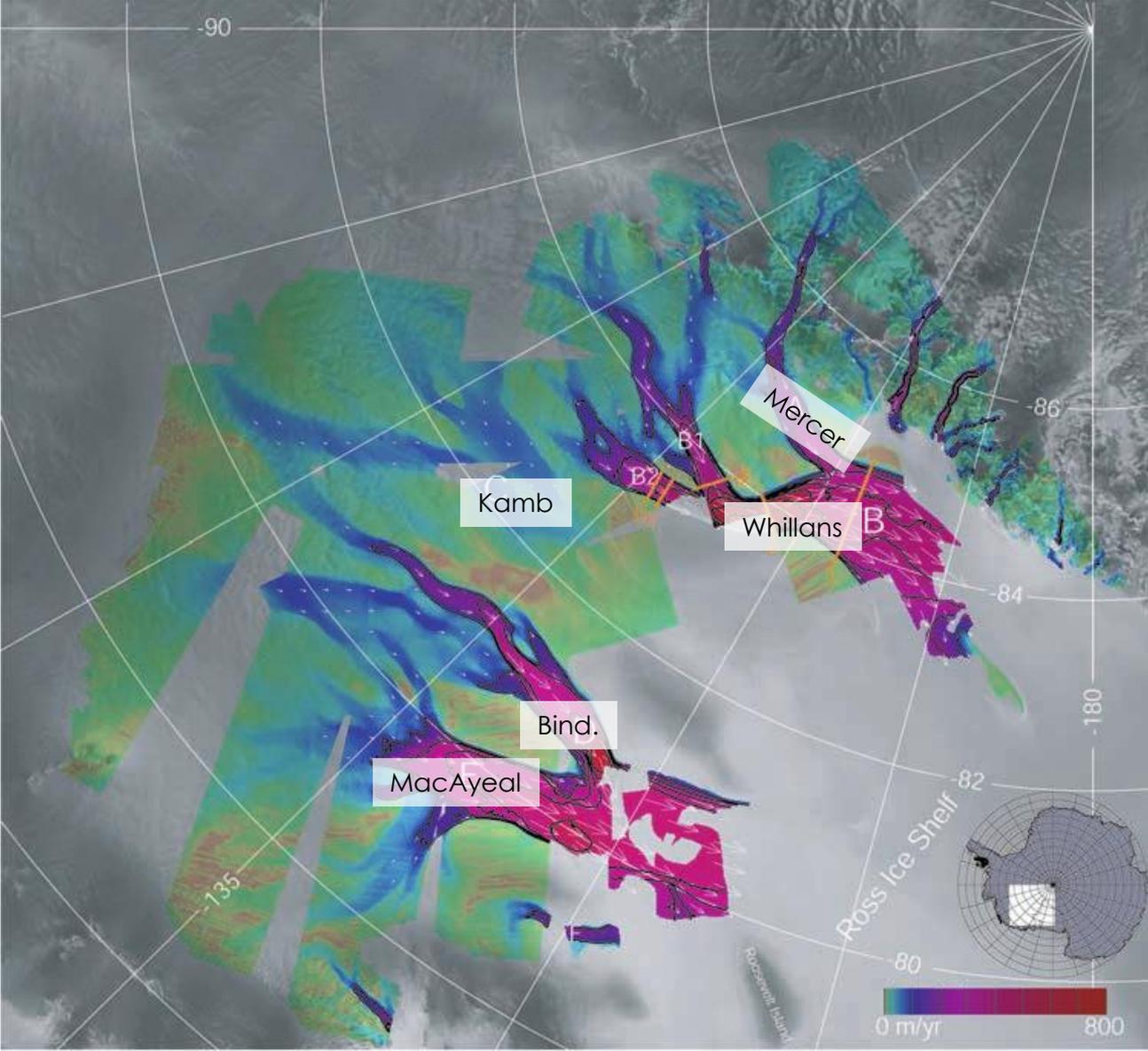
Compression  
Extension

Lateral Drag

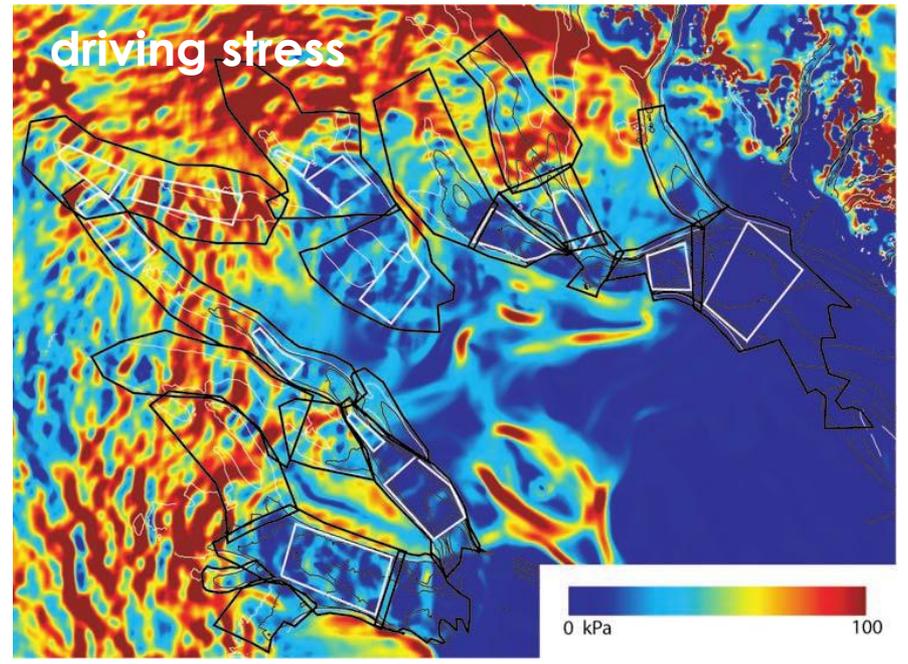
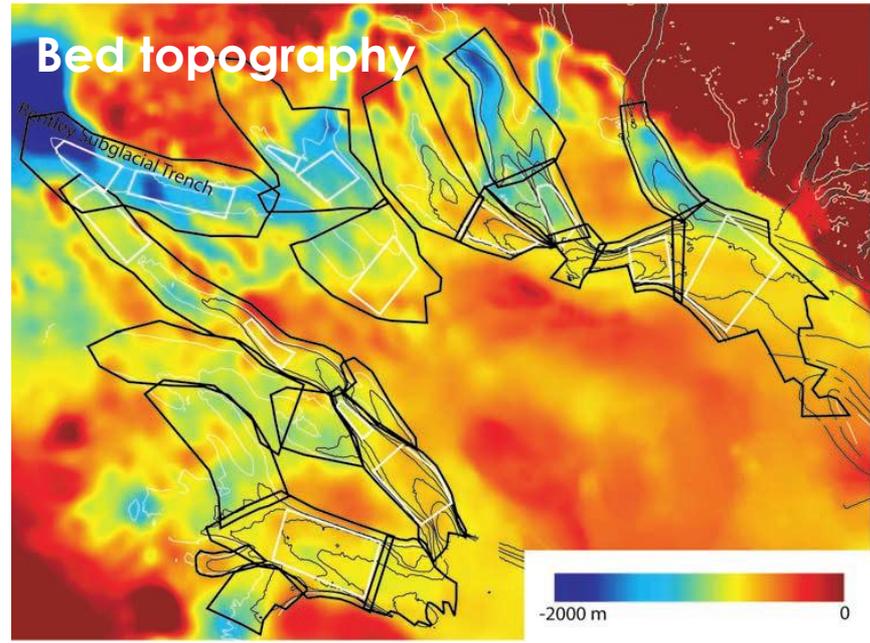
$$\tau_{dx} = \tau_{bx} - \frac{\partial}{\partial x} HR_{xx} - \frac{\partial}{\partial y} HR_{xy}$$



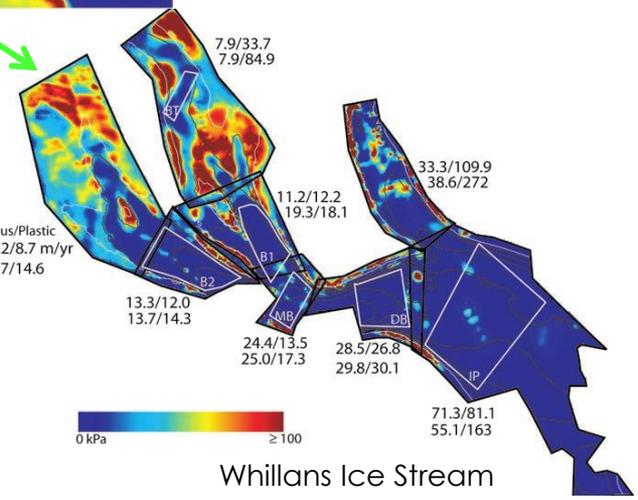
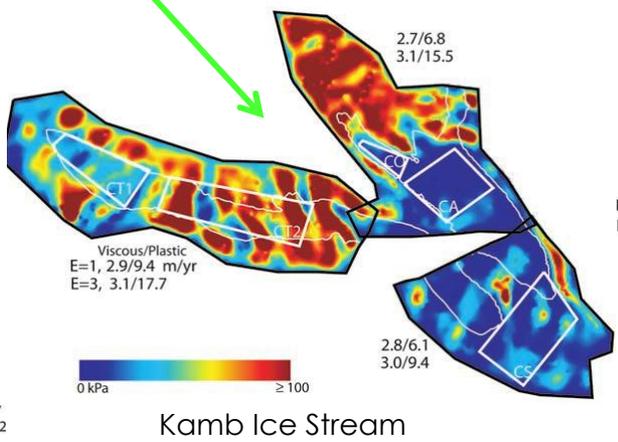
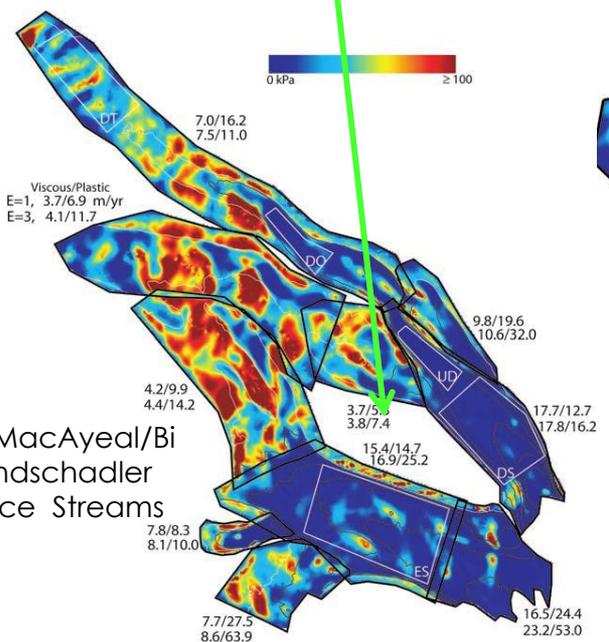
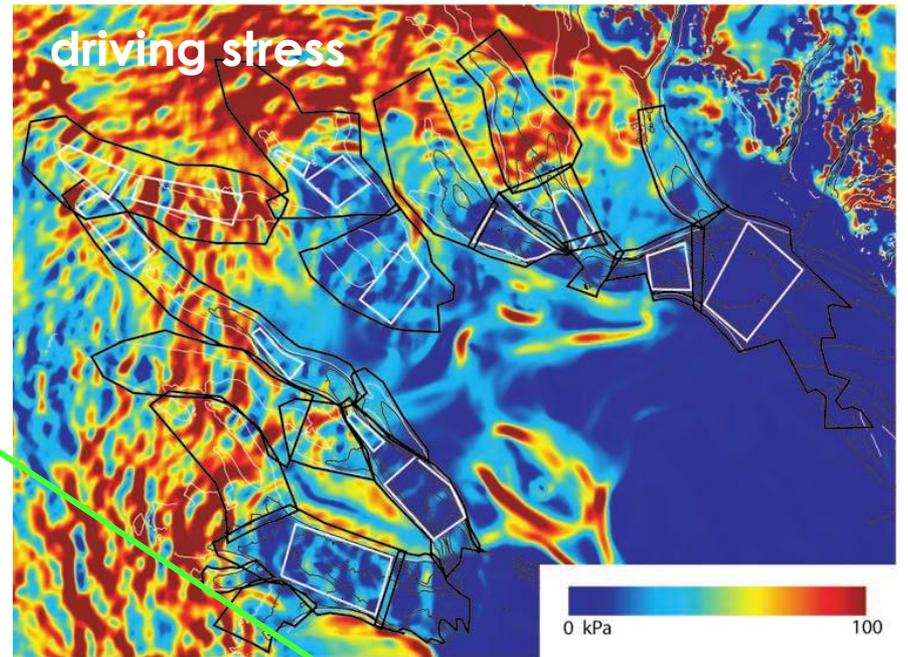
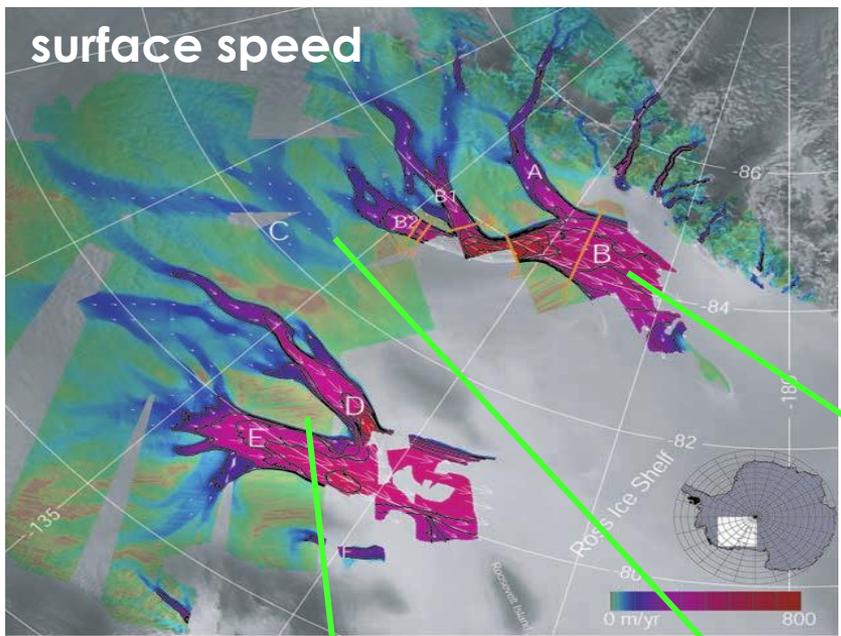
# Glacier Fundamentals: ice stream force balance



# Glacier Fundamentals: ice stream force balance

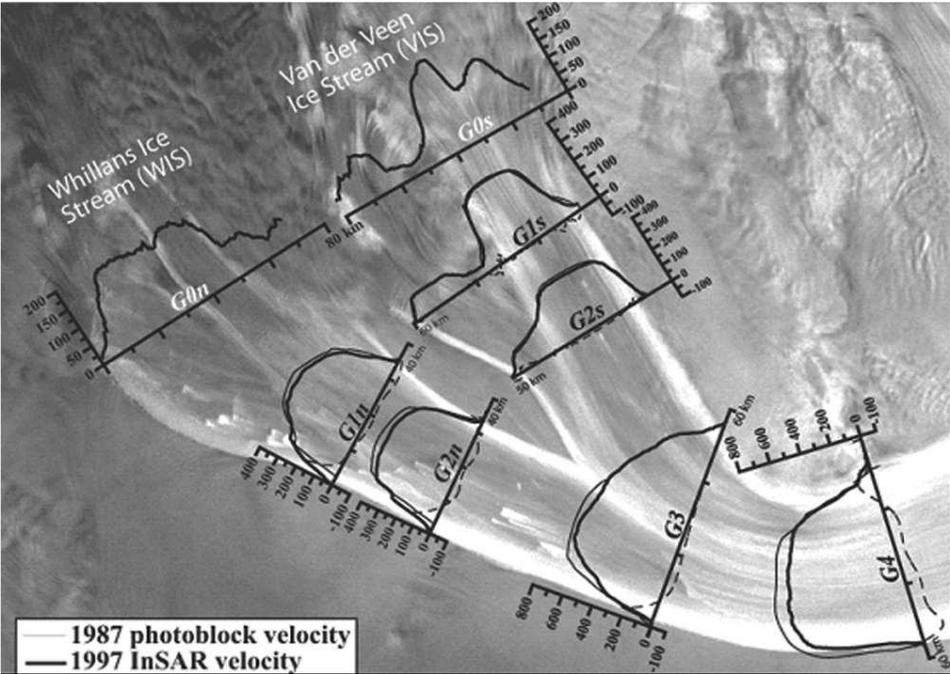


# Glacier Fundamentals: ice stream force balance



## BASAL DRAG

# Glacier Fundamentals: ice stream force balance



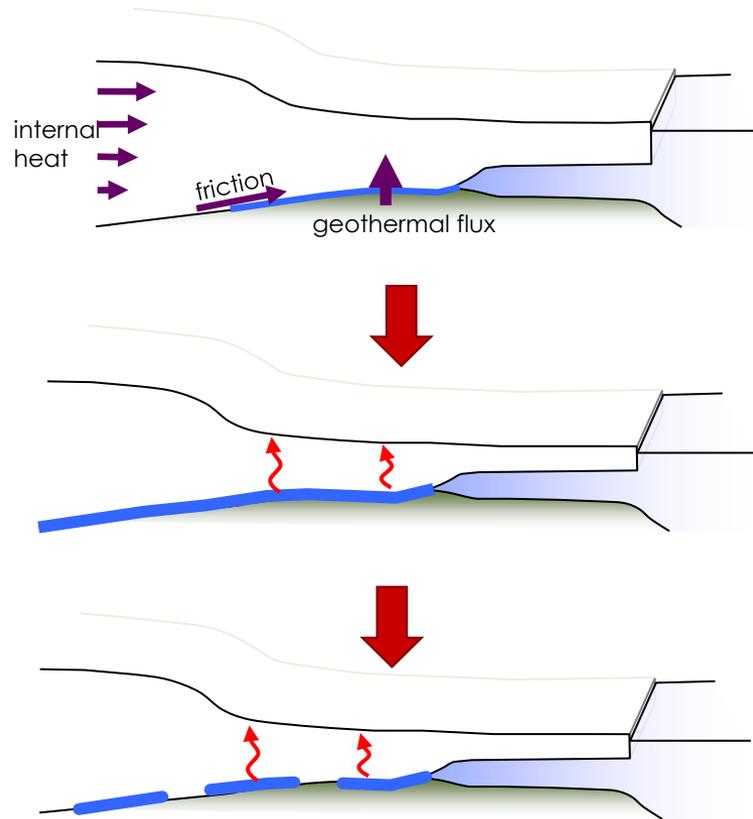
$$\tau_{dx} = \tau_{bx} - \frac{\partial}{\partial x} HR_{xx} - \frac{\partial}{\partial y} HR_{xy}$$

Basal Drag      Compression Extension      Lateral Drag

Transect	Driving stress kPa	percent supported by sides in 1987	lateral drag		basal drag	
			$\tau_w$ 1997 kPa	percent supported by sides in 1997	$\tau_{bx}$ 1997 kPa	
G0n-G1n	13.3 ± 1.1		7.1 ± 0.9	~53%	6.2 ± 1.4	
G1n-G3n	13.1 ± 1.0	~100%	11.8 ± 2.1	~90%	1.3 ± 2.3	
G3-G4	11.7 ± 0.9	~68%	7.2 ± 0.9	~61%	4.5 ± 1.3	

**over time more of the driving stress is supported by bed**

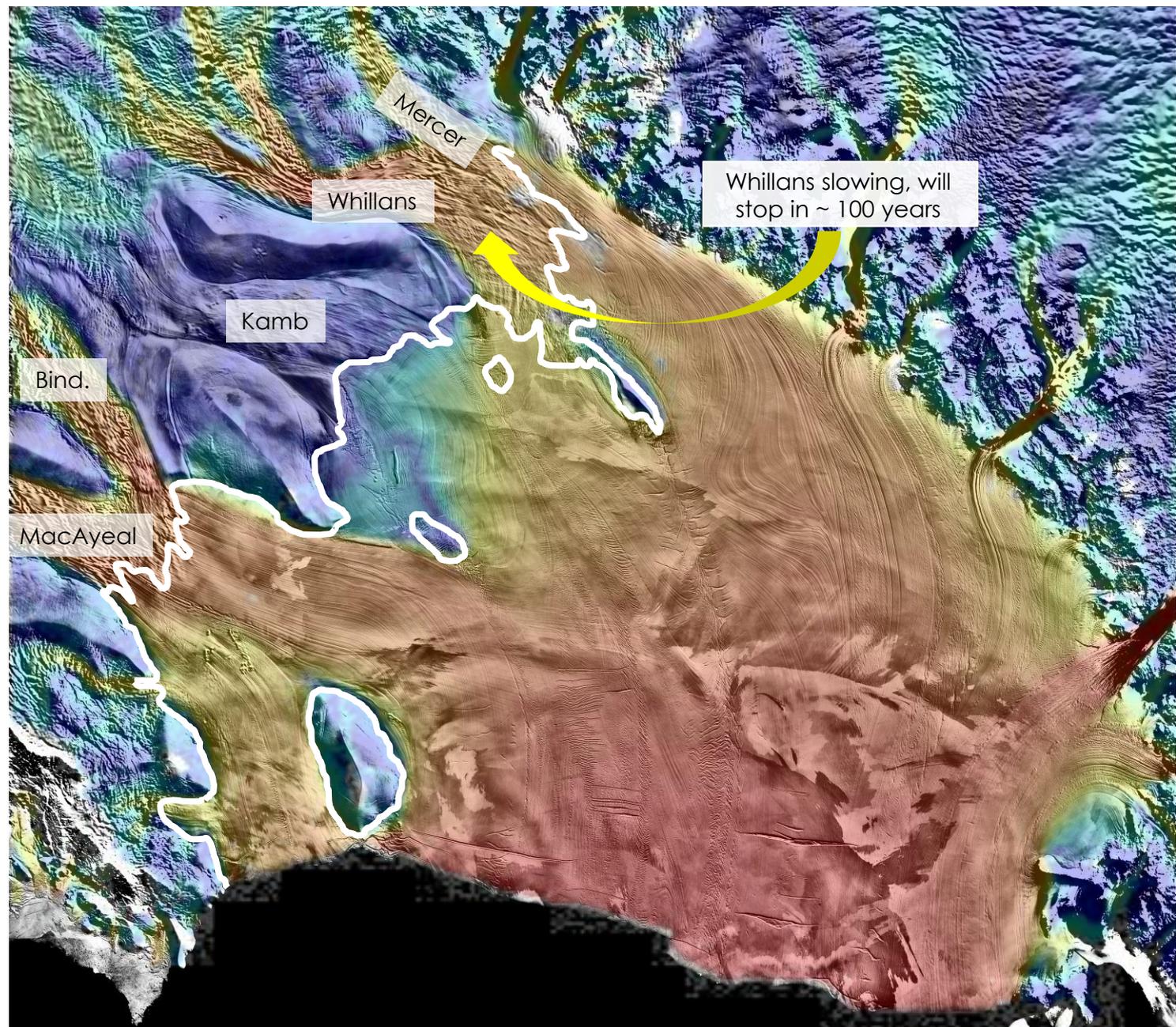
# Glacier Fundamentals: ice stream force balance



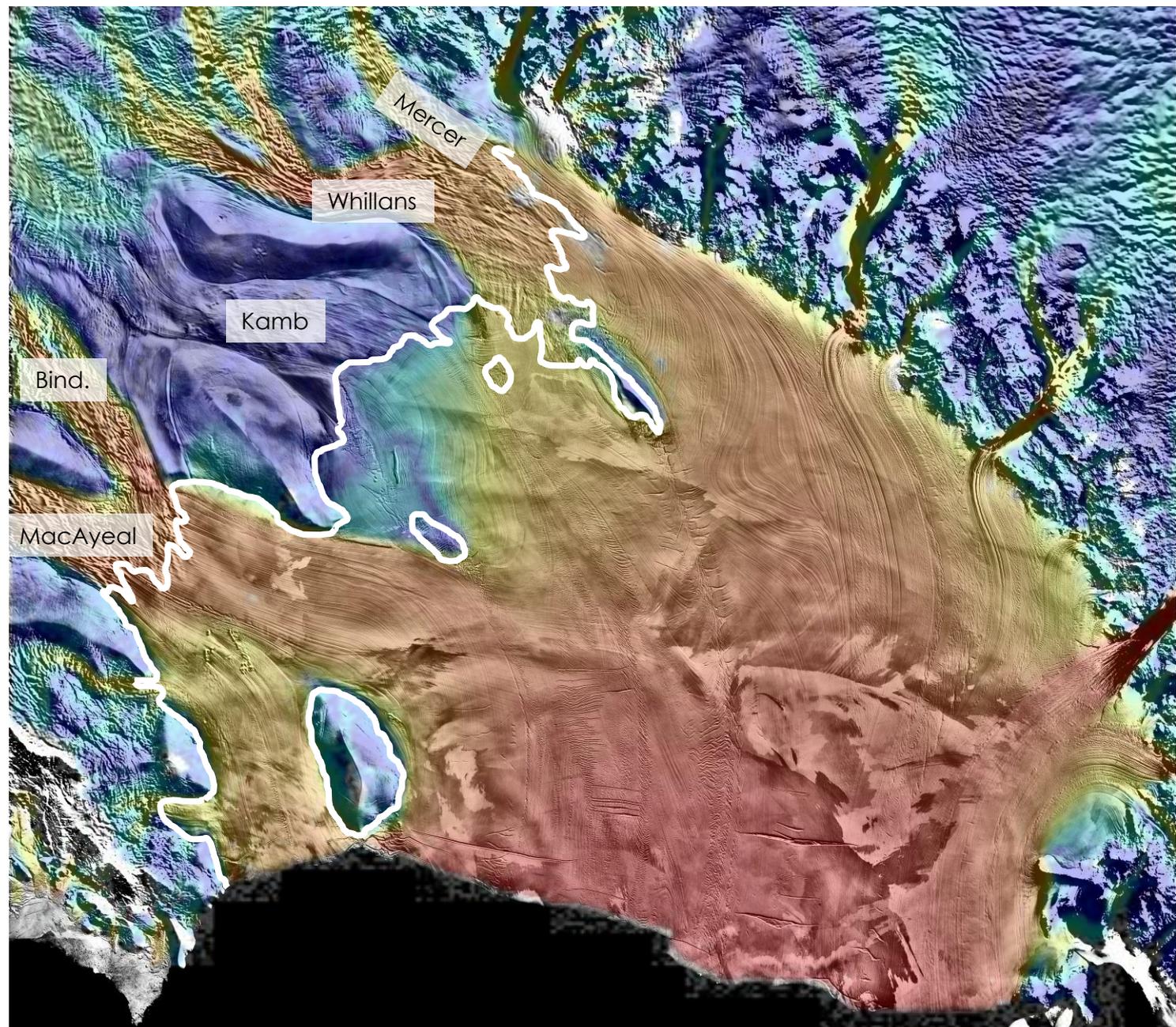
■

- thick ice/subglacial volcanism systems provide basal lubrication that permit fast flow
- fast flow leads to thinning, which steepens the internal temperature gradient causes freezing at the basal interface
- lubrication is removed or reduced, ice stream eventually stops

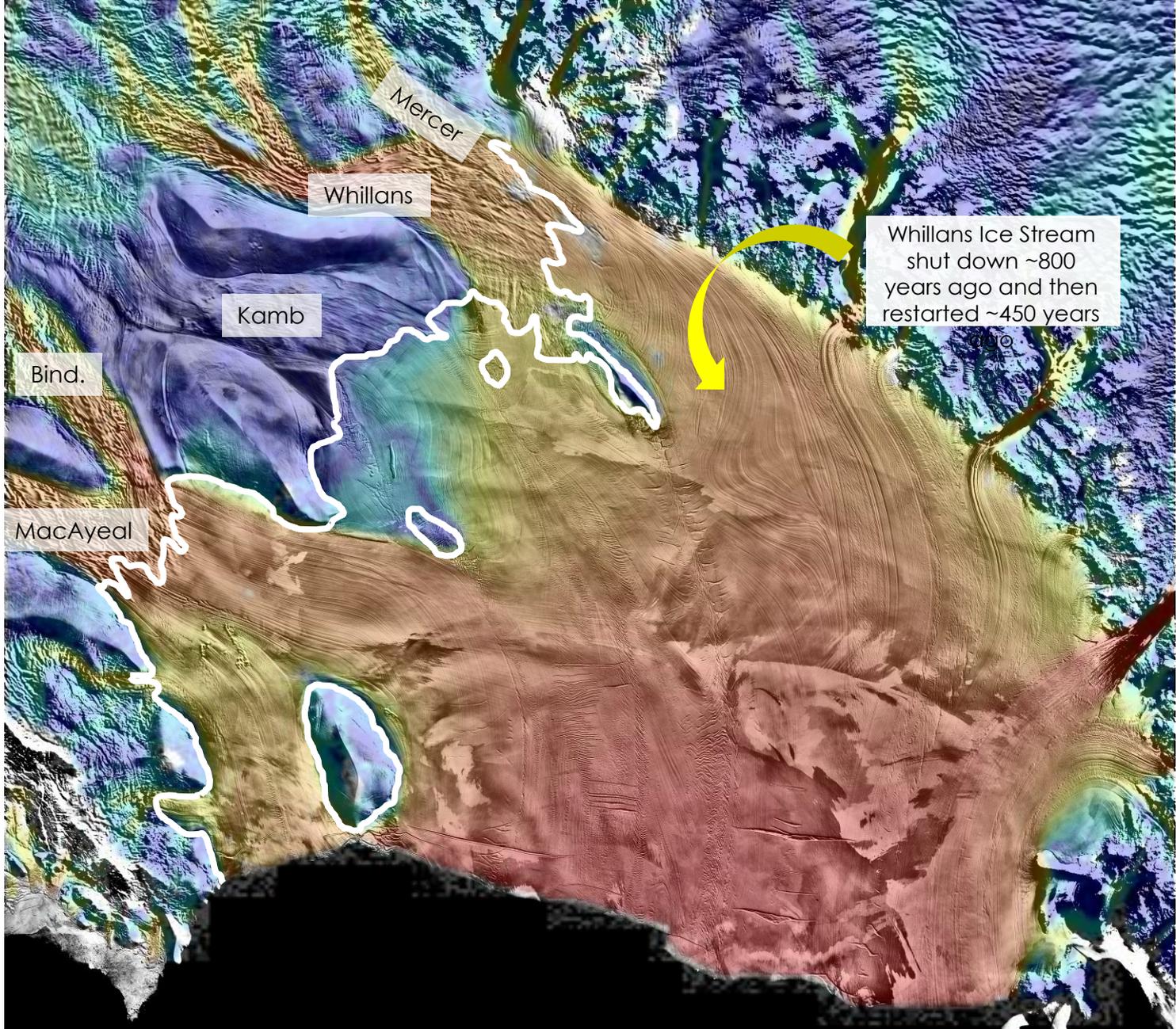
# Glacier Fundamentals: ice stream variability



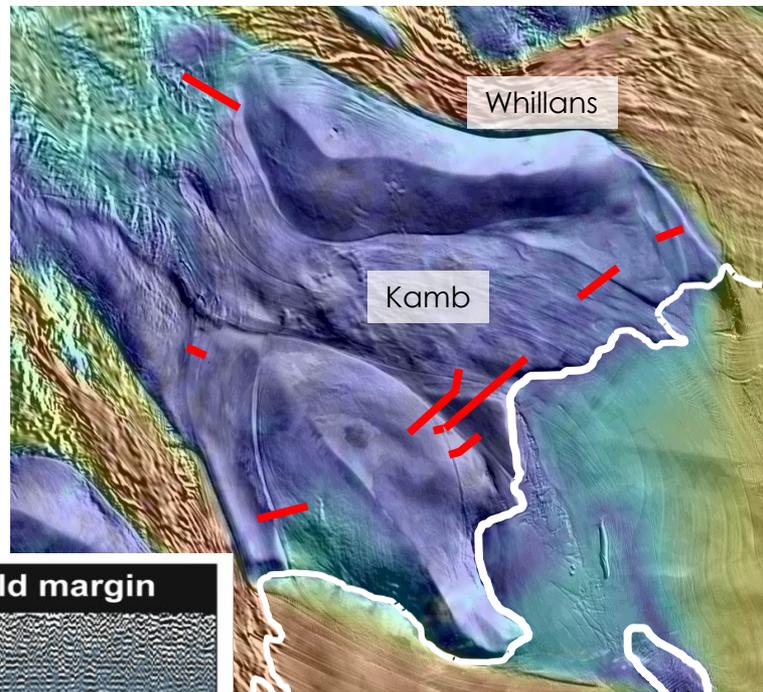
# Glacier Fundamentals: ice stream variability



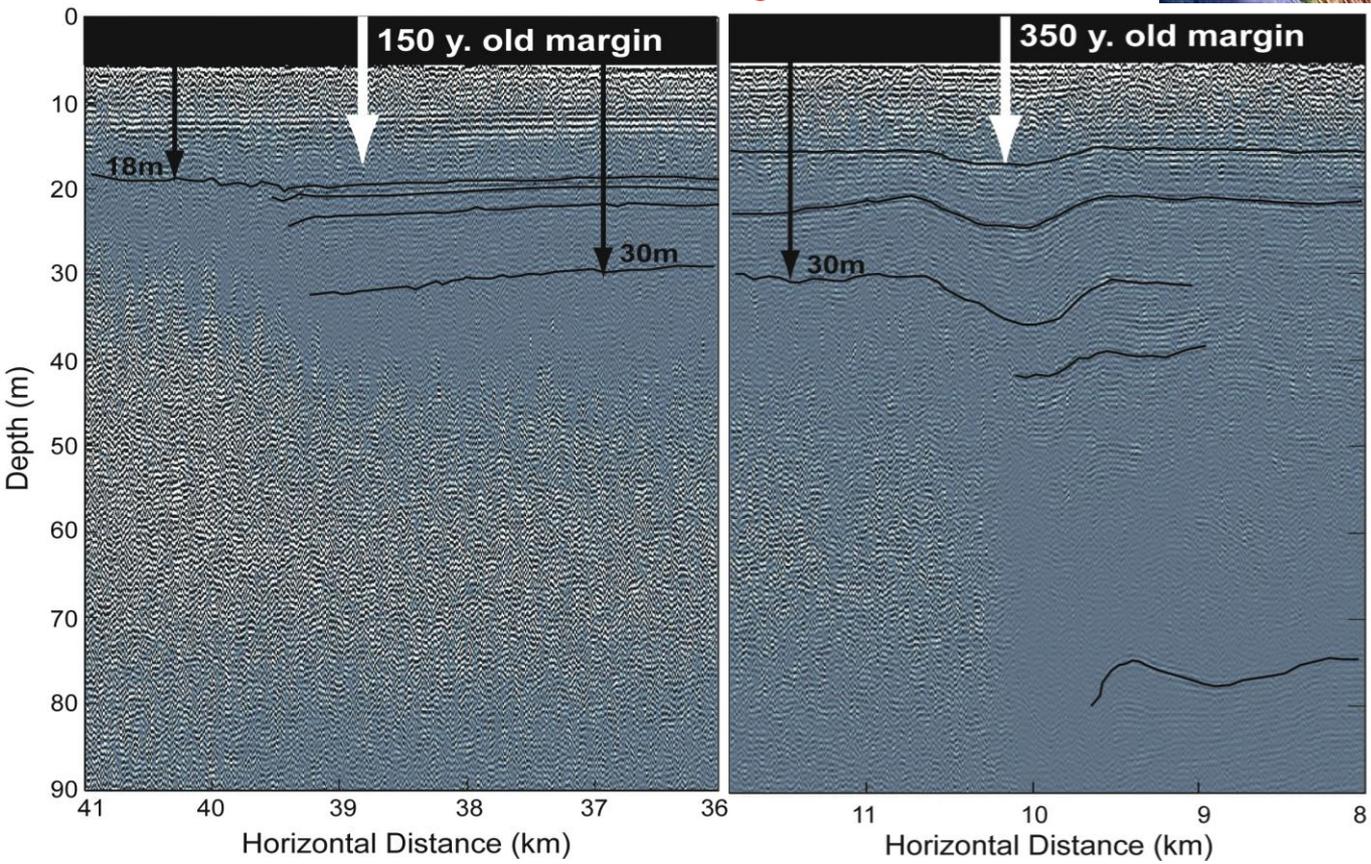
# Glacier Fundamentals: ice stream variability



# Glacier Fundamentals: ice stream variability

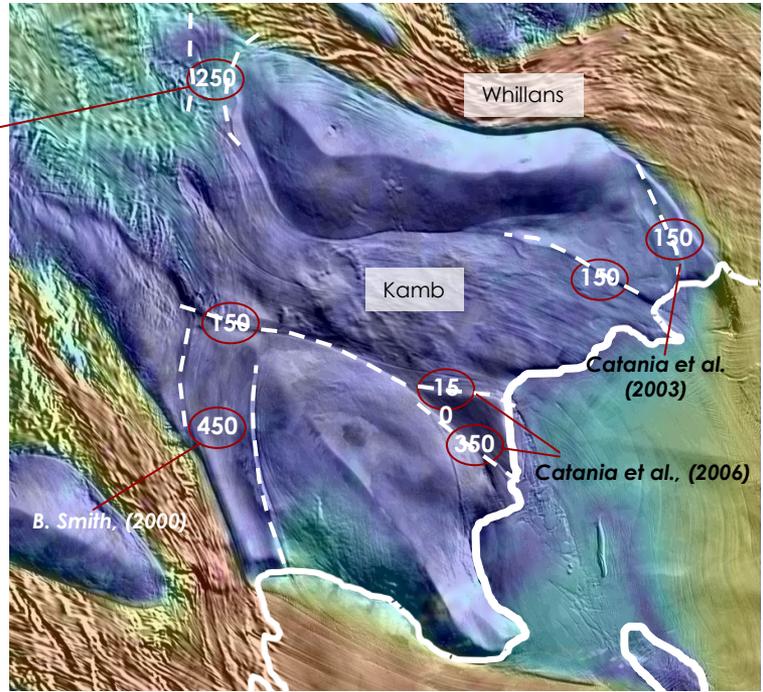


Relict Shear Margins



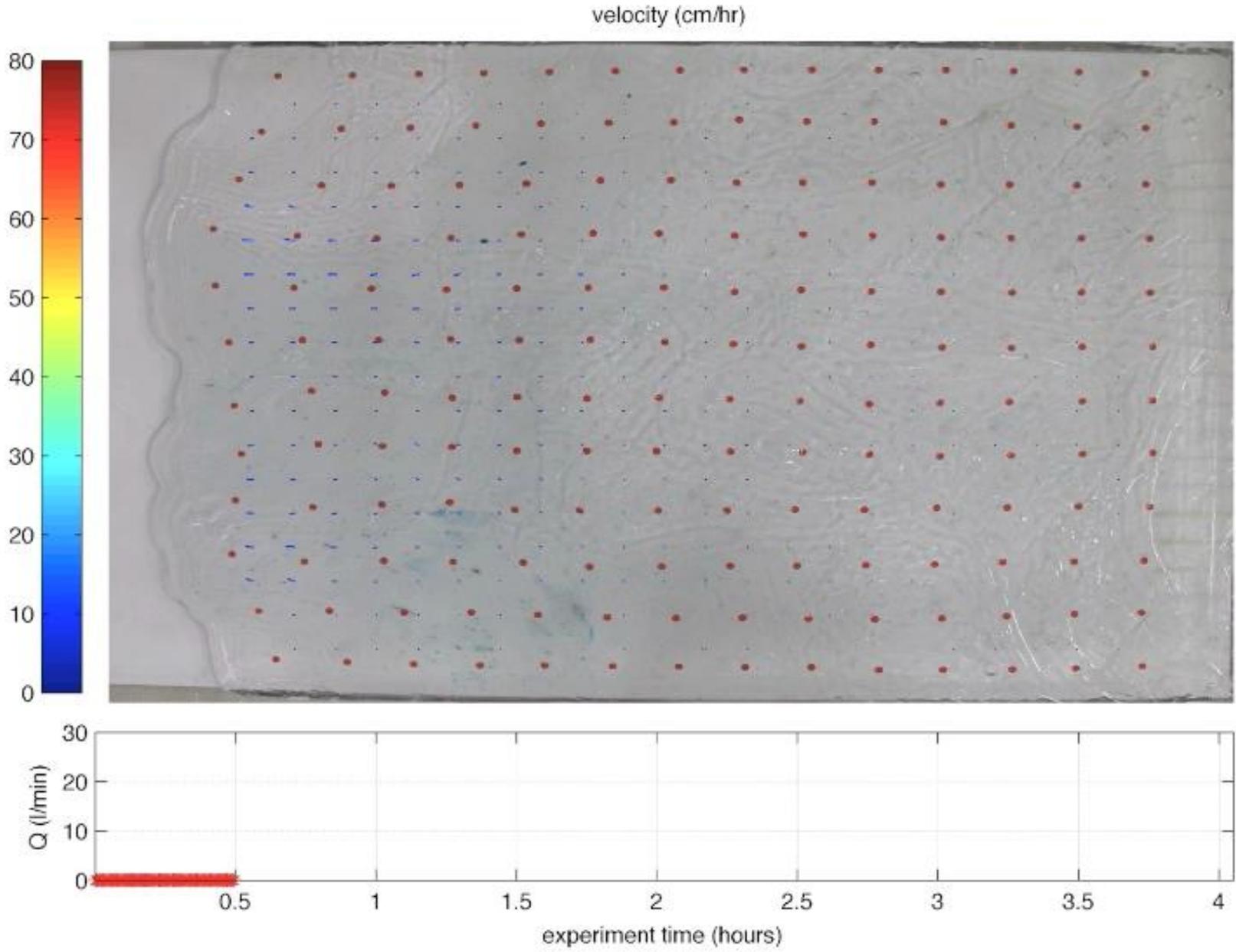
# Glacier Fundamentals: ice stream variability

Conway et al. (2002)

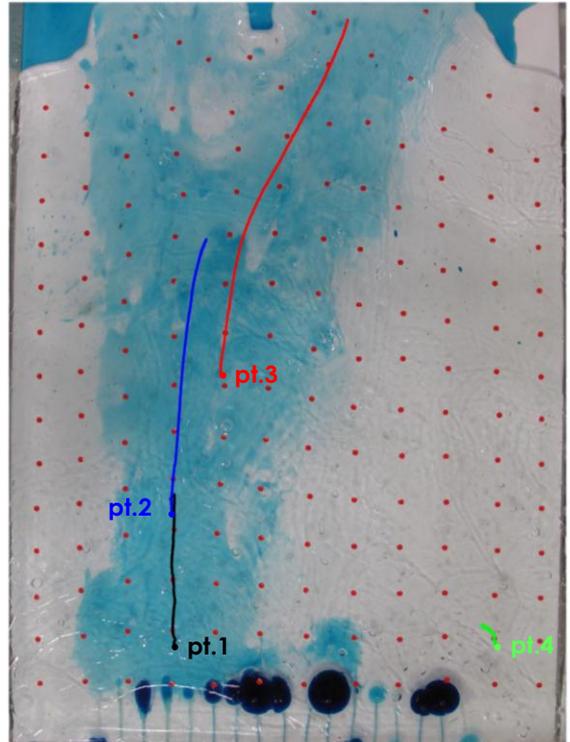
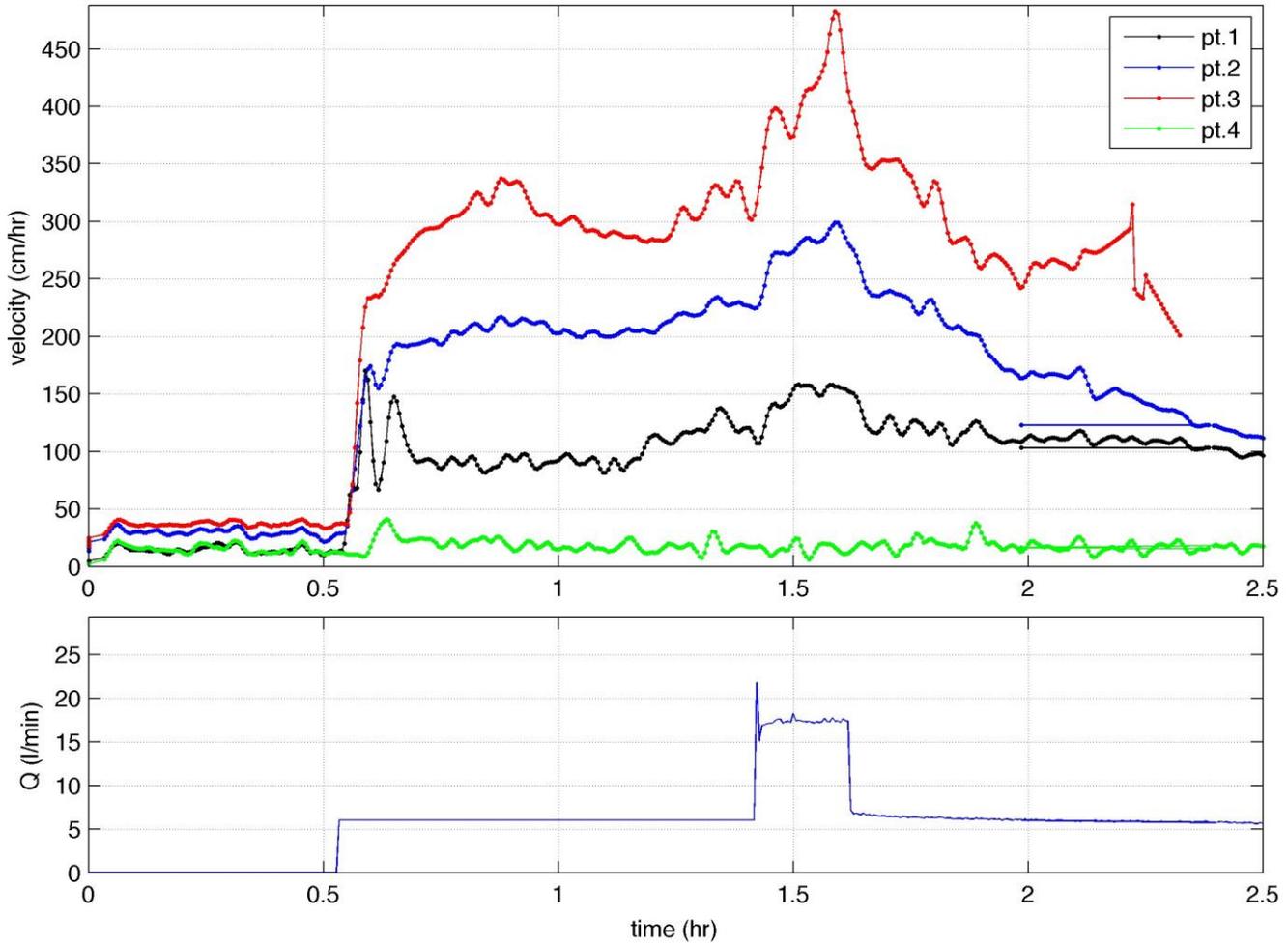


- ice stream system underwent numerous changes in configuration over time

# Physical Model: ice stream flow variability

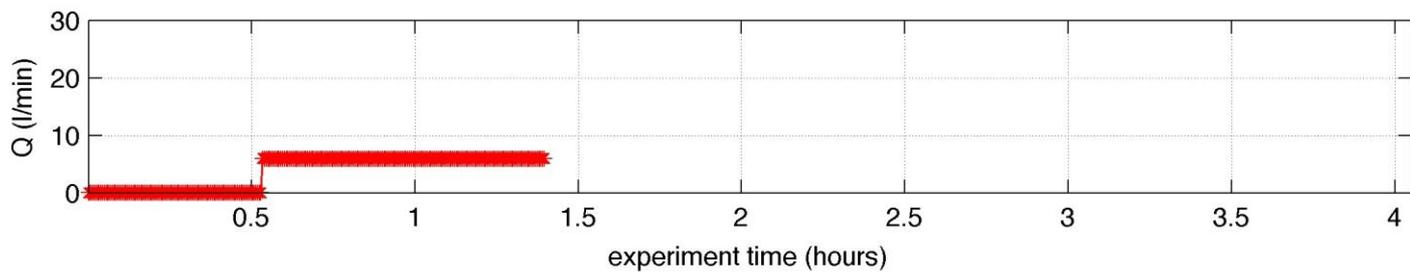
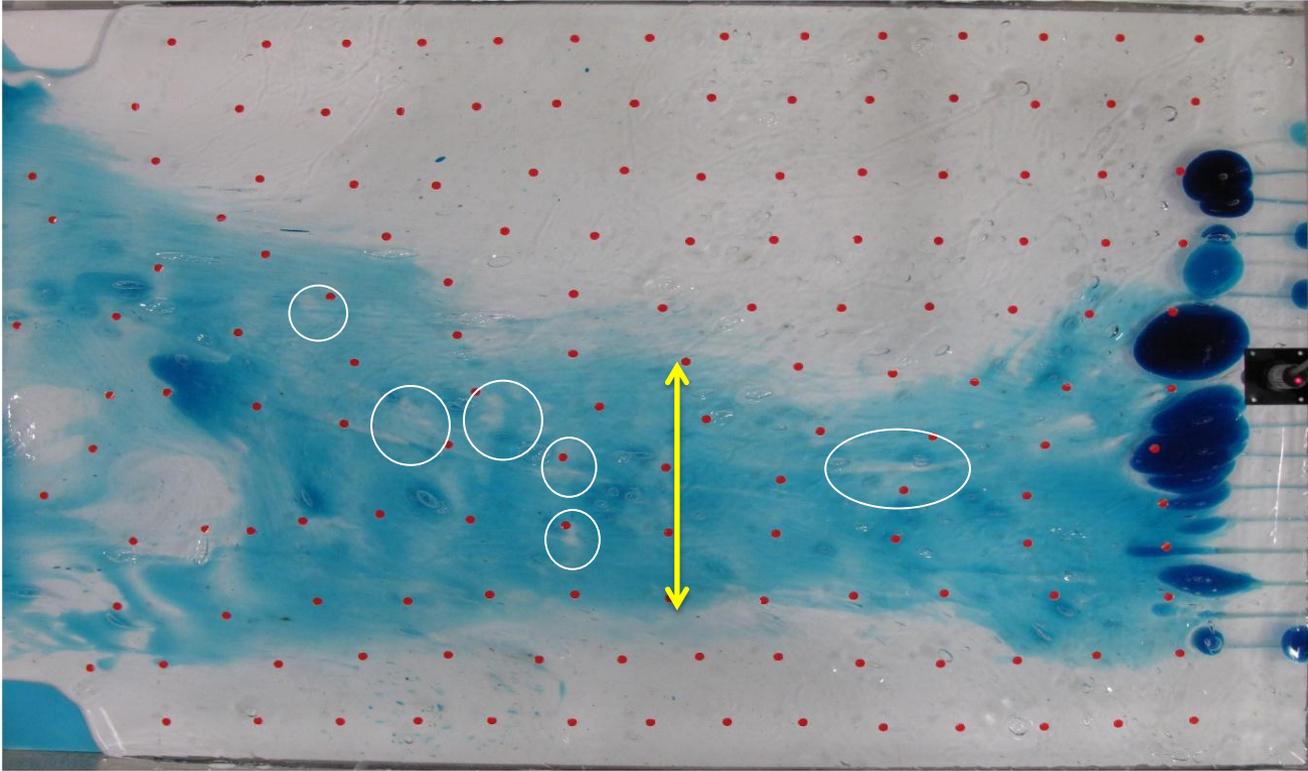


# Physical Model: ice stream flow variability



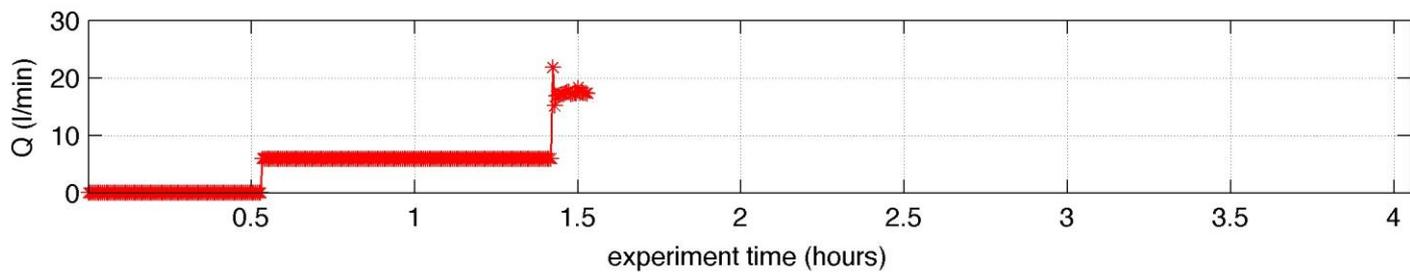
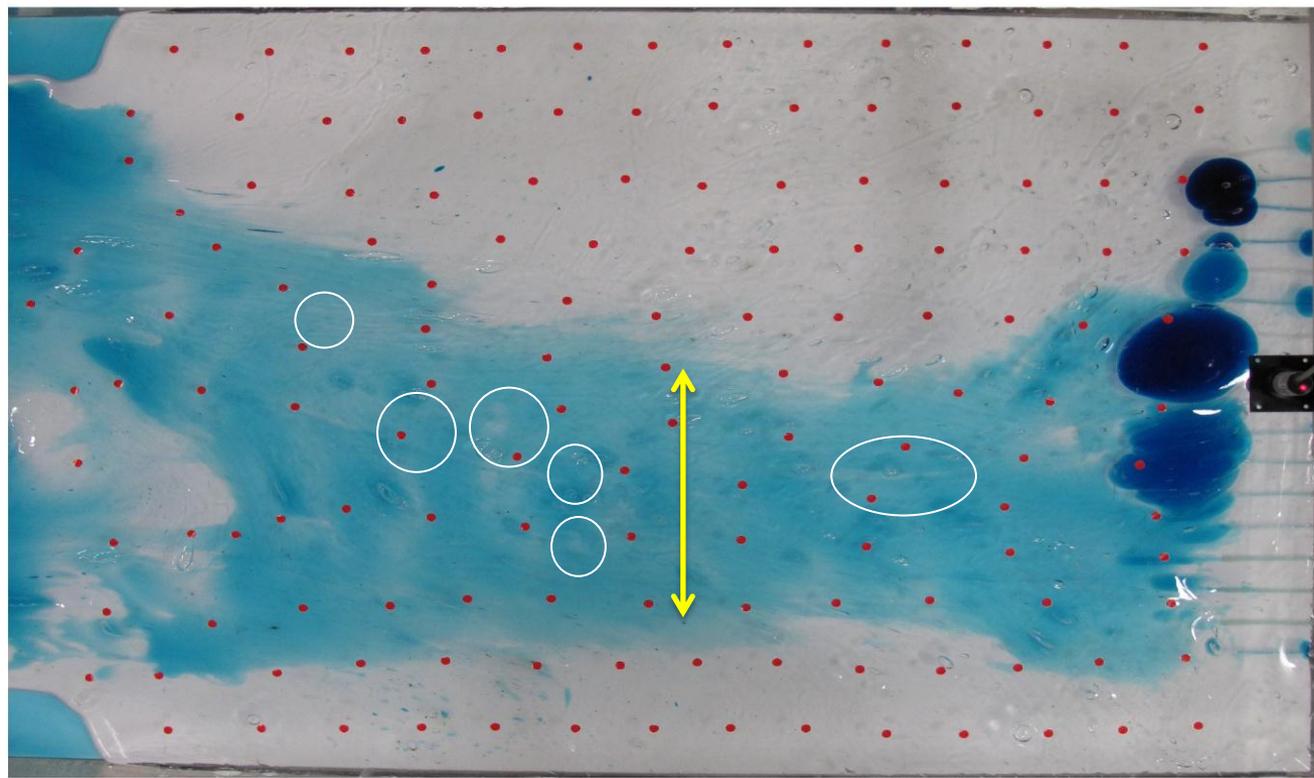
# Physical Model: ice stream flow variability

- lighter-coloured areas have a thinner (or absent) water layer due to variations in polymer thickness
- thinner water layer may increase drag of the polymer locally

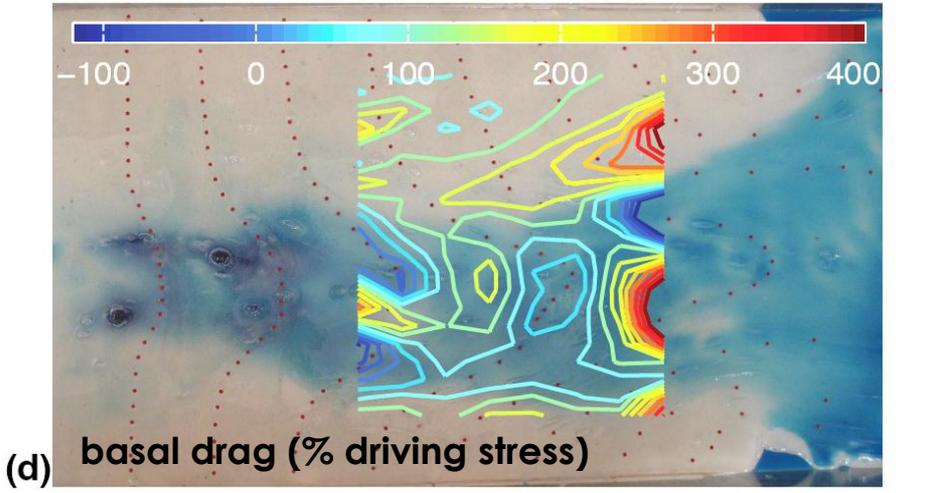
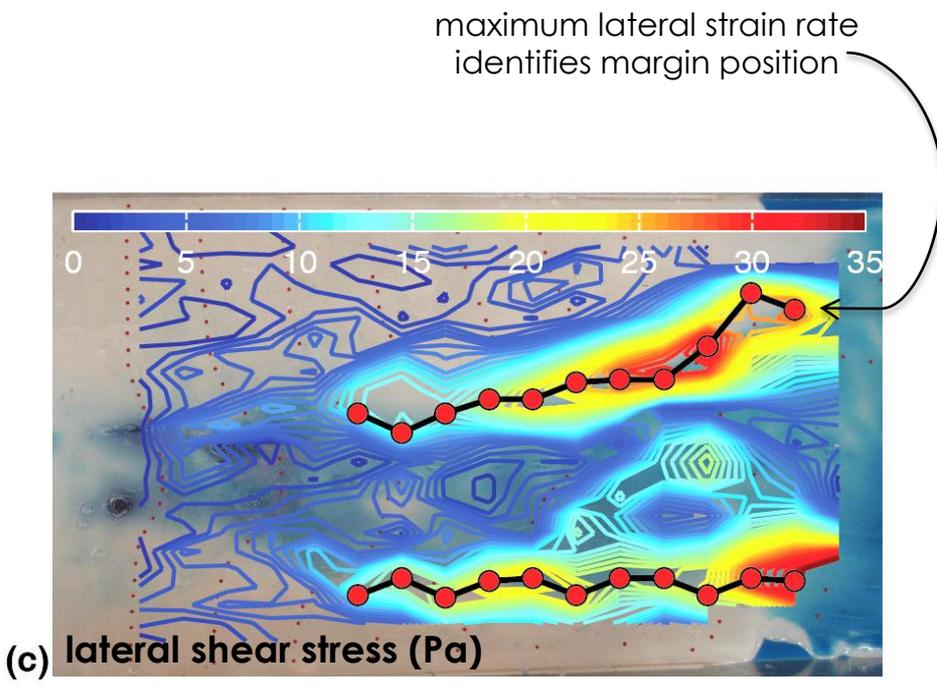
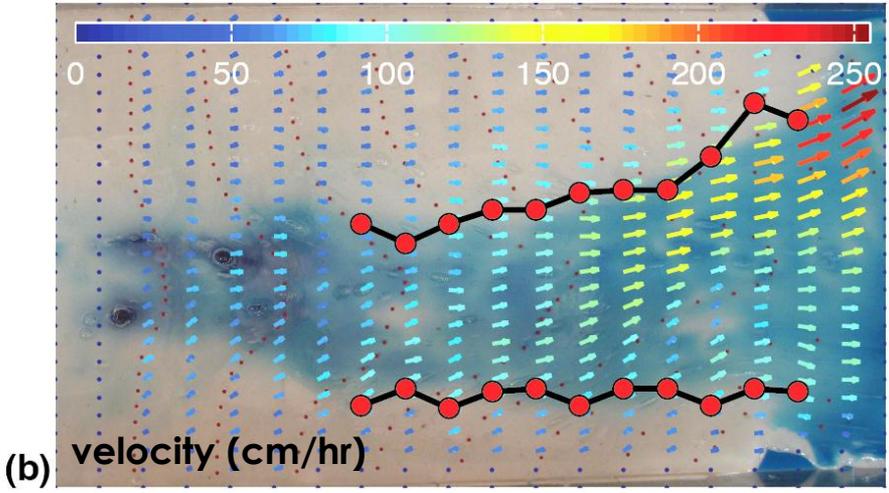
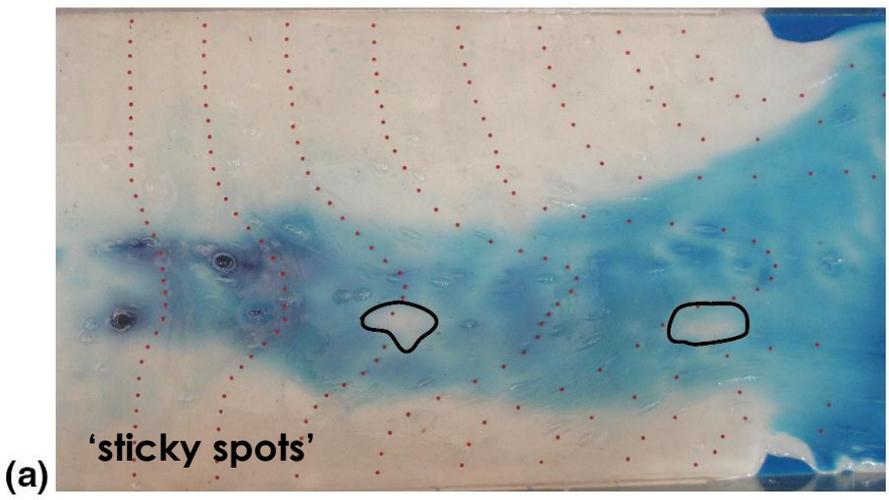


# Physical Model: ice stream flow variability

- increases in water discharge cause uplift that “drowns out” regions where polymer was dragging on bed
- increased water discharge causes greater wetted area (reduces lateral drag)

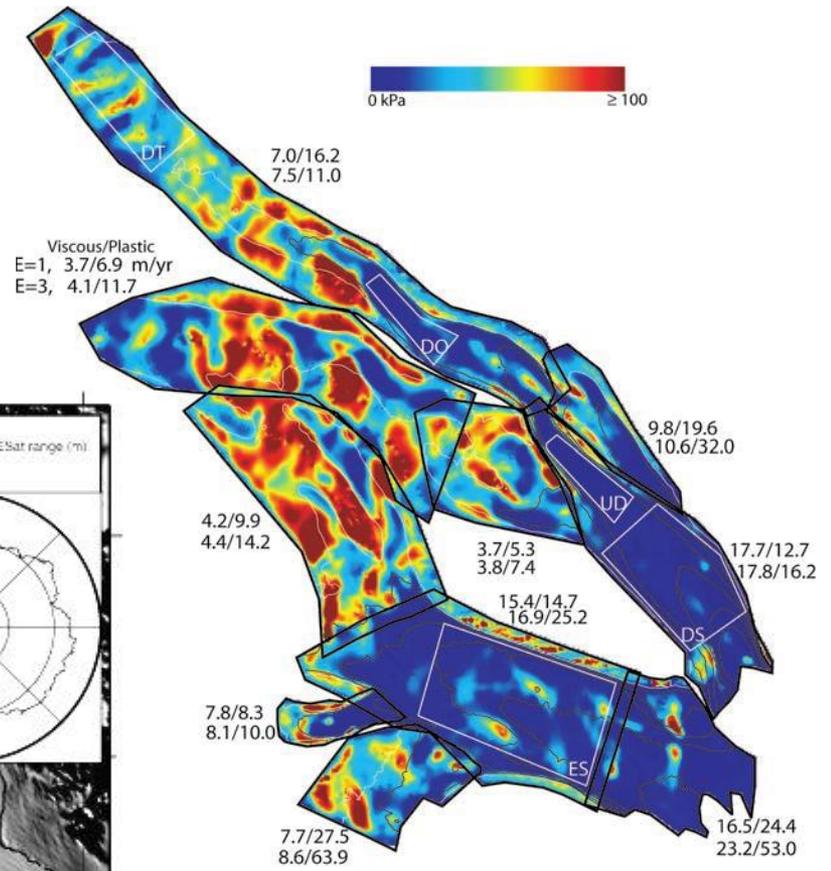
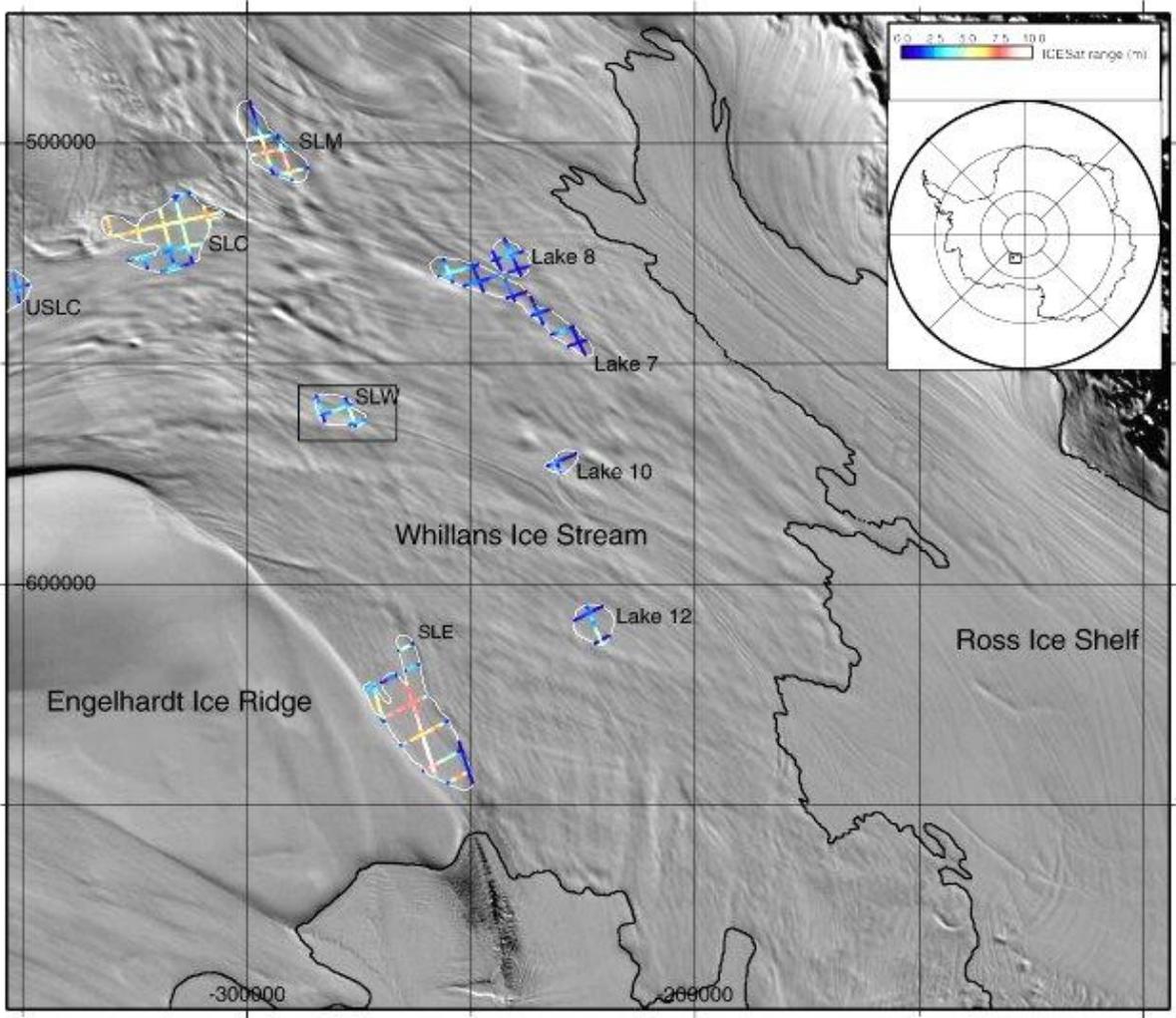


# Physical Model: ice stream flow variability

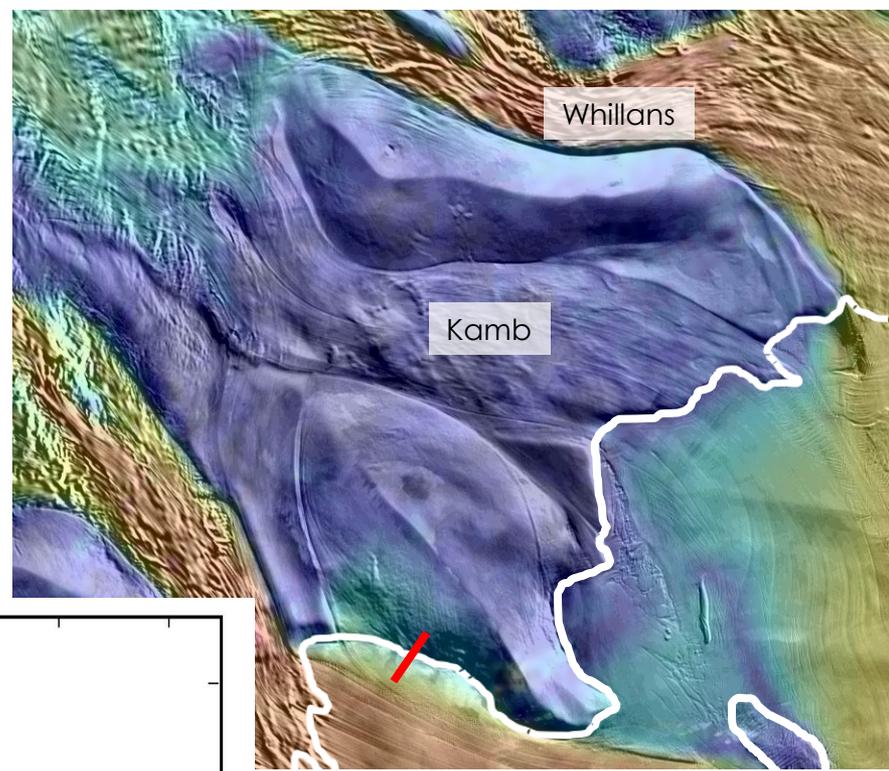


# Antarctica: Ice Stream Variability

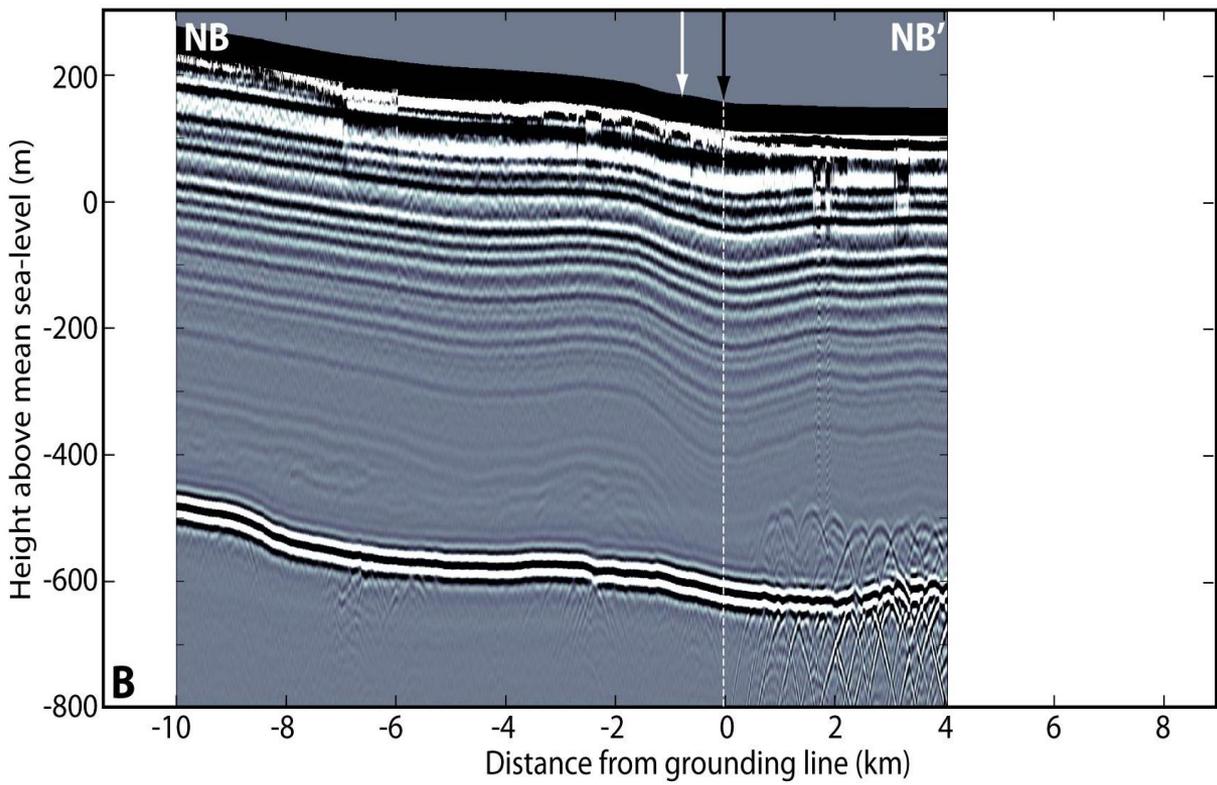
- suggest that some shifts in margin position might result from long-lived sticky spots
- conversely, persistent stationary margins might result from subglacial lakes in close proximity



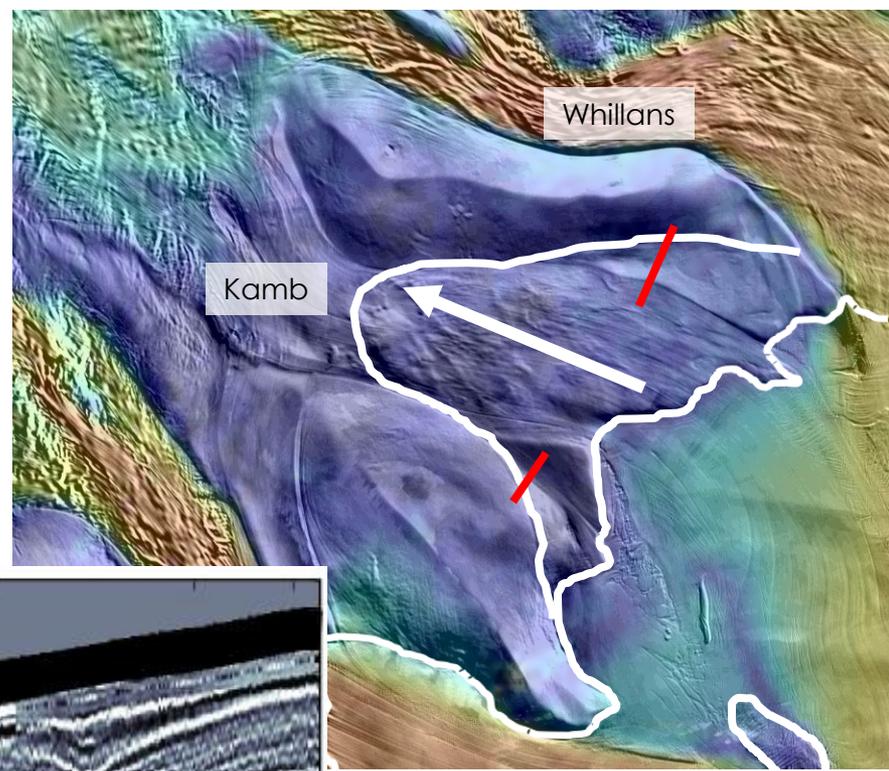
# Glacier Fundamentals: grounding lines



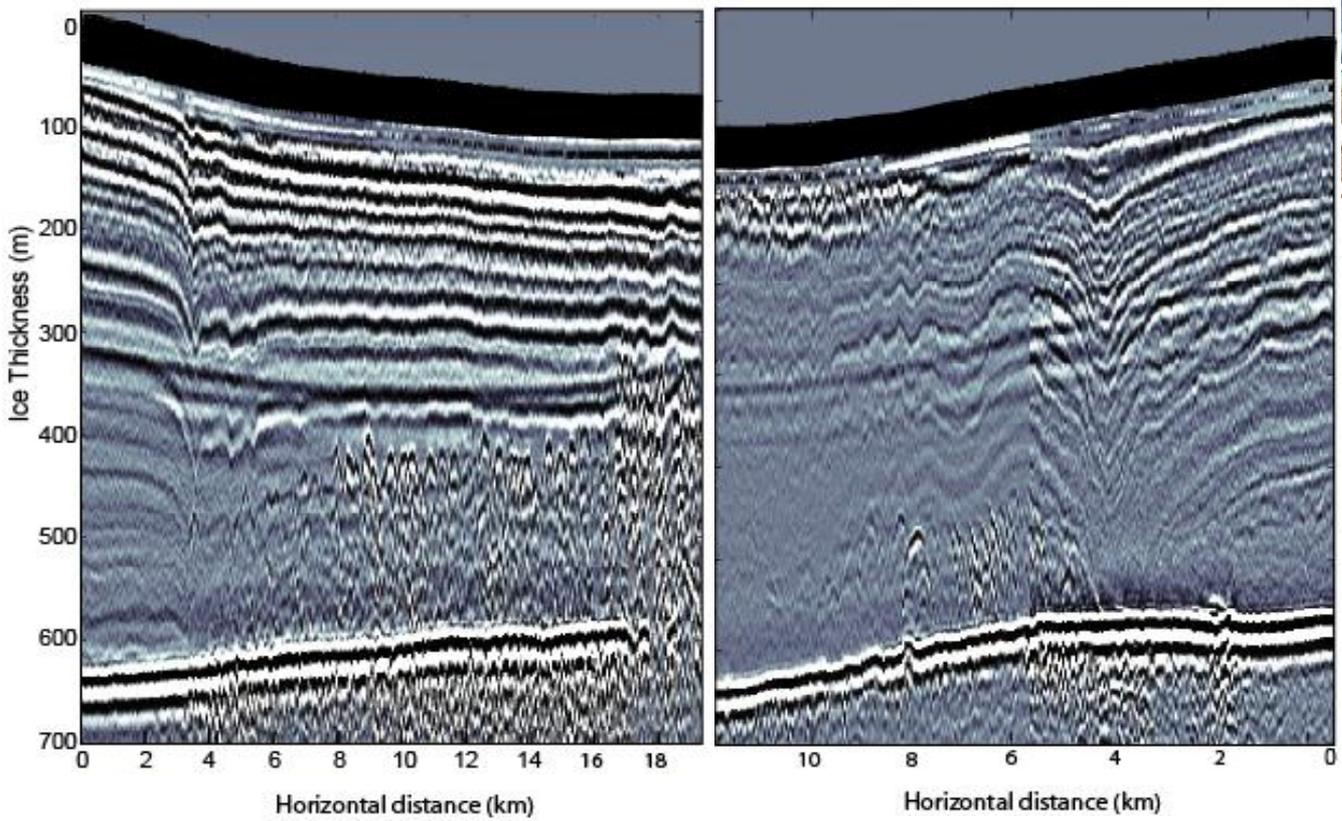
Modern Grounding Line



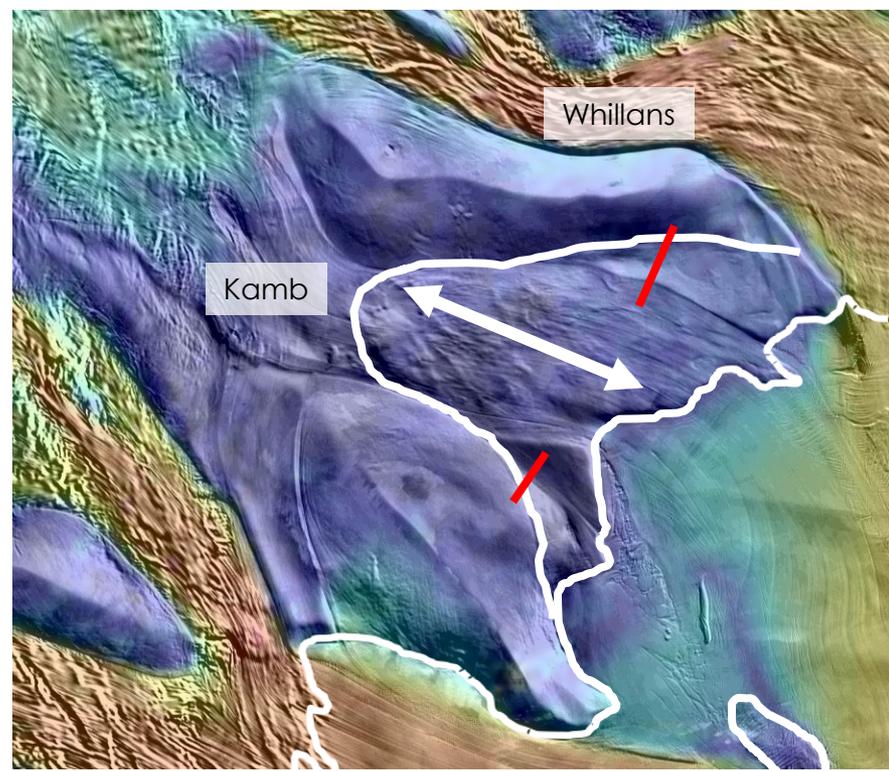
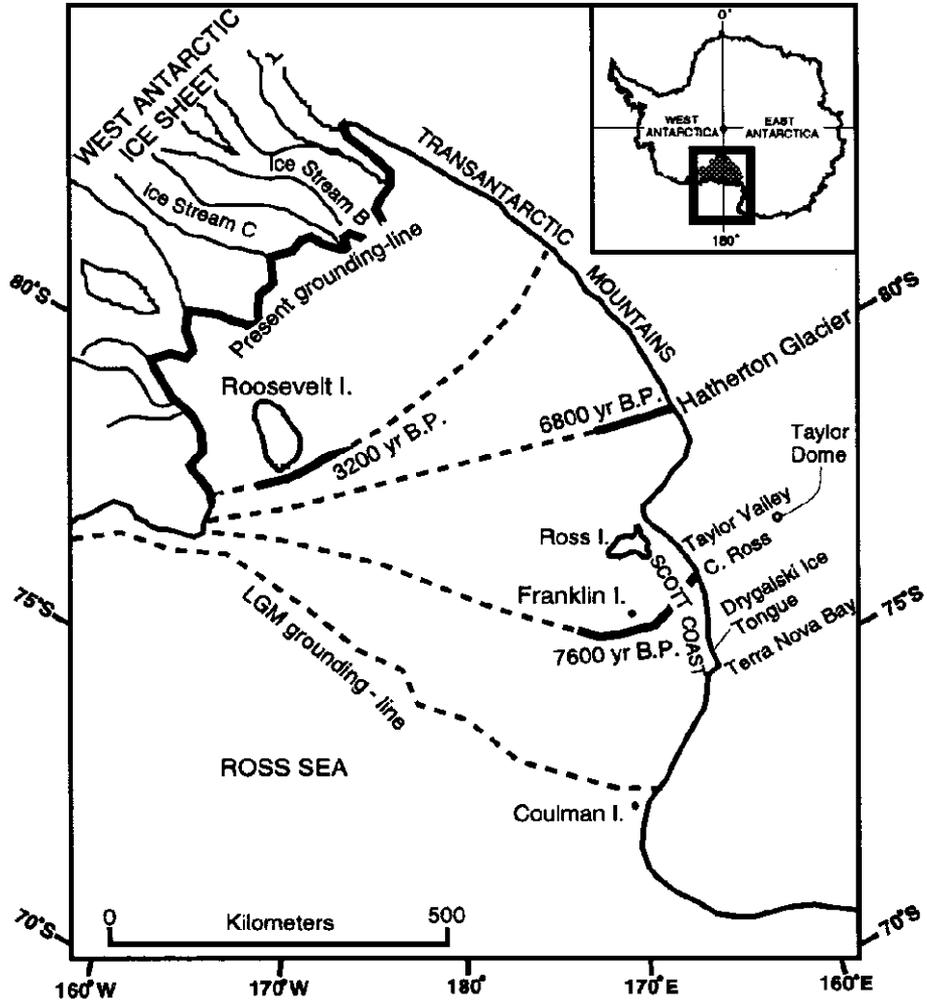
# Glacier Fundamentals: grounding lines



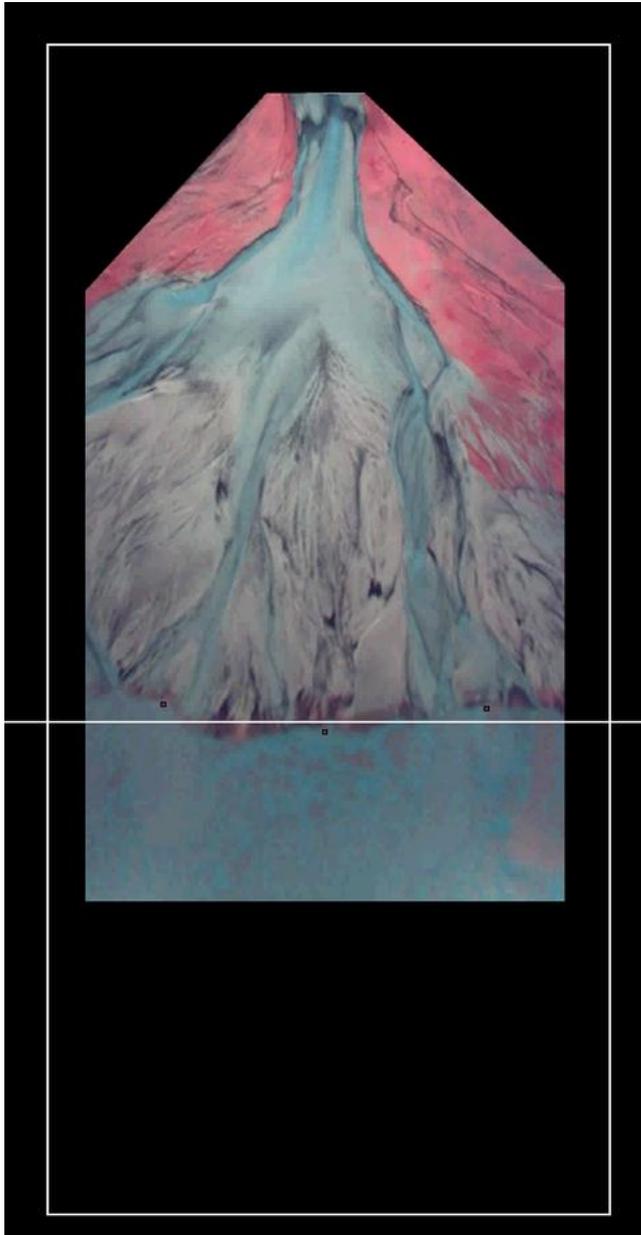
Relict Grounding Line



# Glacier Fundamentals: grounding lines

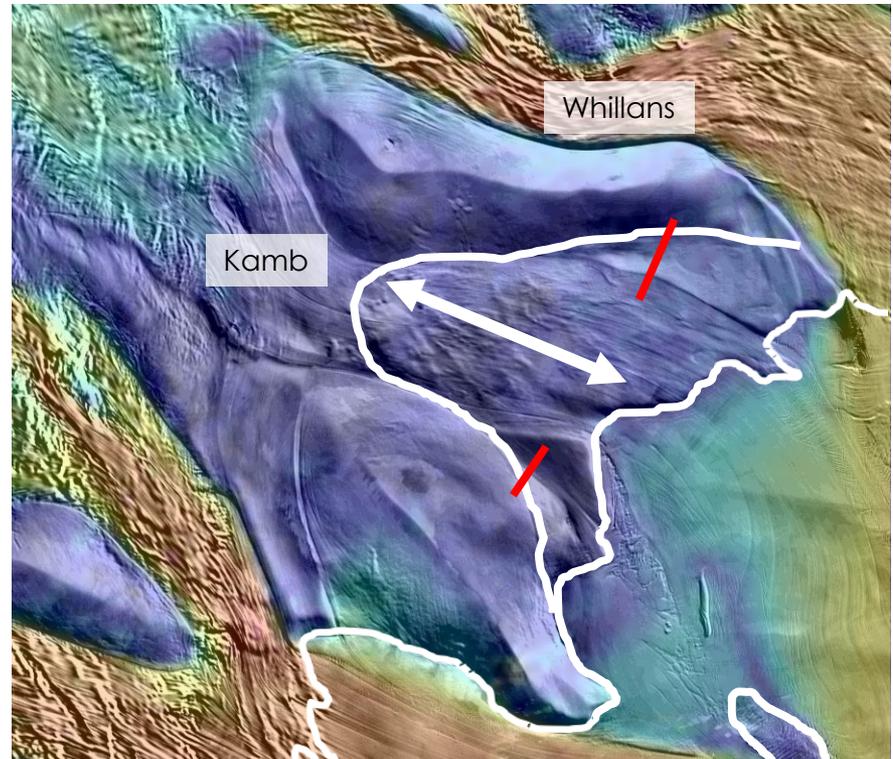


# Physical Model: grounding lines

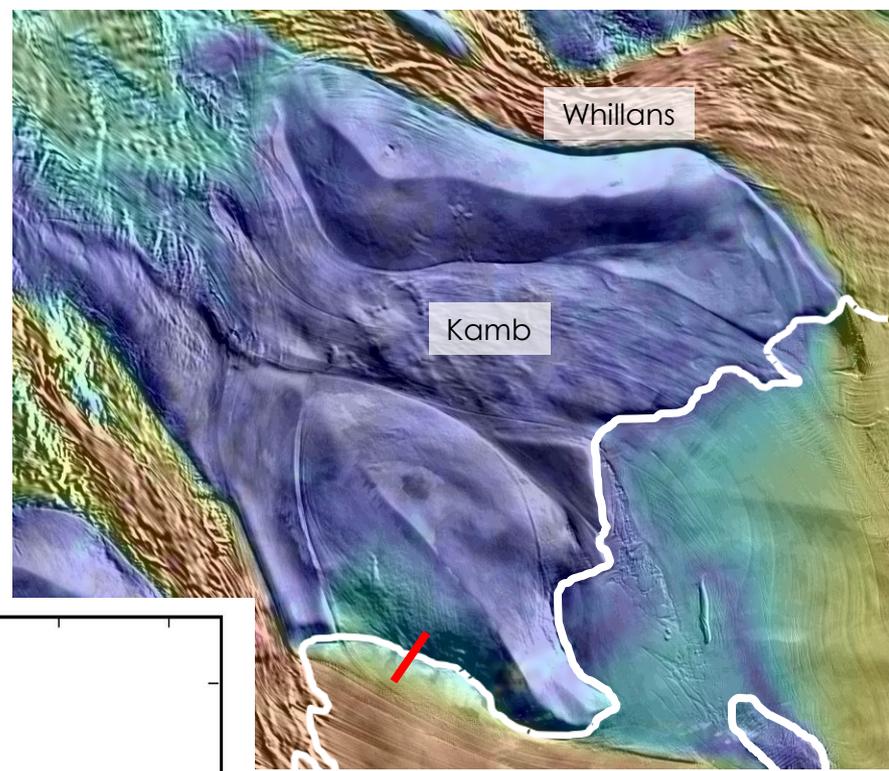


## Variability in Grounding Line

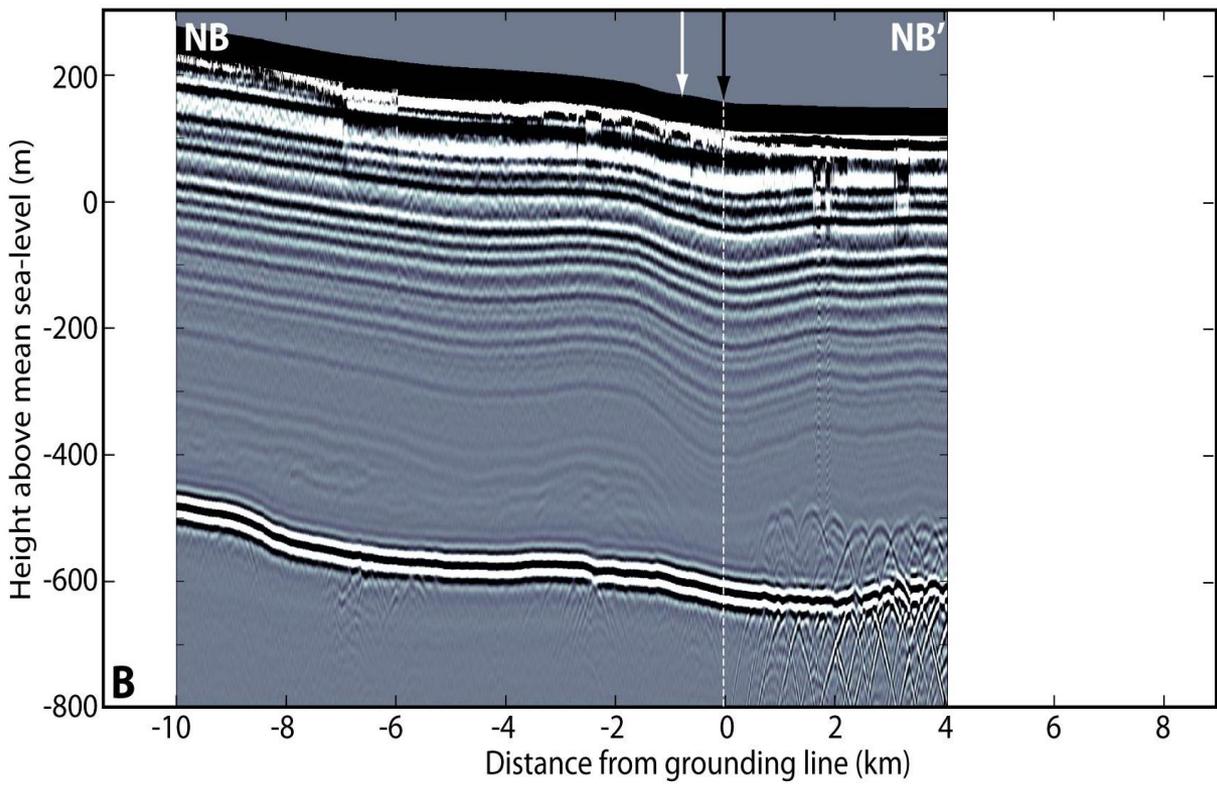
- look to other disciplines where internal variability occurs over **much faster time scales**
- sea-level changes work for/against ice thickness changes and can amplify/diminish changes in the grounding line
- more variability in the grounding line might be expected during periods of sea-level rise



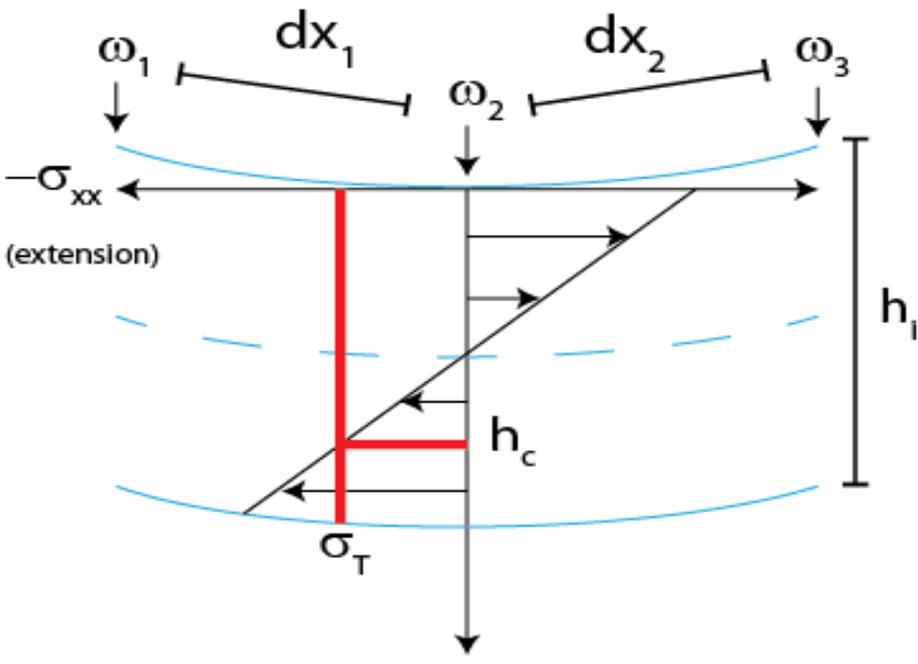
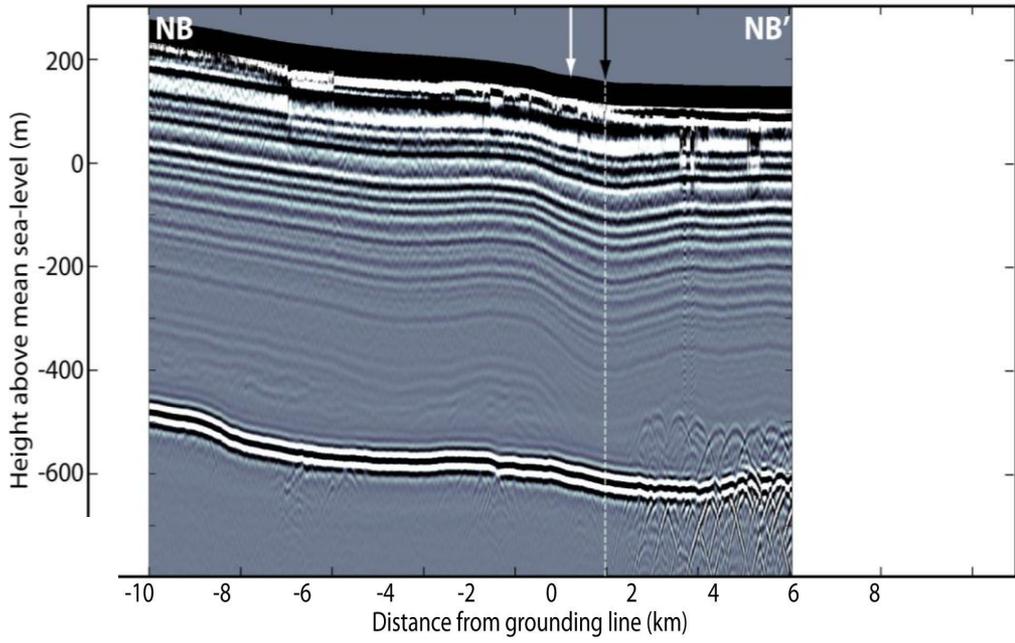
# Glacier Fundamentals: grounding lines



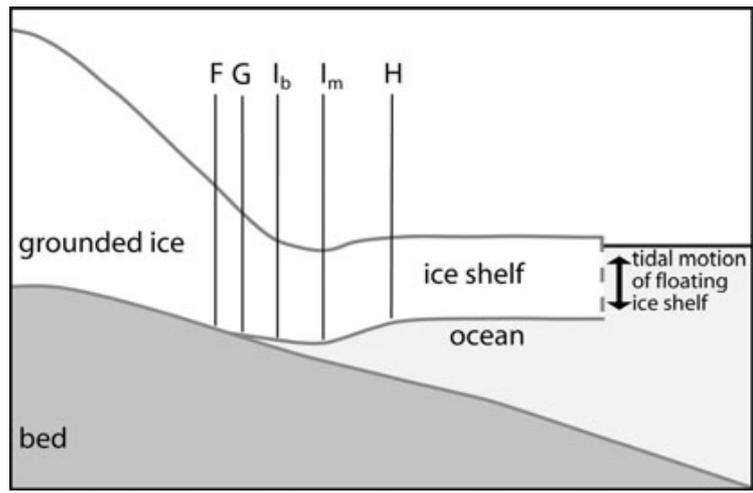
Modern Grounding Line



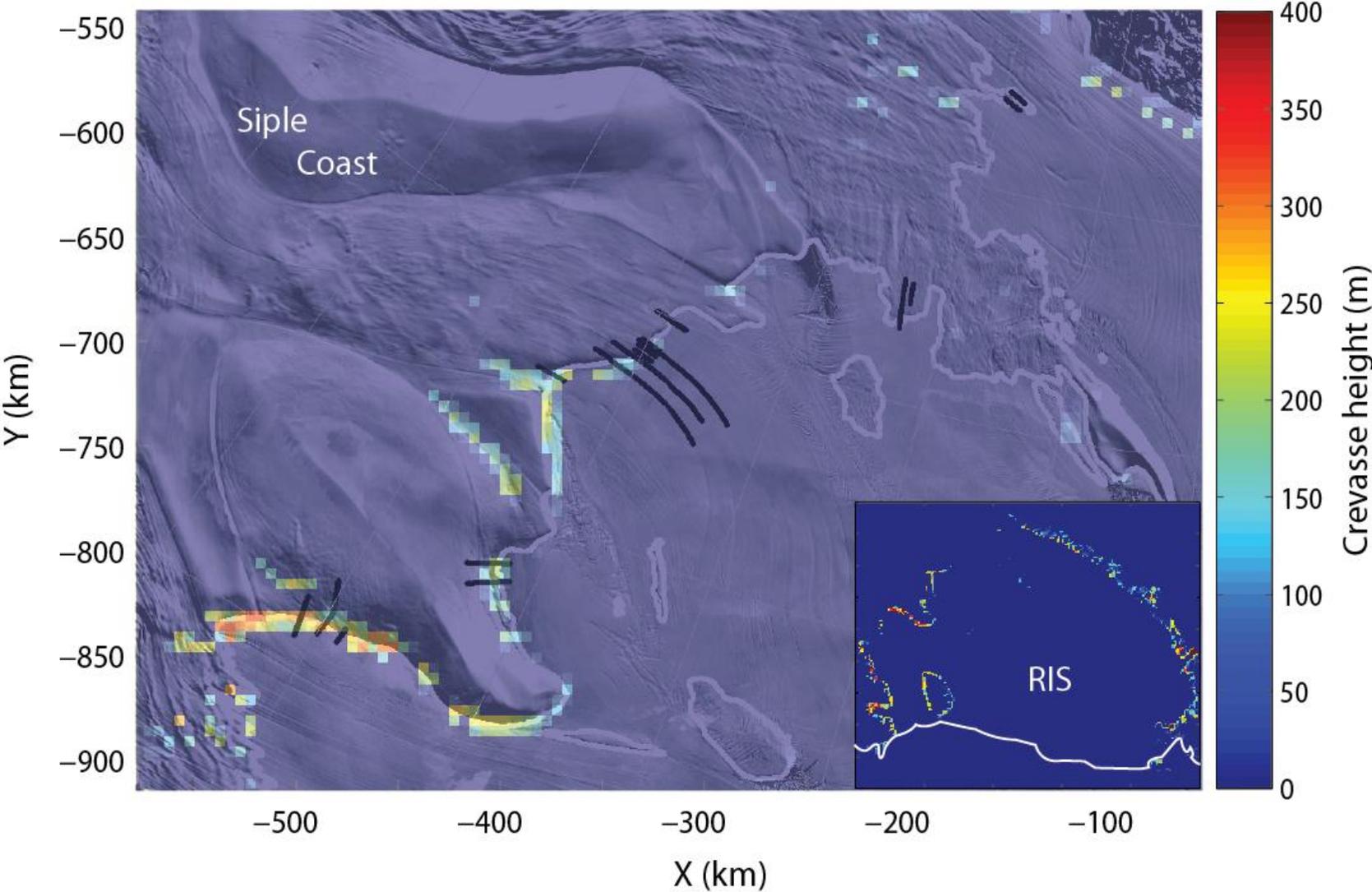
# Glacier Fundamentals: grounding lines



$$\omega''(x) = \frac{\omega_1 - 2\omega_2 + \omega_3}{dx_1 dx_2}$$

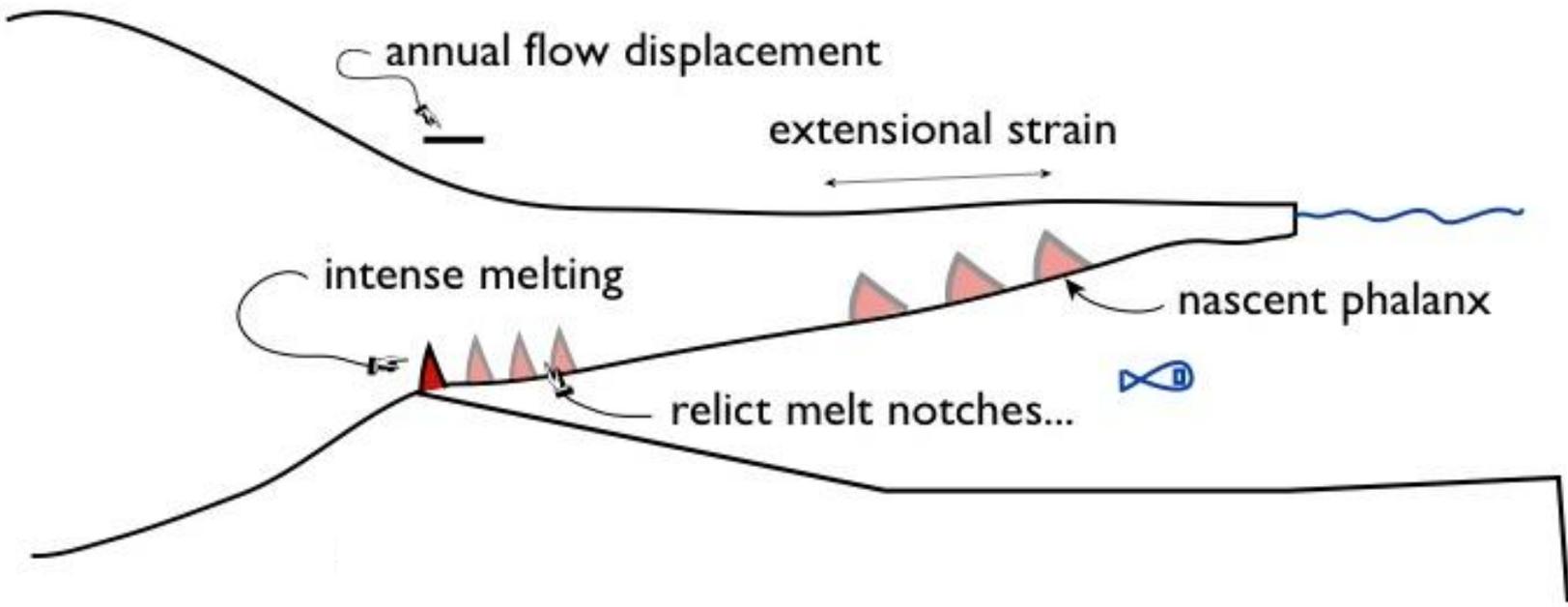


# Glacier Fundamentals: grounding lines

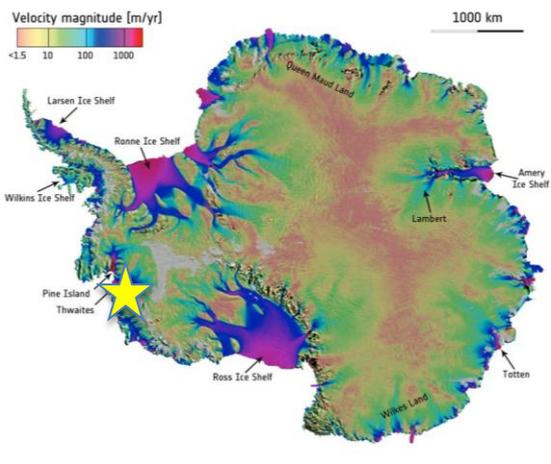


# Glacier Fundamentals: iceberg calving

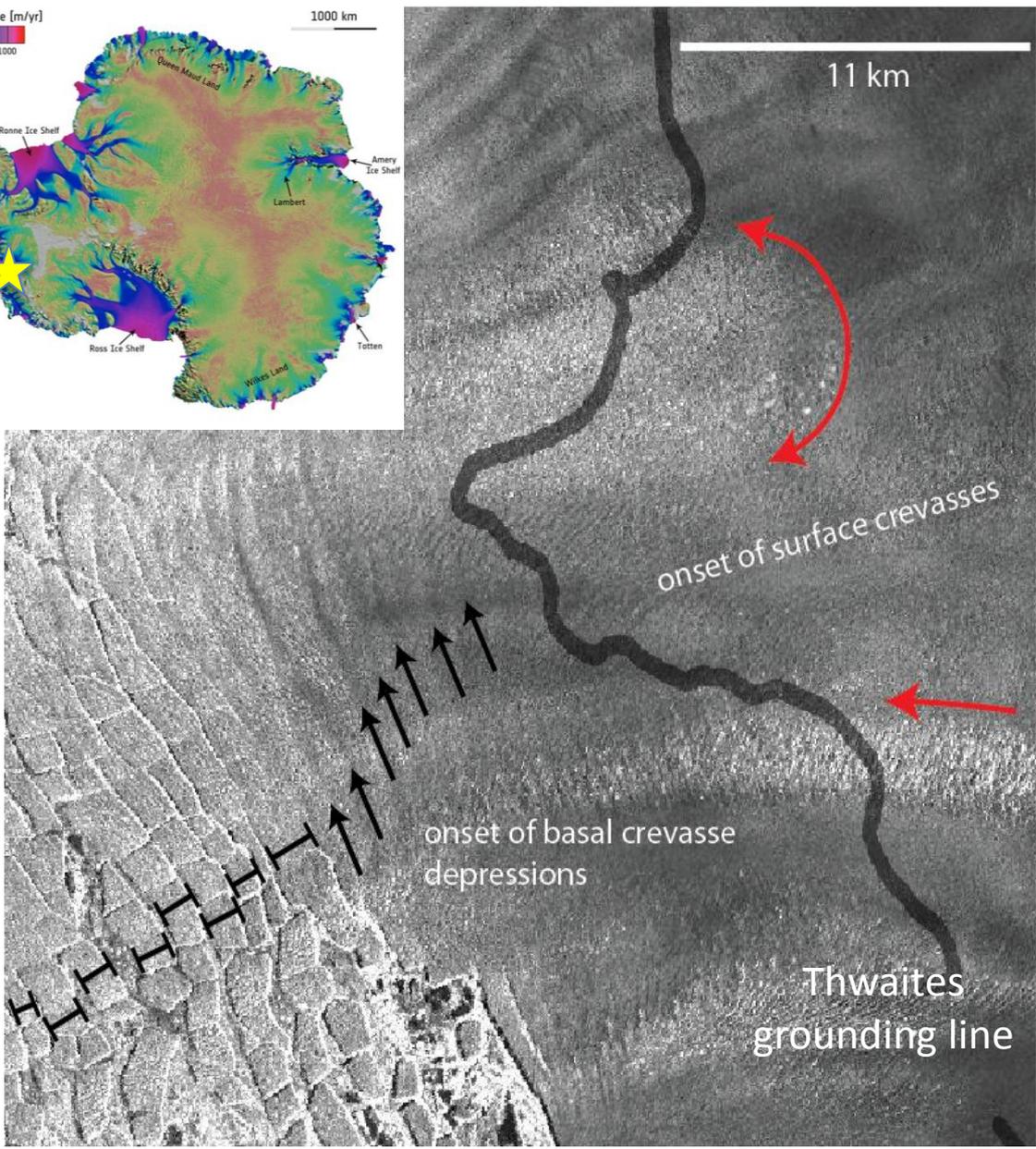
- How to “imprint” a fracture spacing that can allow iceberg capsizes:



# Glacier Fundamentals: iceberg calving

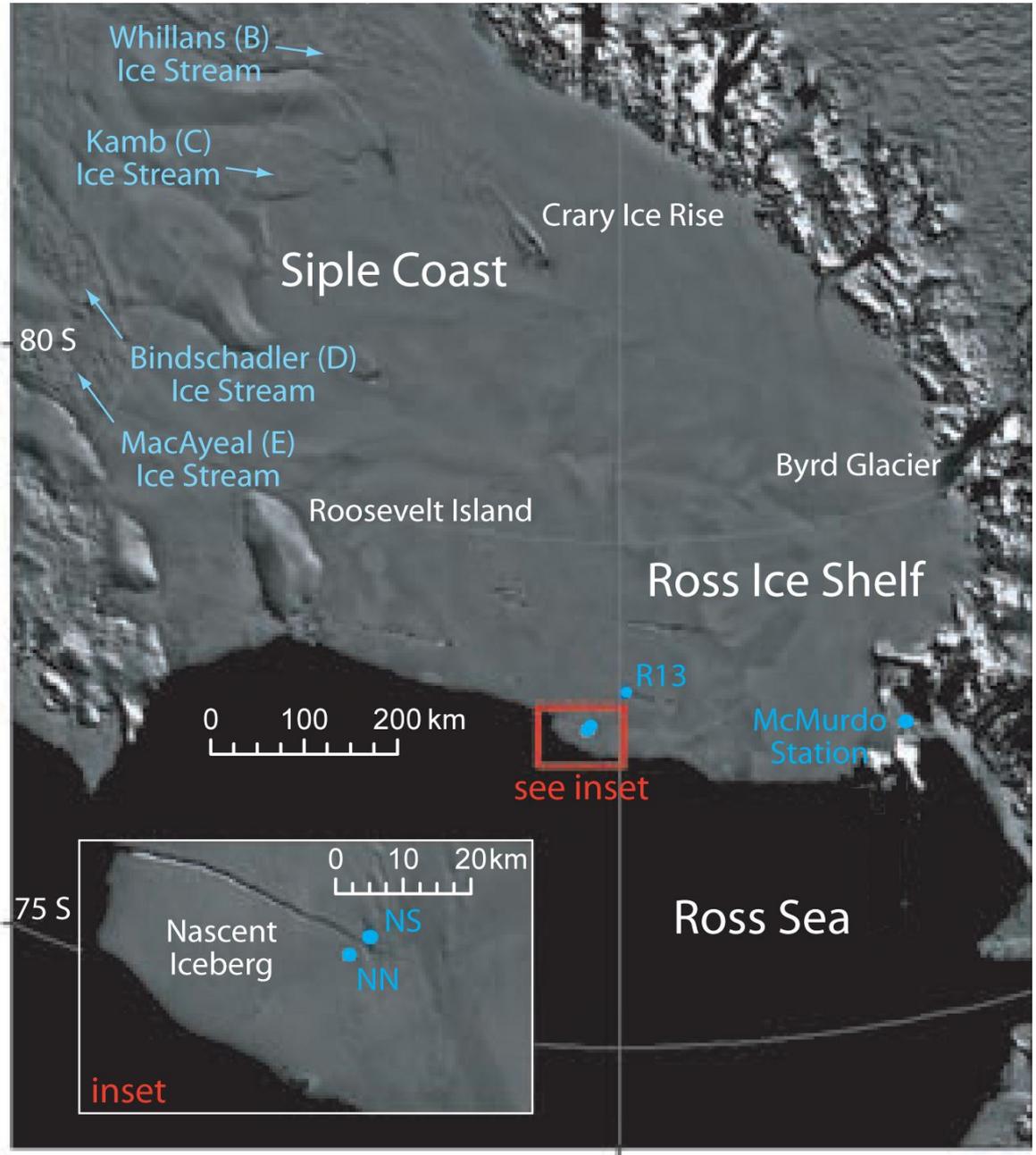


- explains uniformity of iceberg size at the calving front



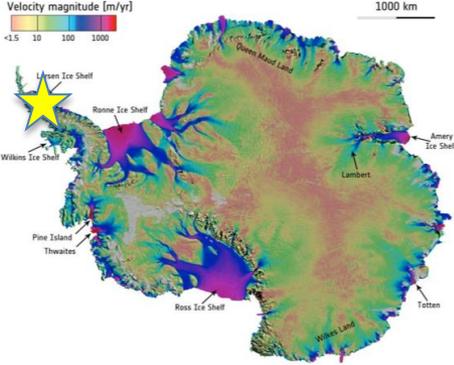
# Glacier Fundamentals: iceberg calving

- explains stability of fast-moving ice shelves that periodically produce large tabular icebergs

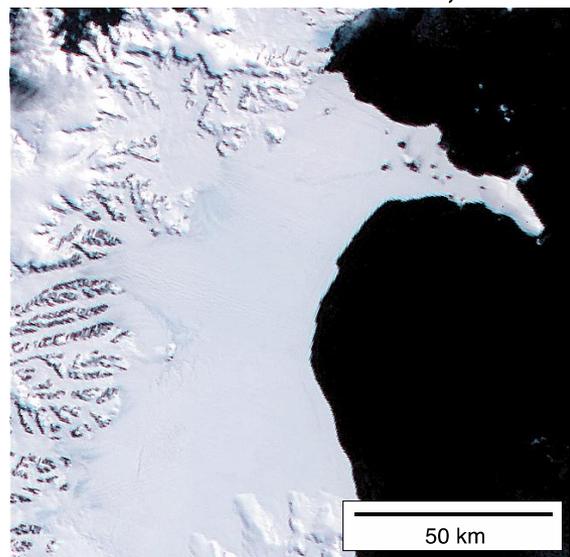


# Glacier Fundamentals: iceberg calving

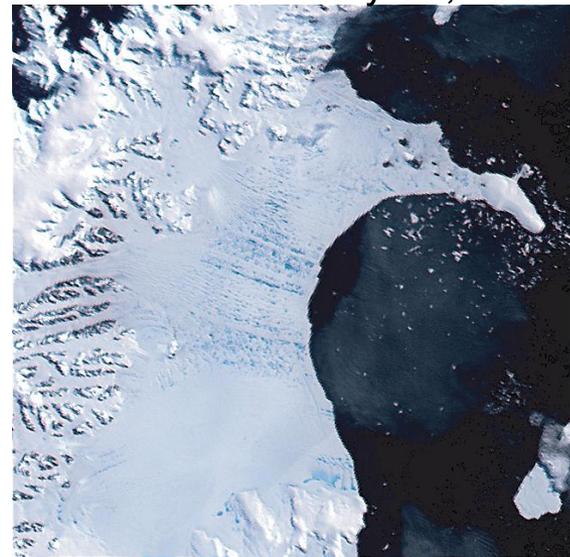
## collapse of Larsen B late summer 2002



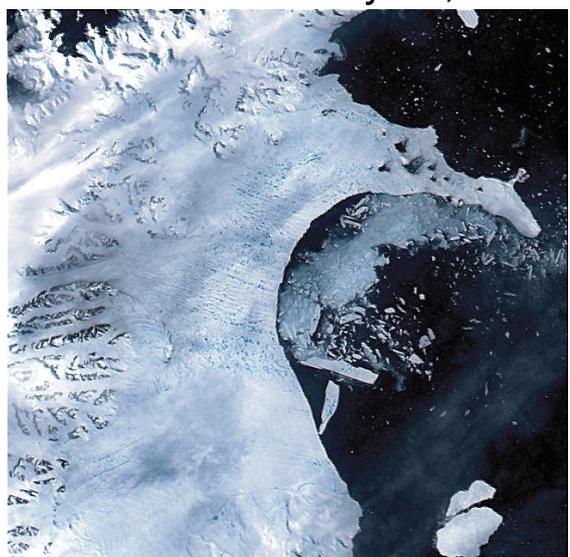
November 22, 2001



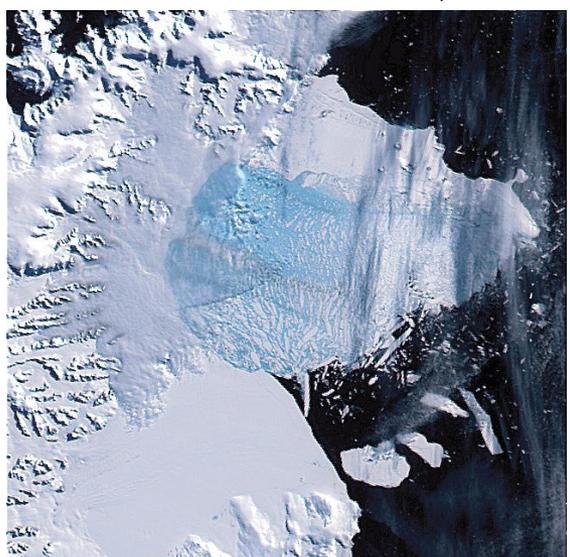
January 31, 2002



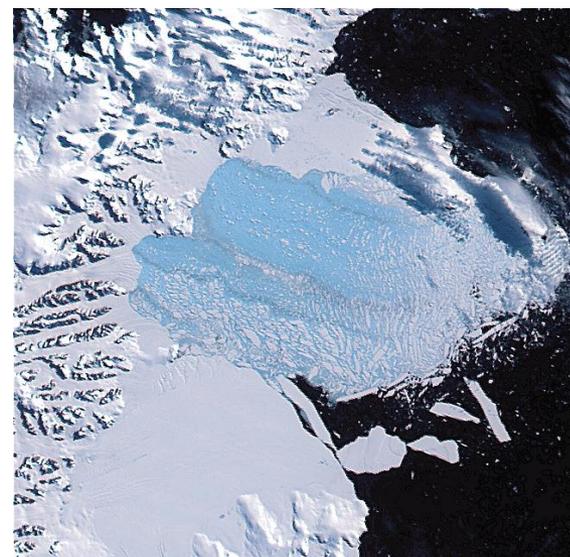
February 17, 2002



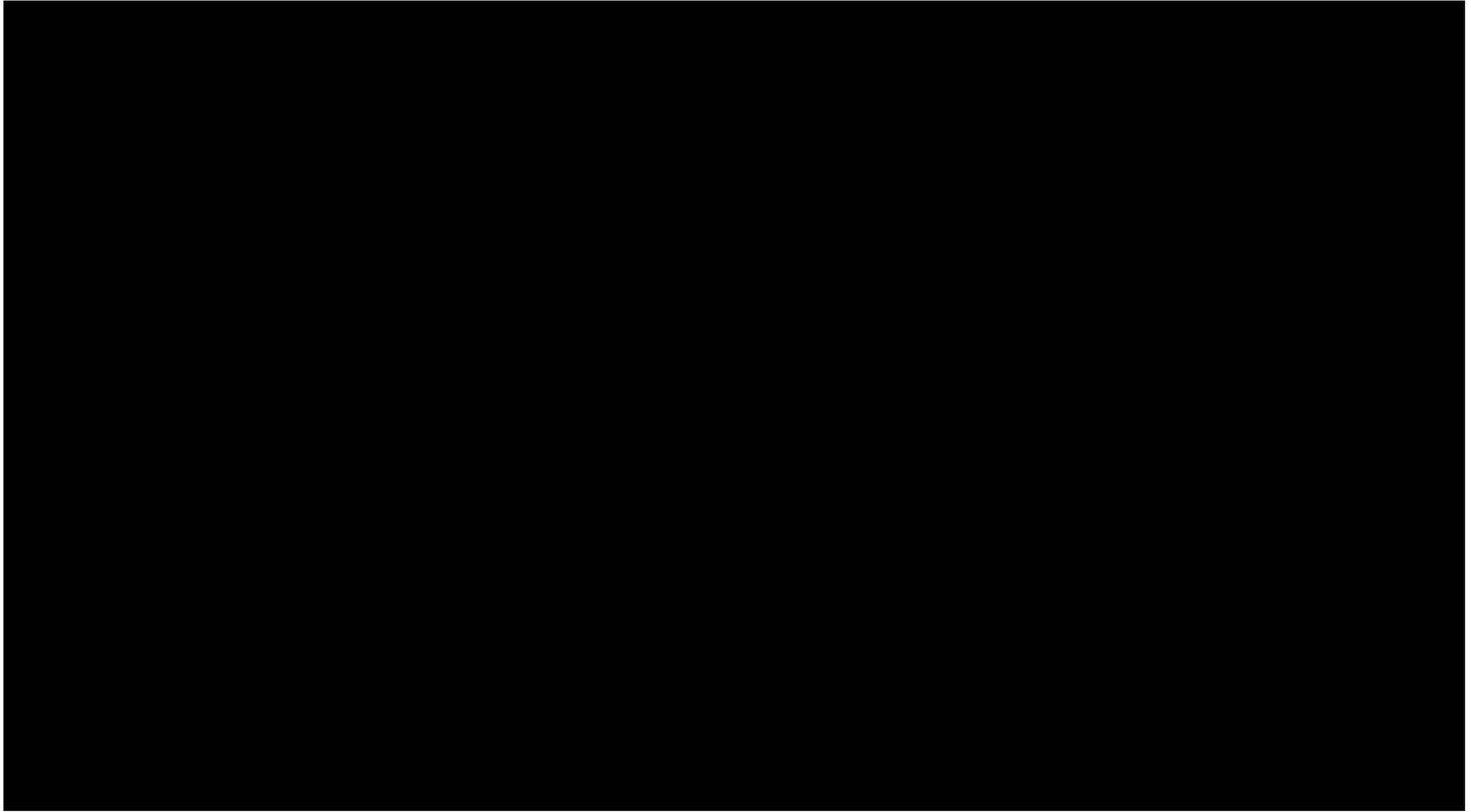
March 5, 2002



March 7, 2002



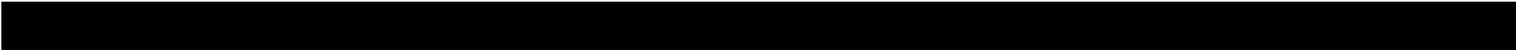
# Physical Model: iceberg behaviour



# Physical Model: iceberg behaviour



# Physical Model: iceberg behaviour

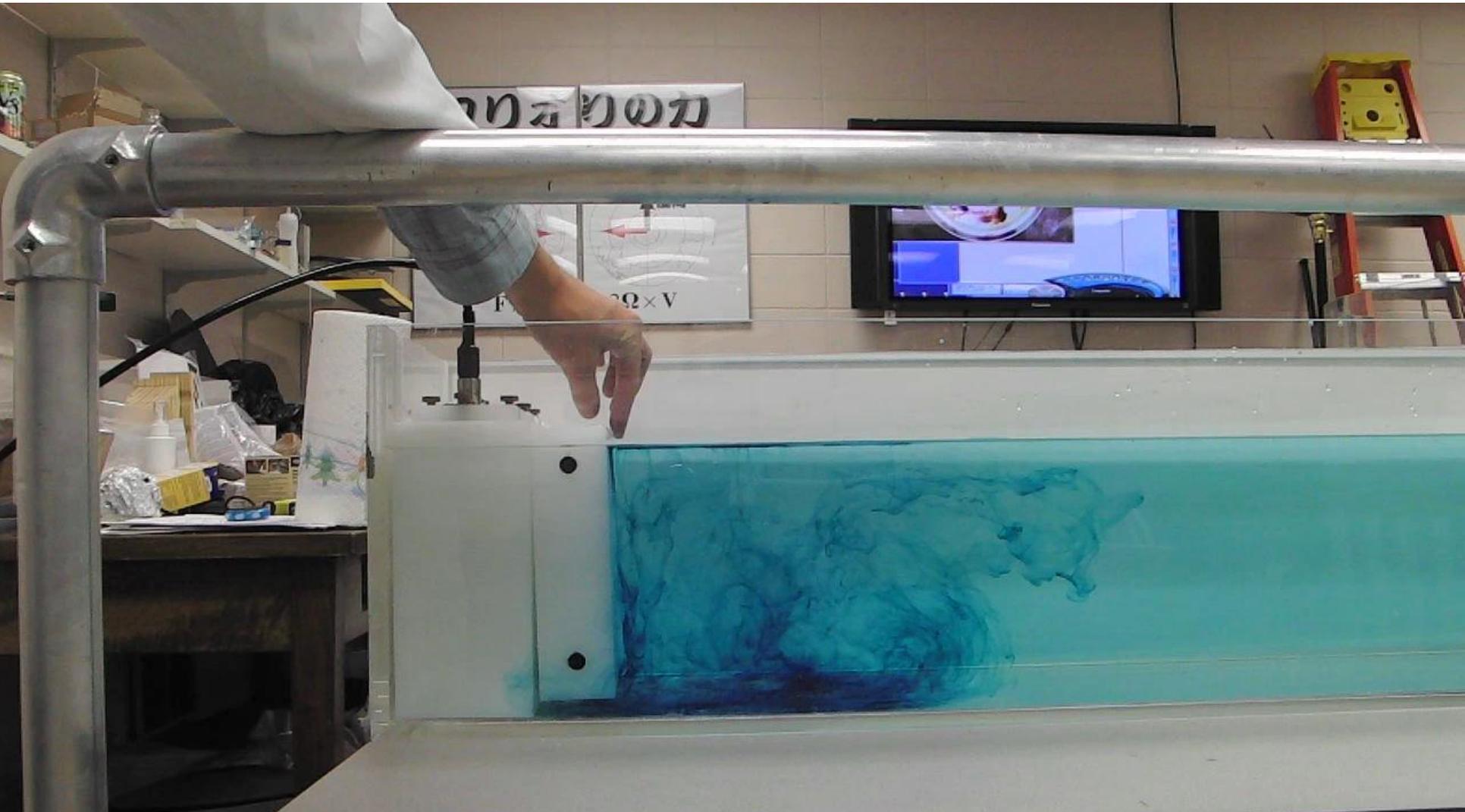


Sermeq Kujalleq - Ilulissat Glacier - Jakobshavn Isbrae  
5 June 2007  
14:10 - 14:28 UTC

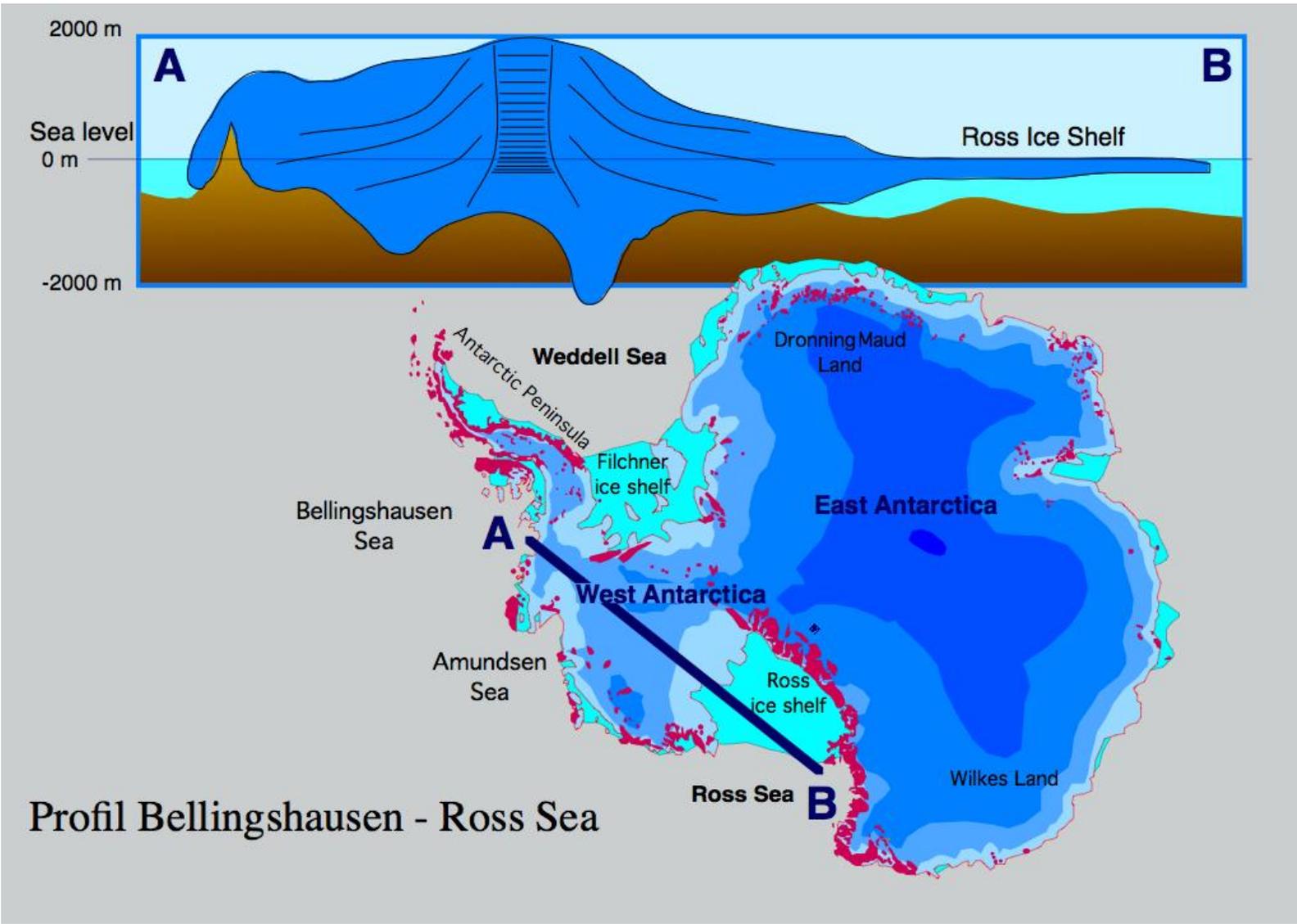
Photos by Jason Amundson  
University of Alaska Fairbanks



**Physical Model:** iceberg behaviour



# Physical Model: ice shelves



Profil Bellingshausen - Ross Sea

# Floating Extensional Flows

Newtonian *versus* non-Newtonian

Roiy Sayag

Samuel S. Pegler

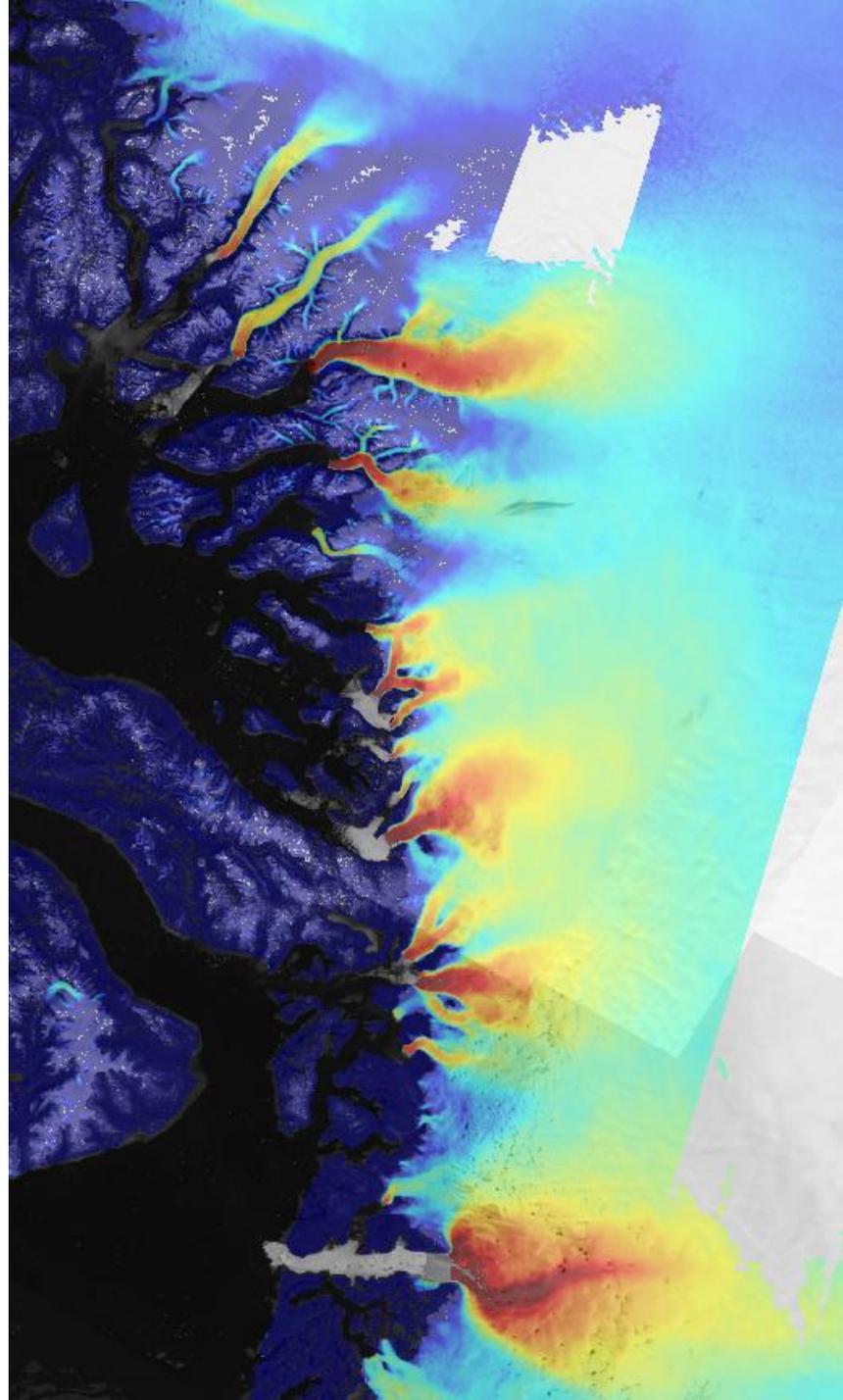
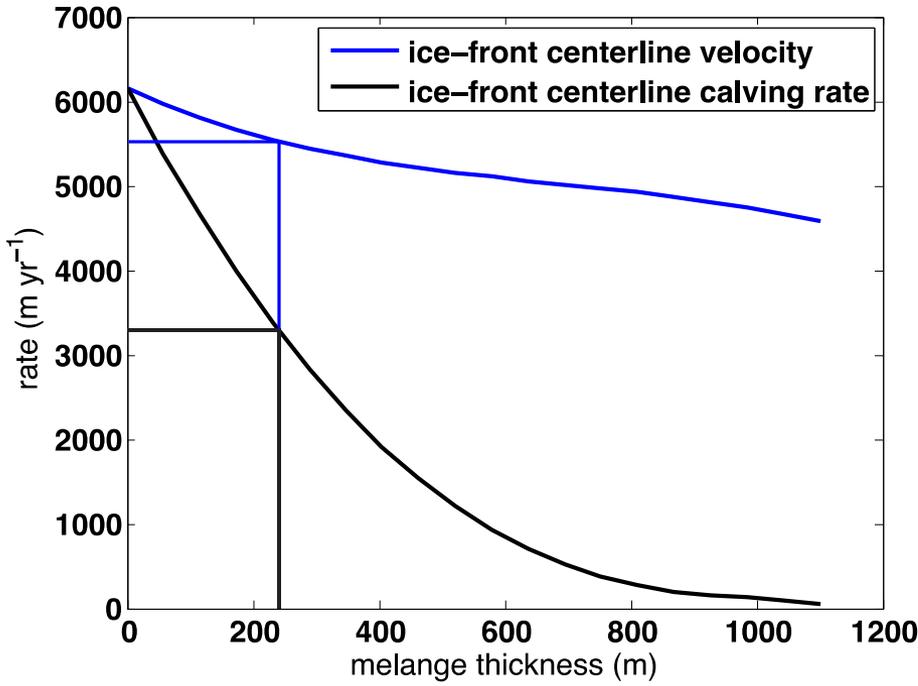
M. Grae Worster

Department of Applied Mathematics and Theoretical Physics  
University of Cambridge

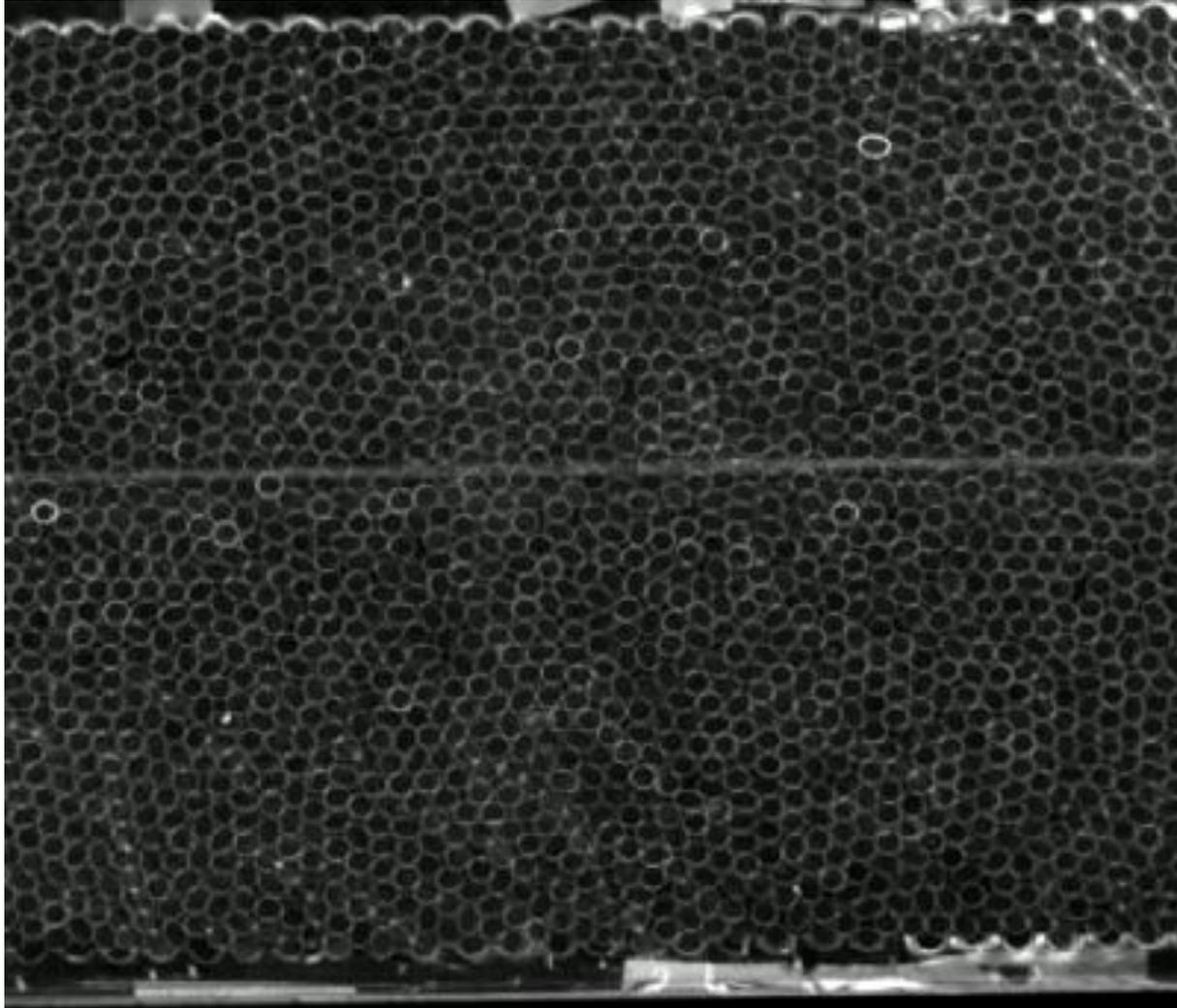
# Physical Model: future directions?

**melange**: mixture of icebergs, sea ice in outlet glacier fjord

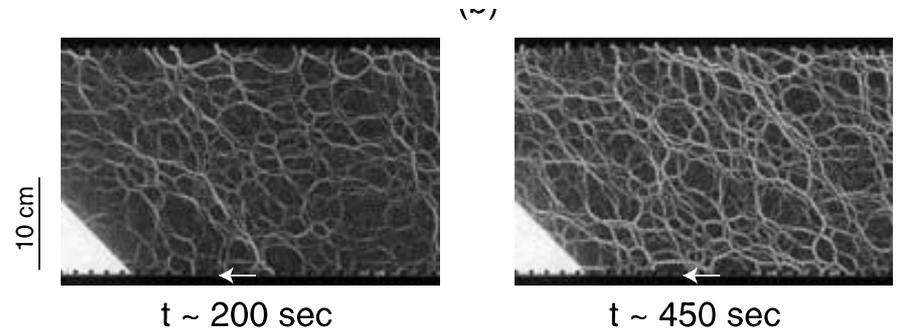
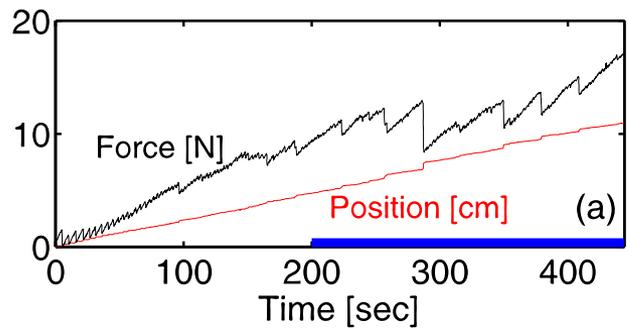
- influences calving rate and glacier velocity



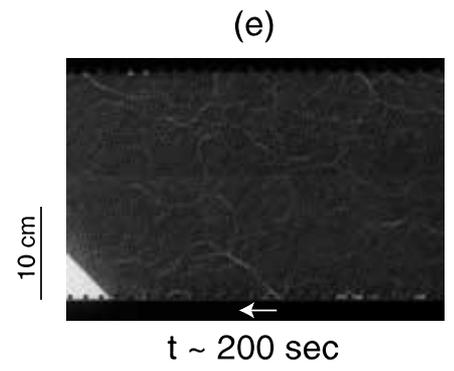
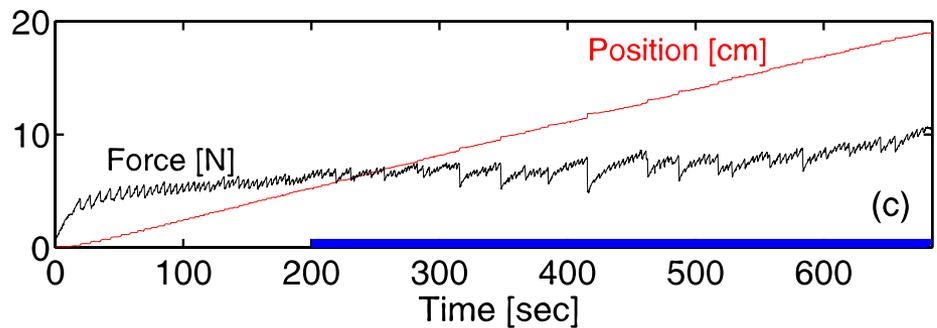
## Physical Model: future directions?

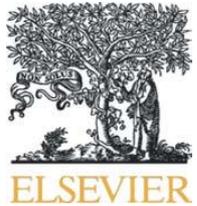


# Physical Model: future directions?



## Dilational





Contents lists available at [ScienceDirect](#)

## Earth-Science Reviews

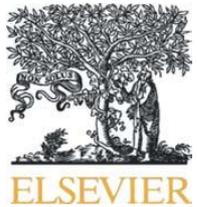
journal homepage: [www.elsevier.com/locate/earscirev](http://www.elsevier.com/locate/earscirev)



### The “unreasonable effectiveness” of stratigraphic and geomorphic experiments

Chris Paola <sup>a,\*</sup>, Kyle Straub <sup>a,b</sup>, David Mohrig <sup>c</sup>, Liam Reinhardt <sup>d</sup>

- We can easily be convinced of the utility of physical experiments
  - evolve under controlled conditions
  - can examine the independent control from changing a single variable
  - can provide a greater degree of measurement not possible in the field
  - can speed up time



Contents lists available at [ScienceDirect](#)

## Earth-Science Reviews

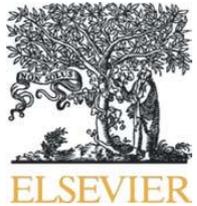
journal homepage: [www.elsevier.com/locate/earscirev](http://www.elsevier.com/locate/earscirev)



### The “unreasonable effectiveness” of stratigraphic and geomorphic experiments

Chris Paola <sup>a,\*</sup>, Kyle Straub <sup>a,b</sup>, David Mohrig <sup>c</sup>, Liam Reinhardt <sup>d</sup>

- Skepticism arises from concerns about how representative these systems are (i.e. scaling)
  - most experiments fall short of full dynamic scaling – but still capture the essence of many important processes in natural systems



Contents lists available at [ScienceDirect](#)

## Earth-Science Reviews

journal homepage: [www.elsevier.com/locate/earscirev](http://www.elsevier.com/locate/earscirev)



### The “unreasonable effectiveness” of stratigraphic and geomorphic experiments

Chris Paola <sup>a,\*</sup>, Kyle Straub <sup>a,b</sup>, David Mohrig <sup>c</sup>, Liam Reinhardt <sup>d</sup>

- Paola and others argue for a broader view including the idea of natural similarity
  - argues for abandonment of the term ‘physical model’ or ‘analogue model’ since a model is an idealization or theory about how nature works.
  - these experiments are a part of nature, however simplified or reduced in scale they may be